

An *Unofficial* BOSS DR12 Analysis: Cosmology from the Galaxy Power Spectrum and Bispectrum

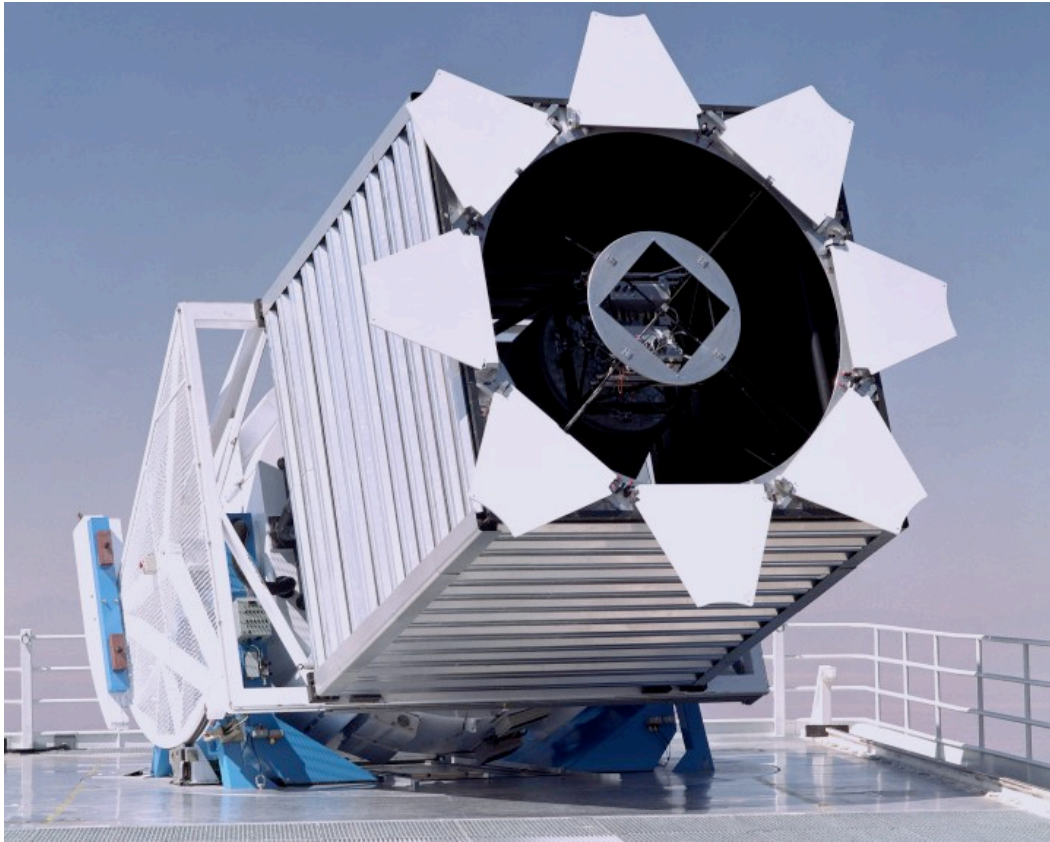
Oliver Philcox (Princeton / IAS)

Misha Ivanov (IAS)

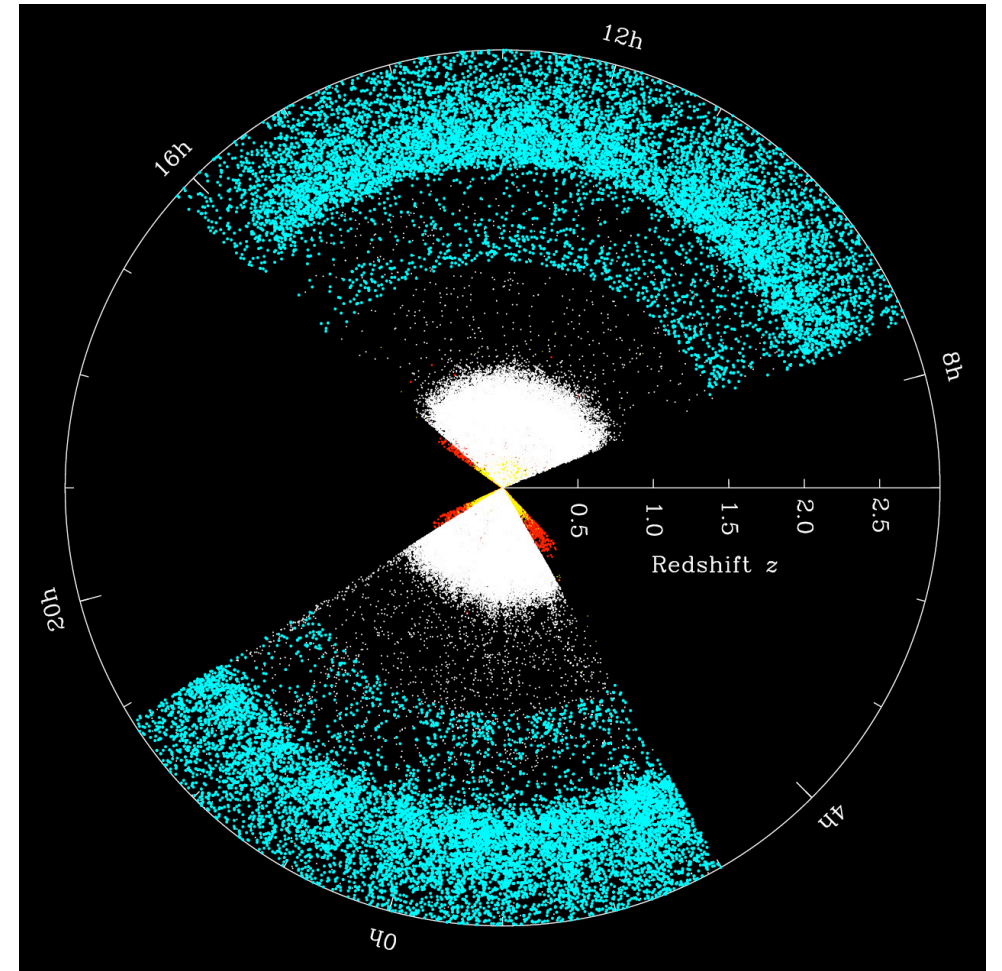
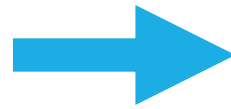
*with Giovanni Cabass (IAS), Marko Simonovic (CERN),
and Matias Zaldarriaga (IAS)*



COSMOLOGY FROM SPECTROSCOPIC SURVEYS



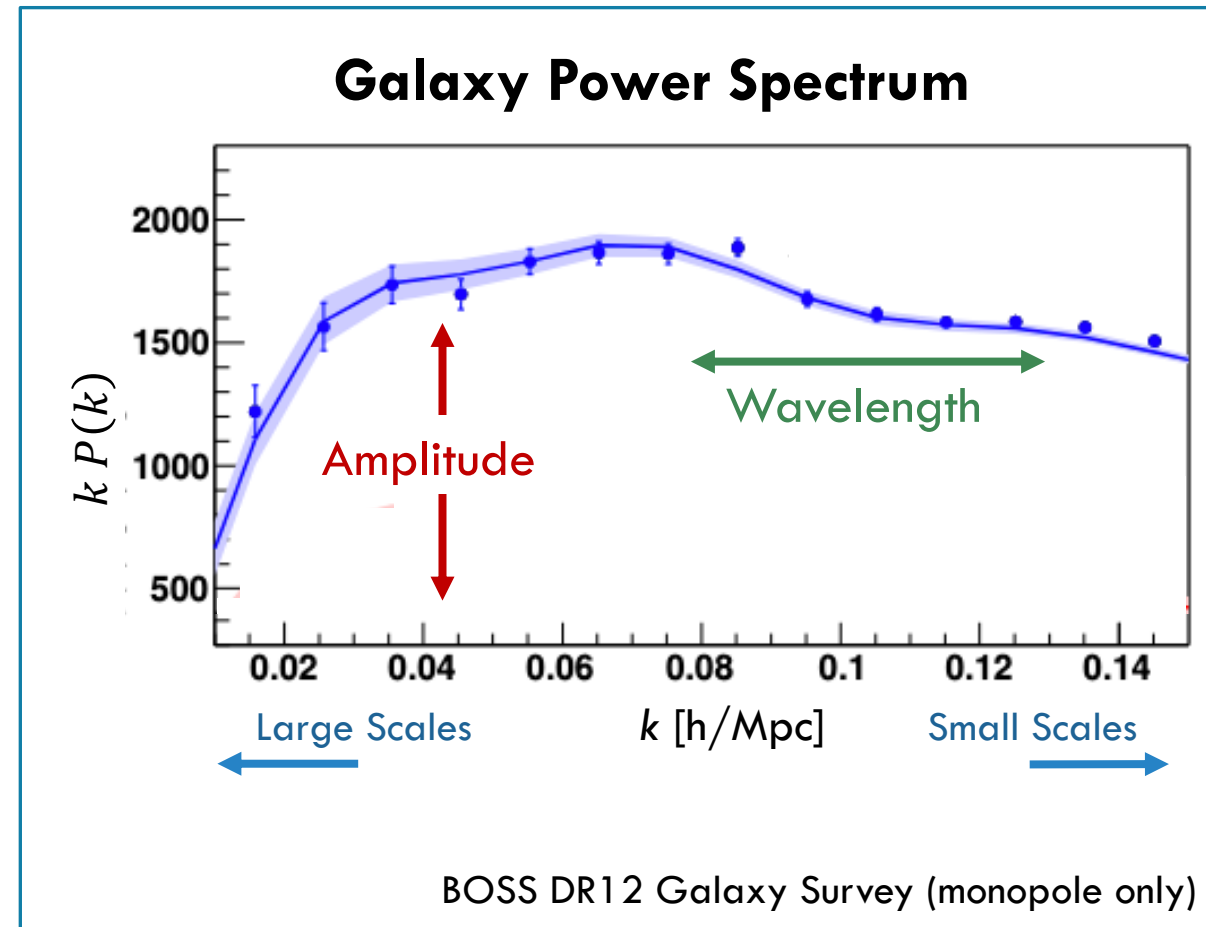
Big Telescope



10^6 Galaxy Positions

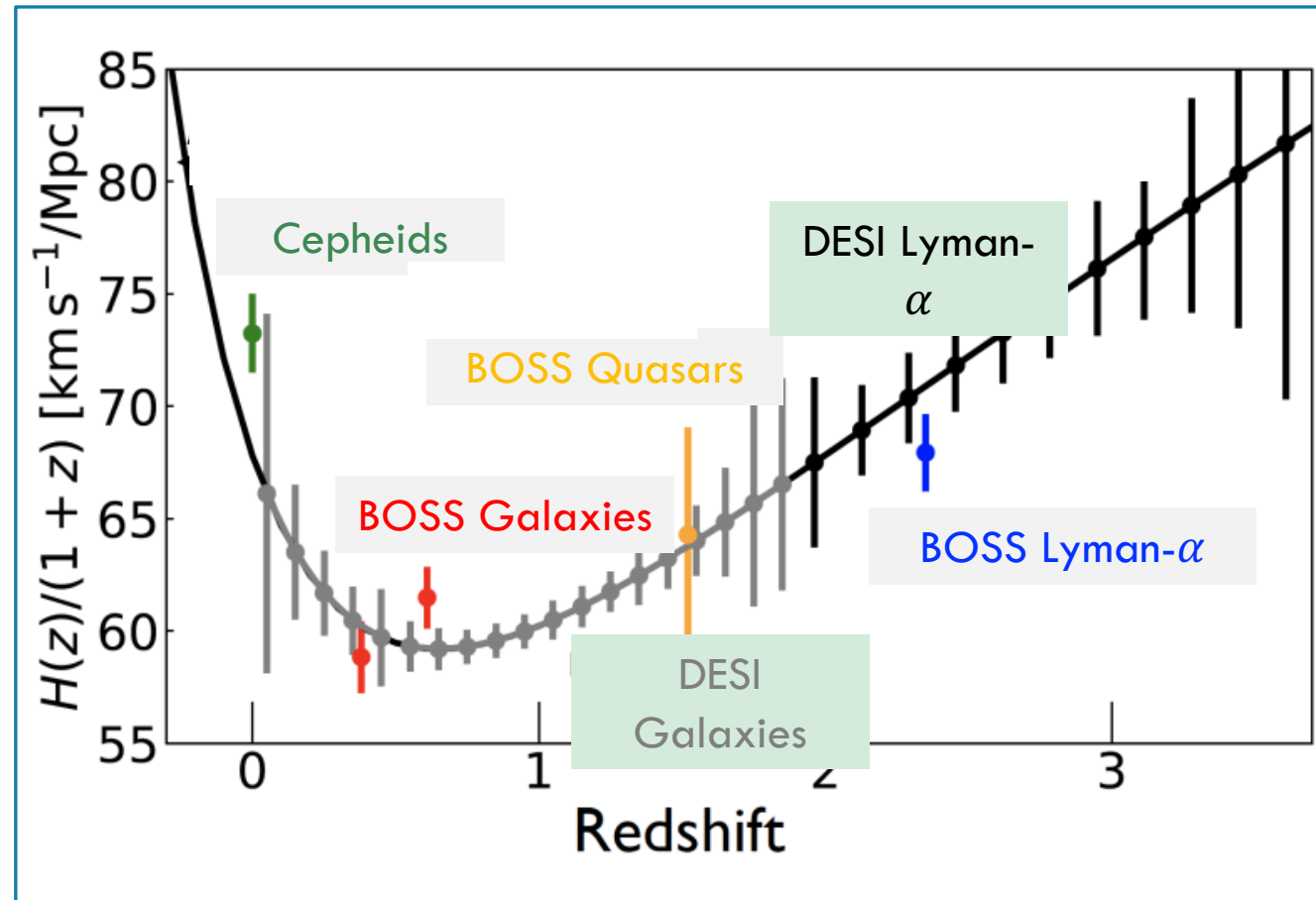
WHAT DO WE DO WITH THE DATA?

- ▶ Compress the 10^6 galaxy positions to a **power spectrum**
- ▶ Use a **scaling analysis** to measure:
 - ▶ Overall **amplitude** (= primordial amplitude)
 - ▶ **Wiggle** positions (= BAO feature)
- ▶ Robust way to constrain **growth rate** and **expansion history**, $H(z)$



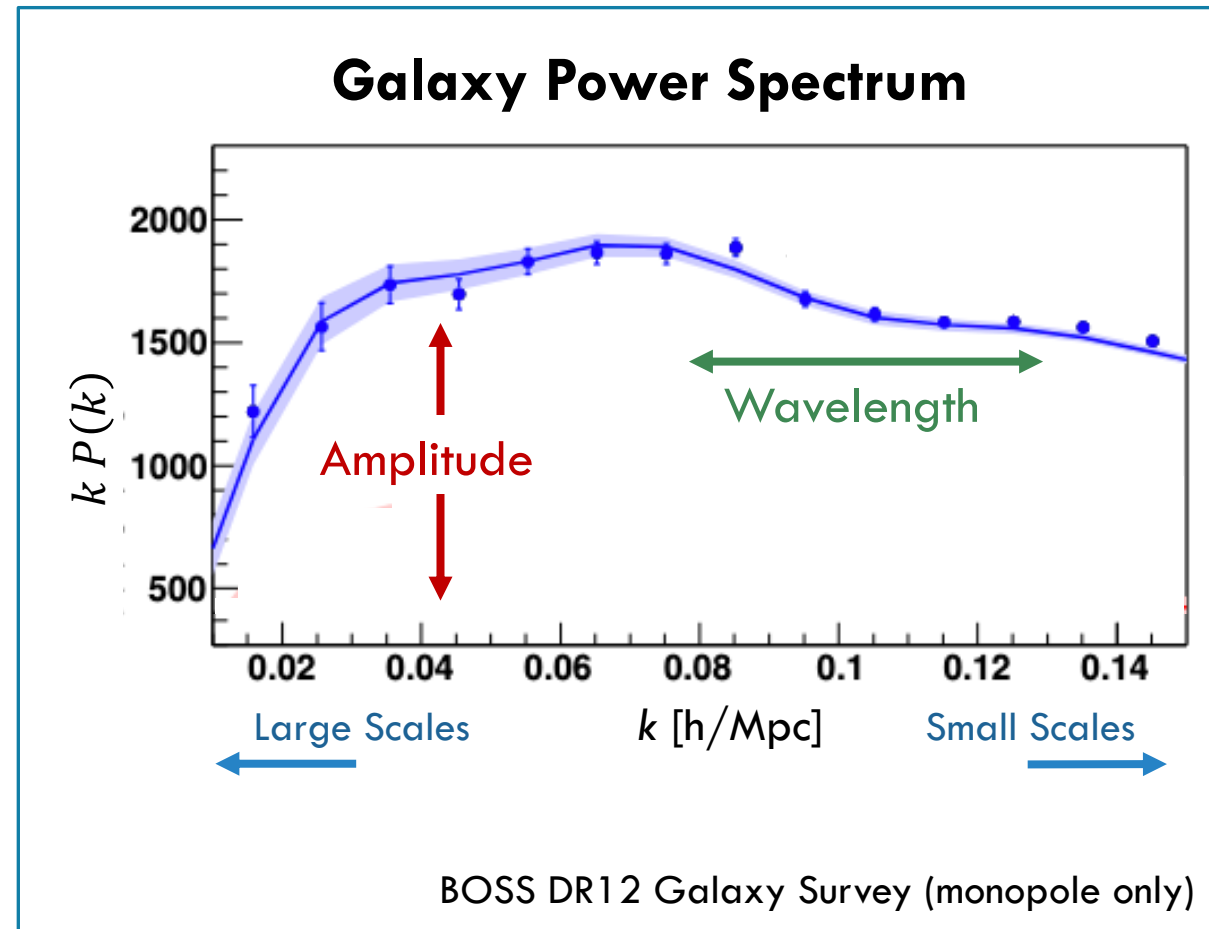
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WHAT COULD WE DO WITH THE DATA?

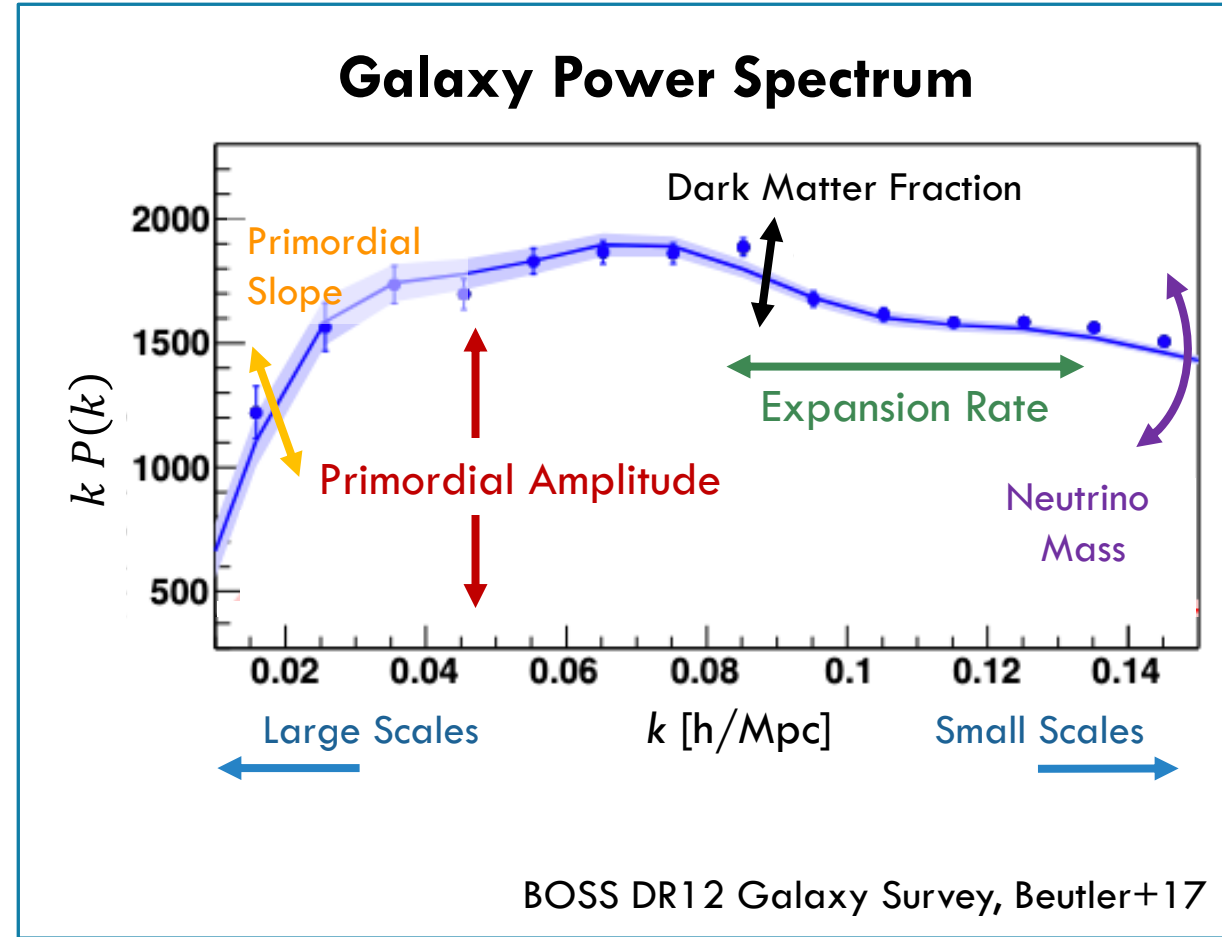
▷ This is *not* all the available information!



WHAT COULD WE DO WITH THE DATA?

- ▶ This is *not* all the available information!
- ▶ Measure parameters **directly** from the **full shape** of the galaxy power spectrum
- ▶ This is just like for the CMB!

This needs an accurate theory model...



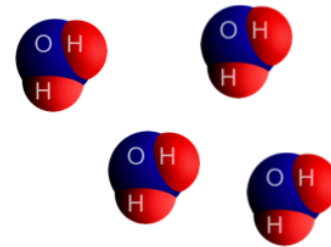
THE EFFECTIVE FIELD THEORY OF LARGE SCALE STRUCTURE

- ▷ **Analytic** theory for $\delta(\mathbf{x})$, based on the **fluid equations**

$$\dot{v}^i + H v^i + v^j \delta_j v^i = \frac{1}{\rho} \delta_j \tau^{ij}$$

This includes:

- ▷ **Back-reaction** of small-scale physics on large-scale modes
- ▷ Long-wavelength displacements
- ▷ Galaxy bias
- ▷ Redshift-space distortions
- ▷ Primordial non-Gaussianity etc.



large
scales



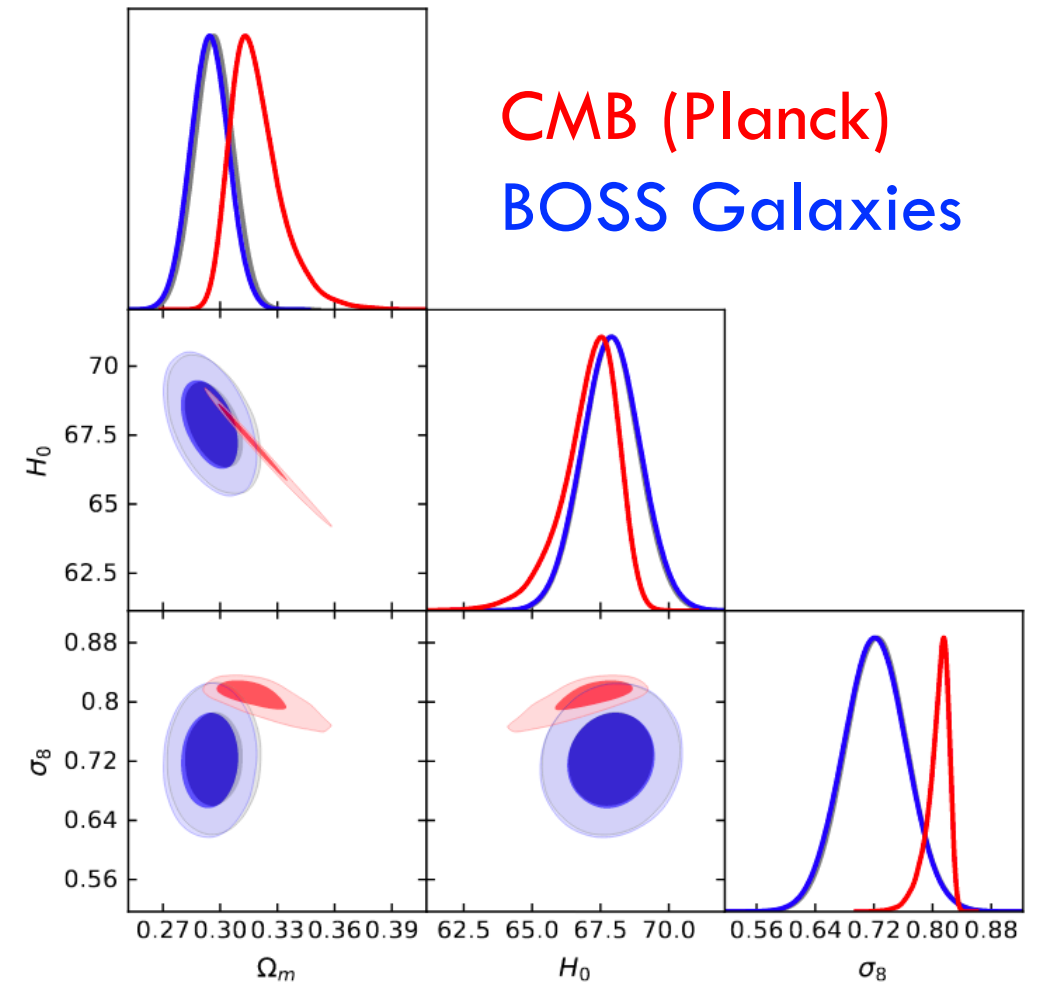
Arbitrarily accurate on large scales!

WHAT COULD WE DO WITH THE DATA?

▶ Theory tested at **high precision** in blind mock challenges → it works!

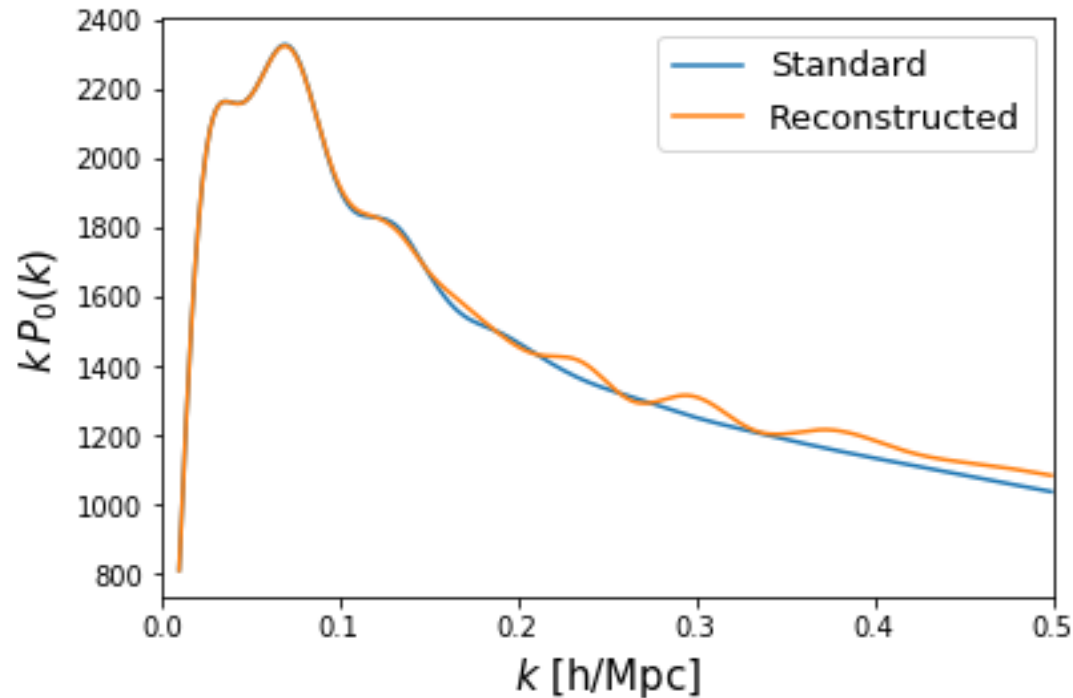
▶ Applied to **BOSS power spectra**

	H_0	Ω_m	σ_8
BOSS 2021	68.8 ± 1.2	0.32 ± 0.01	0.73 ± 0.04
Planck 2018 (TT, TE, EE, low-l, lensing)	67.4 ± 0.5	0.315 ± 0.007	0.811 ± 0.006



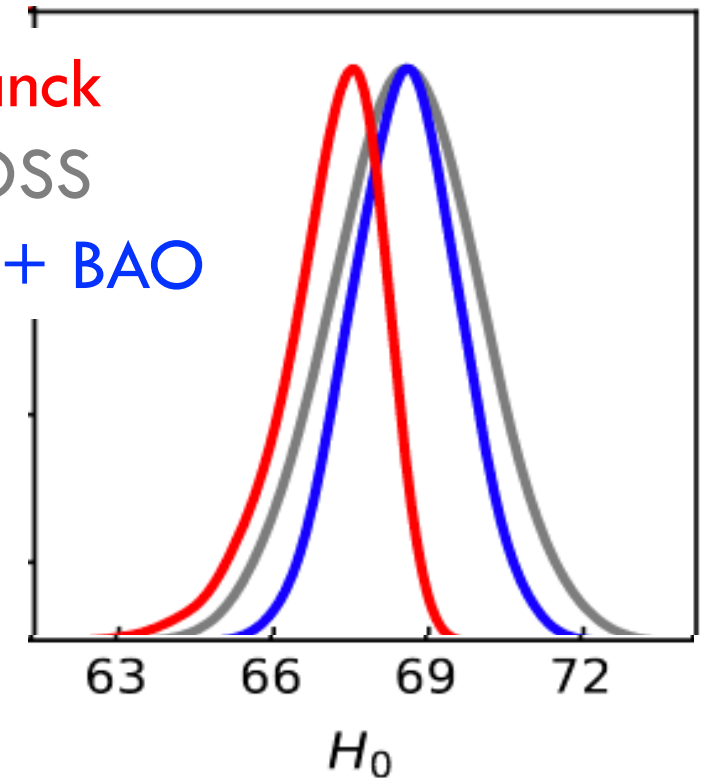
WHAT ELSE CAN WE DO WITH THE DATA?

Add the **wiggly** information from **baryon acoustic oscillations**



40% better H_0 !

Planck
BOSS
BOSS + BAO



WHAT ELSE CAN WE DO WITH THE DATA?

Add the **real-space** power spectrum

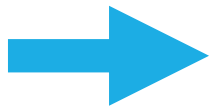
$$P_0(k)$$

+

$$P_2(k)$$

+

$$P_4(k)$$

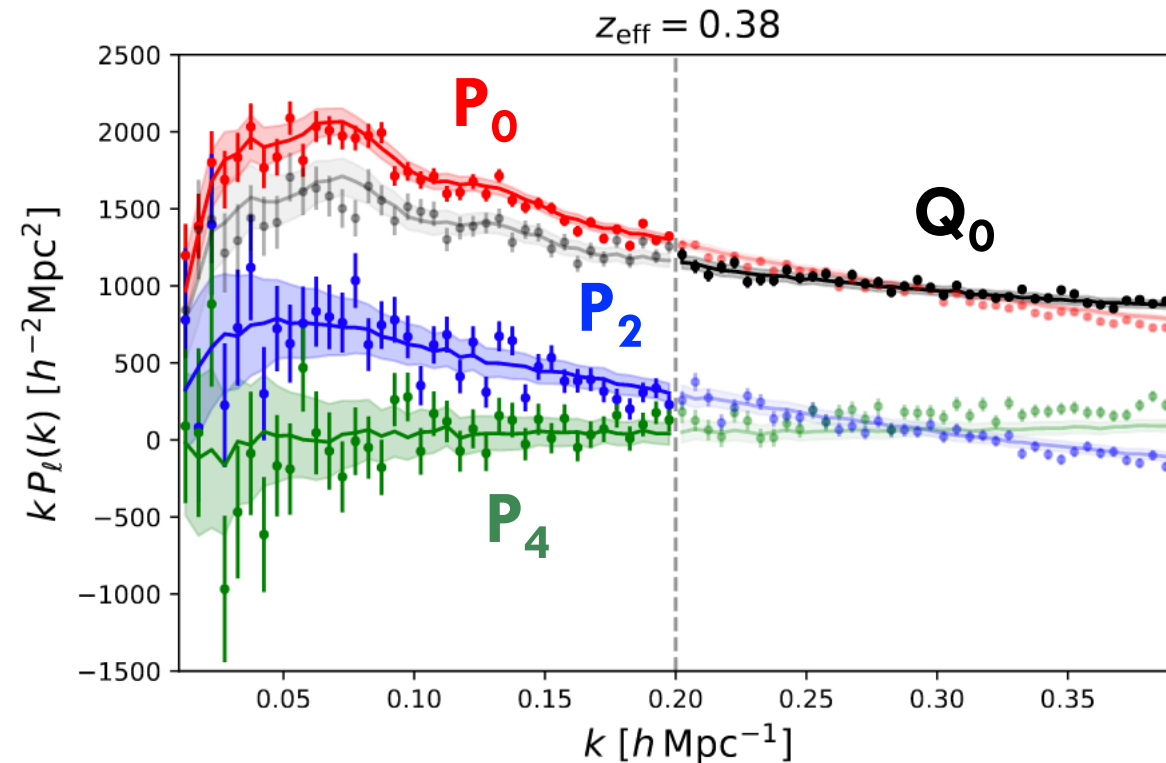


$$Q_0(k)$$

\approx

$$P(k, \mu = 0)$$

- No Fingers-of-God!
- Push to $k_{\max} = 0.4h/\text{Mpc}$
- Constraints improve by (10 – 100)%



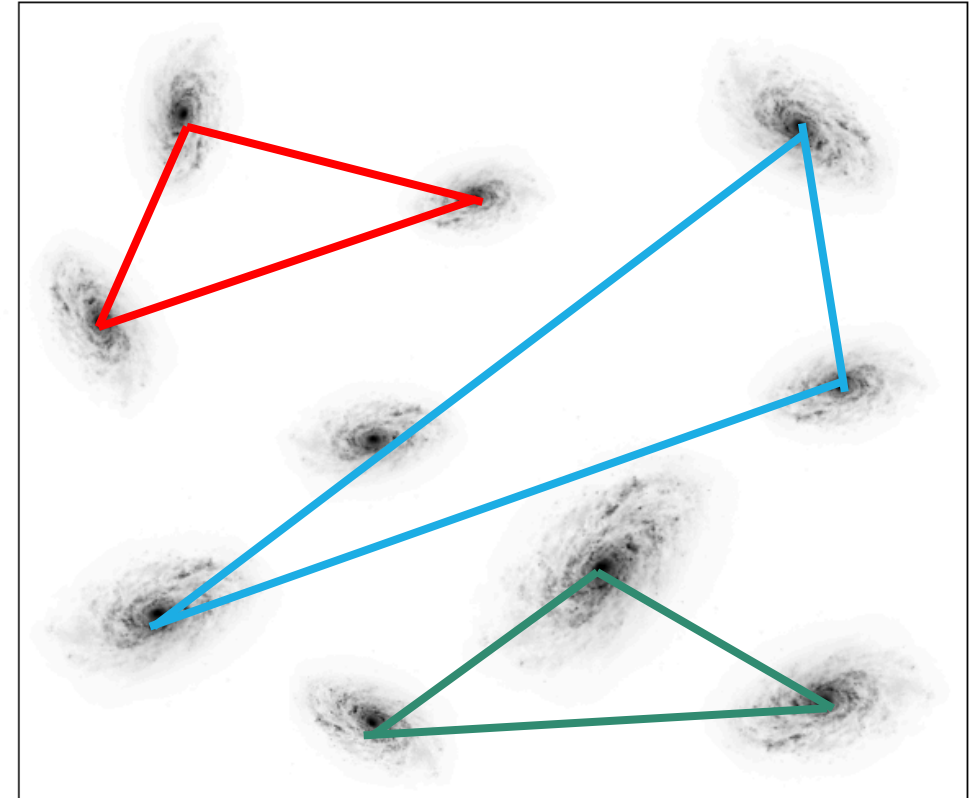
WHAT ELSE CAN WE DO WITH THE DATA?

Add the **galaxy bispectrum**:

$$B_g(k_1, k_2, k_3) = \langle \delta_g(\mathbf{k}_1) \delta_g(\mathbf{k}_2) \delta_g(\mathbf{k}_3) \rangle'$$

This is hard:

- Window functions
- Theory model



THE MASKED BISPECTRUM

Problem: We don't measure the density field directly.

$$\delta_g(\mathbf{r}) \rightarrow W(\mathbf{r})\delta_g(\mathbf{r}) \quad \delta_g(\mathbf{k}) \rightarrow \int \frac{d\mathbf{p}}{(2\pi)^3} W(\mathbf{k} - \mathbf{p})\delta_g(\mathbf{p})$$

Window Function

The measured bispectrum is a **triple convolution**

$$B_g(\mathbf{k}_1, \mathbf{k}_2) \rightarrow \int_{\mathbf{p}_1 \mathbf{p}_2} W(\mathbf{k}_1 - \mathbf{p}_1)W(\mathbf{k}_2 - \mathbf{p}_2)W(\mathbf{p}_1 + \mathbf{p}_2 - \mathbf{k}_1 - \mathbf{k}_2)B_g(\mathbf{p}_1, \mathbf{p}_2)$$

Solution: Convolve the **theory model** too

This is too expensive to do properly!



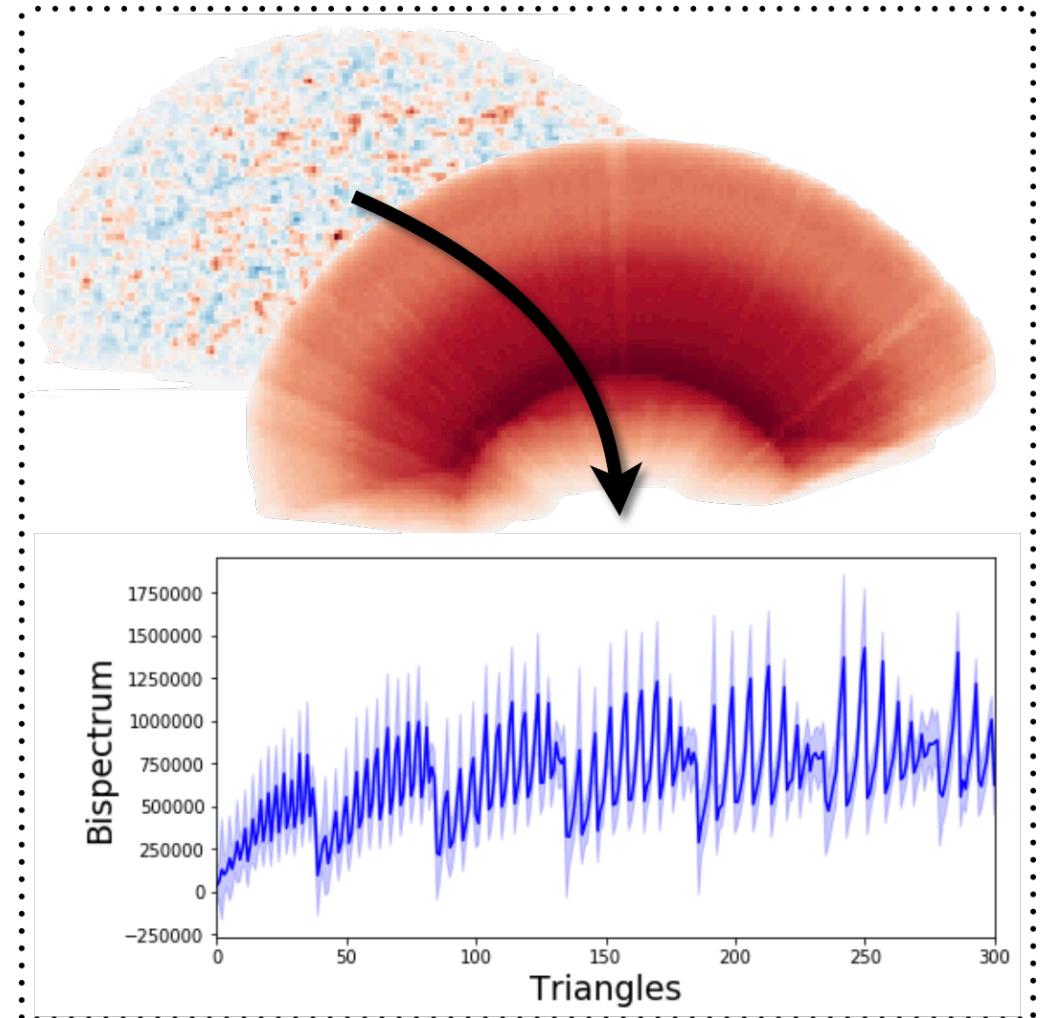
BISPECTRA WITHOUT WINDOWS

Alternatively: estimate the **unwindowed** bispectrum directly

$$B_g^{\text{win}}(\mathbf{k}_1, \mathbf{k}_2) = \int_{\mathbf{p}_1 \mathbf{p}_2} W(\mathbf{k}_1 - \mathbf{p}_1) W(\mathbf{k}_2 - \mathbf{p}_2) W(\mathbf{p}_1 + \mathbf{p}_2 - \mathbf{k}_1 - \mathbf{k}_2) B_g(\mathbf{p}_1, \mathbf{p}_2)$$

- ▶ Derive a **maximum-likelihood** estimator for the **true** bispectrum
- ▶ Effectively **deconvolves** the window

$$\nabla_{B_g} L[\text{data} | B_g] = 0 \quad \Rightarrow \quad \hat{B}_g = \dots$$



MODELLING THE BISPECTRUM

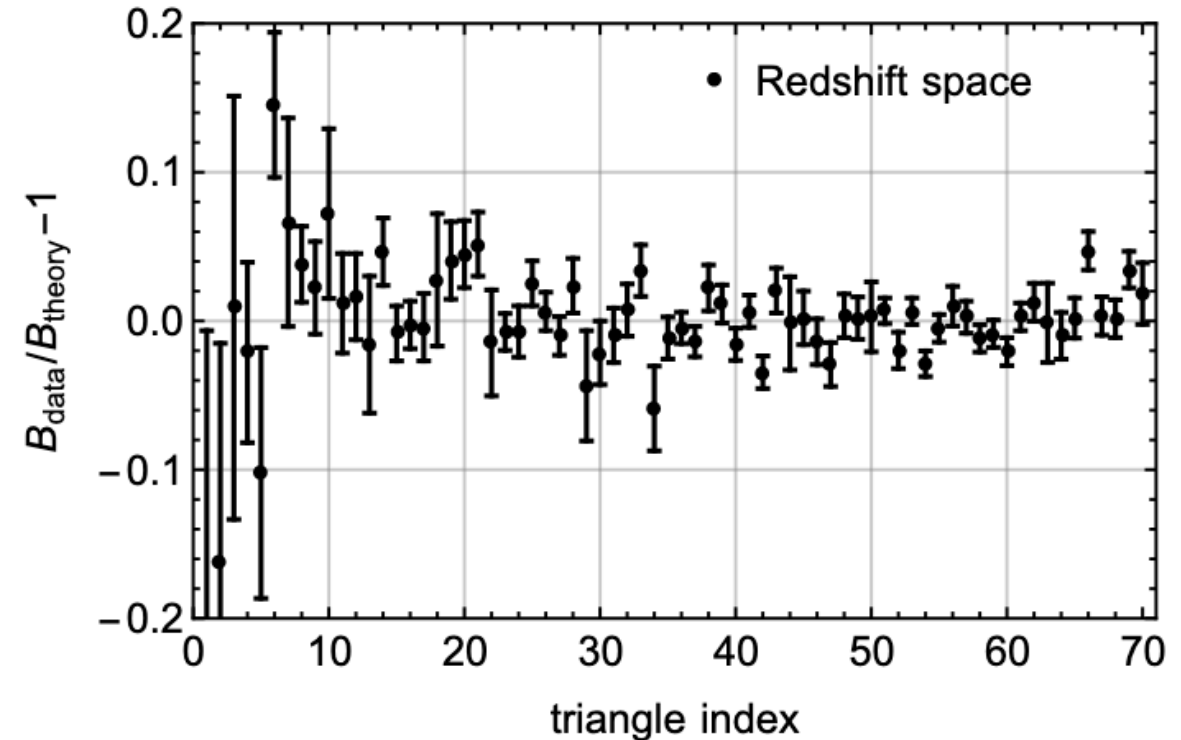
Model:

- Tree-level theory
- Second-order galaxy bias
- Large-scale displacements
- Coordinate transformations
- Fingers-of-God

Tested on 566 (Gpc/h)^3 simulations

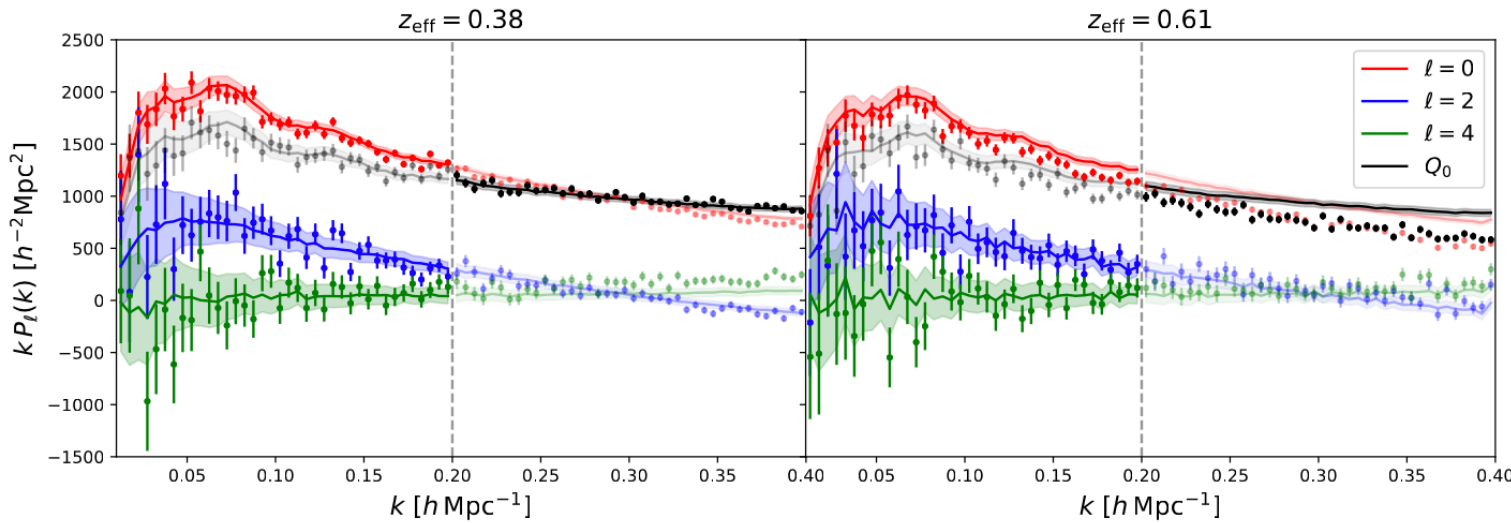
Accurate up to $k_{max} = 0.08 \text{ h/Mpc}$

Data \div Theory -1

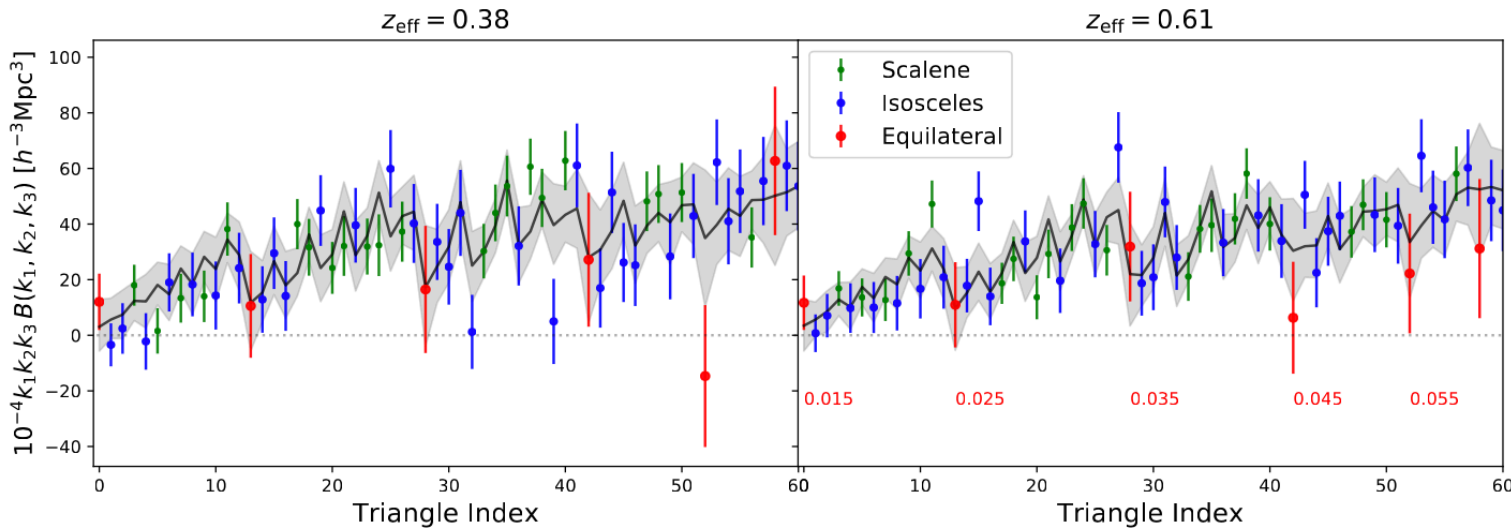


THE UNOFFICIAL BOSS DR12 ANALYSIS

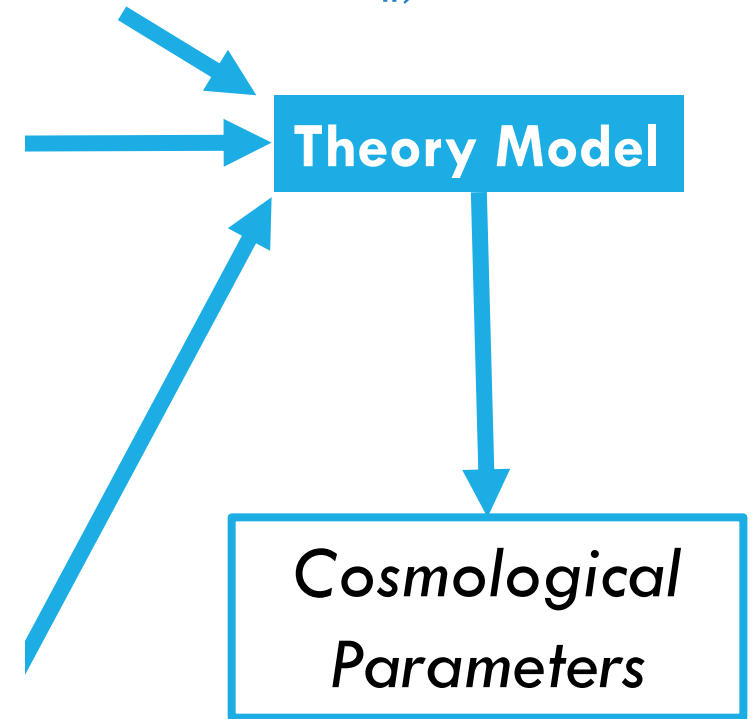
$P_\ell + Q_0$



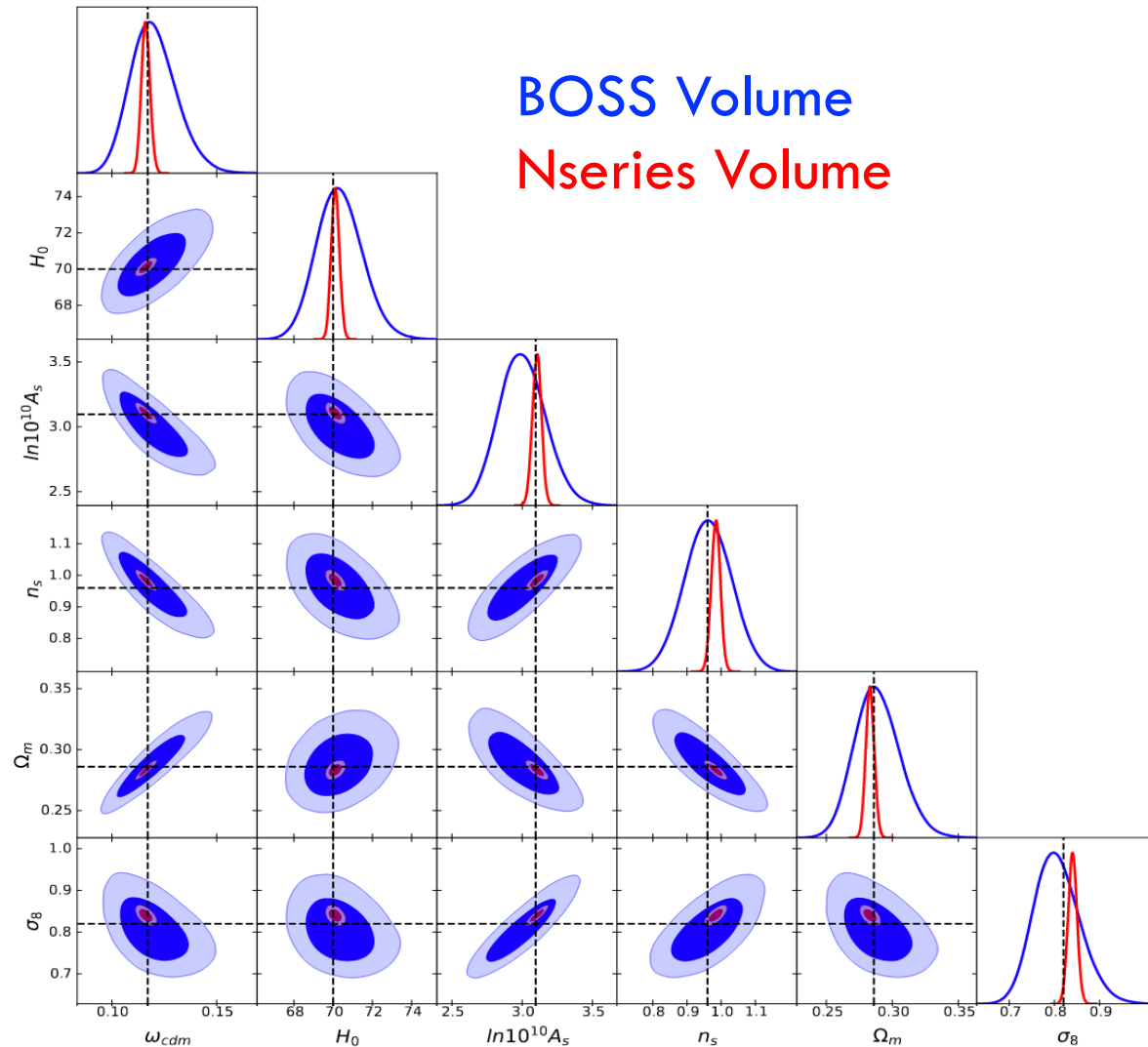
Bispectrum



Wiggles ($\alpha_{\parallel, \perp}$)



THE UNOFFICIAL BOSS DR12 ANALYSIS - TESTING



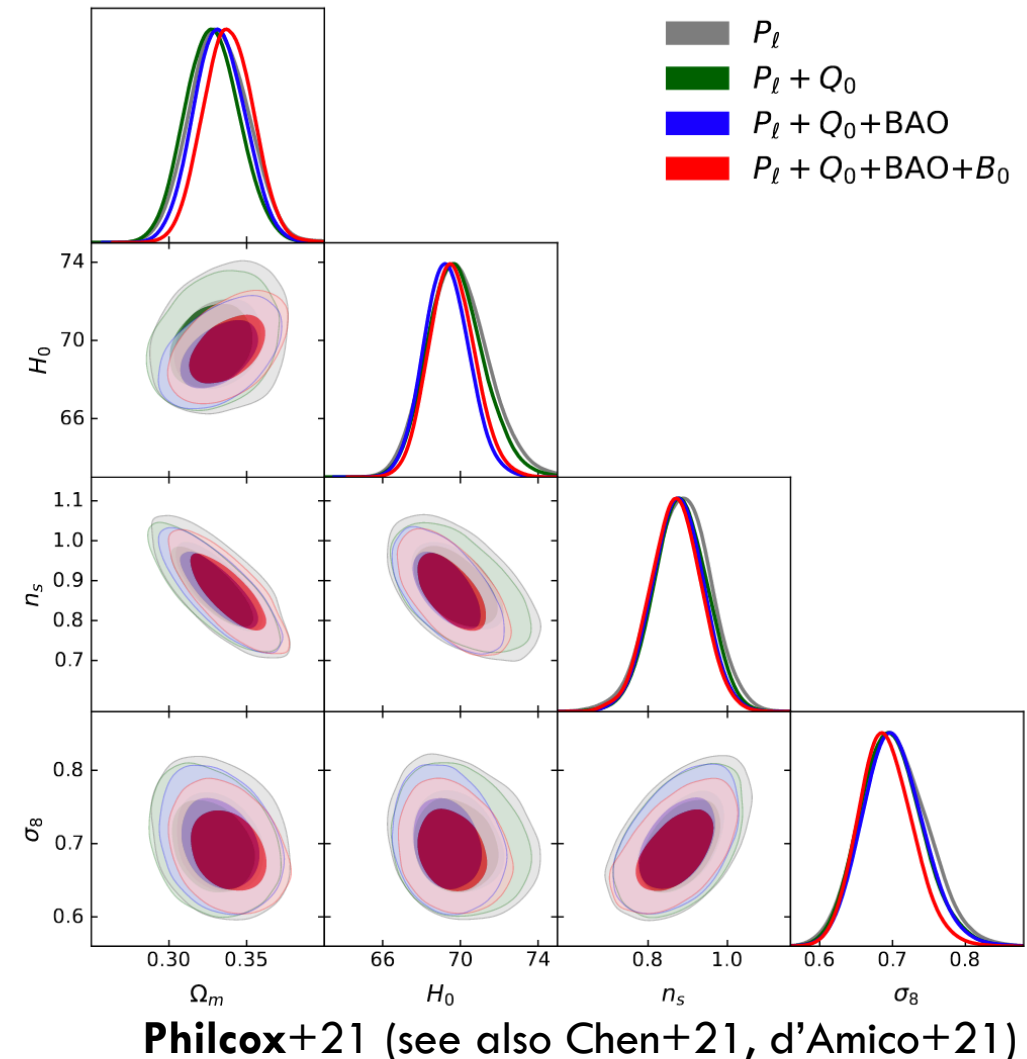
Validate with **Nseries** mocks

- All parameters recovered at $\ll 1\sigma$
- Theory model works!
- Window function works!
- Fiber collisions work!

THE UNOFFICIAL BOSS DR12 ANALYSIS - RESULTS

- Λ CDM analysis gives **tight** parameter constraints
- H_0 agrees with *Planck*
- $S_8 = 0.75 \pm 0.04$ agrees with weak lensing

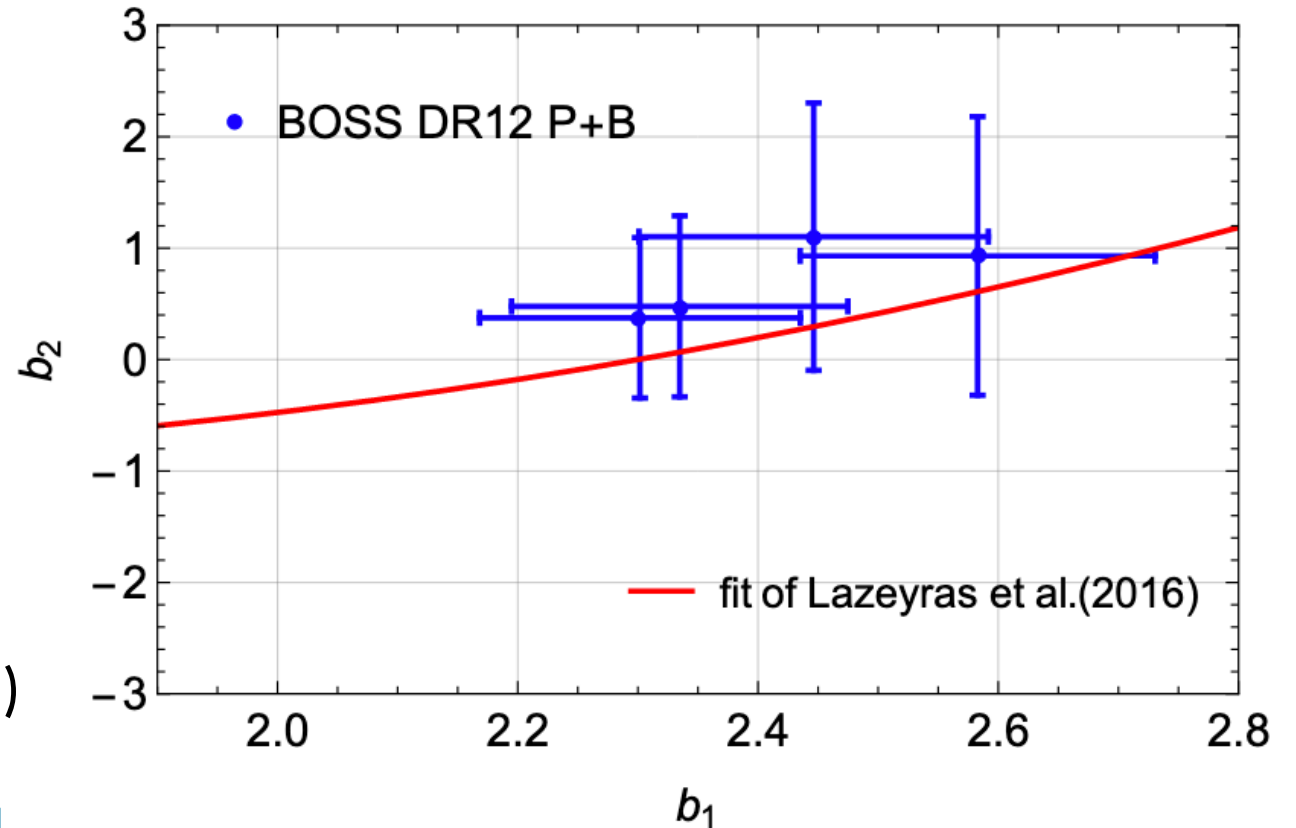
	H_0	Ω_m	σ_8
BOSS Pk	68.8 ± 1.2	0.32 ± 0.01	0.73 ± 0.04
BOSS All	68.3 ± 0.8	0.32 ± 0.01	0.72 ± 0.03
Planck 2018 (TT, TE, EE, low-l, lensing)	67.4 ± 0.5	0.315 ± 0.007	0.811 ± 0.006



THE UNOFFICIAL BOSS DR12 ANALYSIS

Can constrain **other** parameters:

- $n_s = 0.87 \pm 0.07$
- Neutrino mass
- Sound-Horizon free H_0 measurements
- Bias relations (3x better with bispectra!)



All analysis is public:

github.com/oliverphilcox/full_shape_likelihoods

WHAT'S NEXT?

New / Better Statistics

- **One-Loop** Bispectrum
- Bispectrum **Multipoles**
- Trispectrum
- Correlation Functions?

Apply this to DESI?

New Things to Learn

- Primordial Non-Gaussianity (see Misha's talk)
- Ultra-Light Axions
- Early Dark Energy
- Massive Spinning Particles

and much more...

CONCLUSIONS

- We can **directly** extract cosmological parameters from galaxy surveys
- This will (eventually) become stronger than the CMB
- New statistics give **extra** information and can be robustly **measured & modelled**

arXiv

2112.04515

2110.10161

2110.00006

2002.04035

1909.05277

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