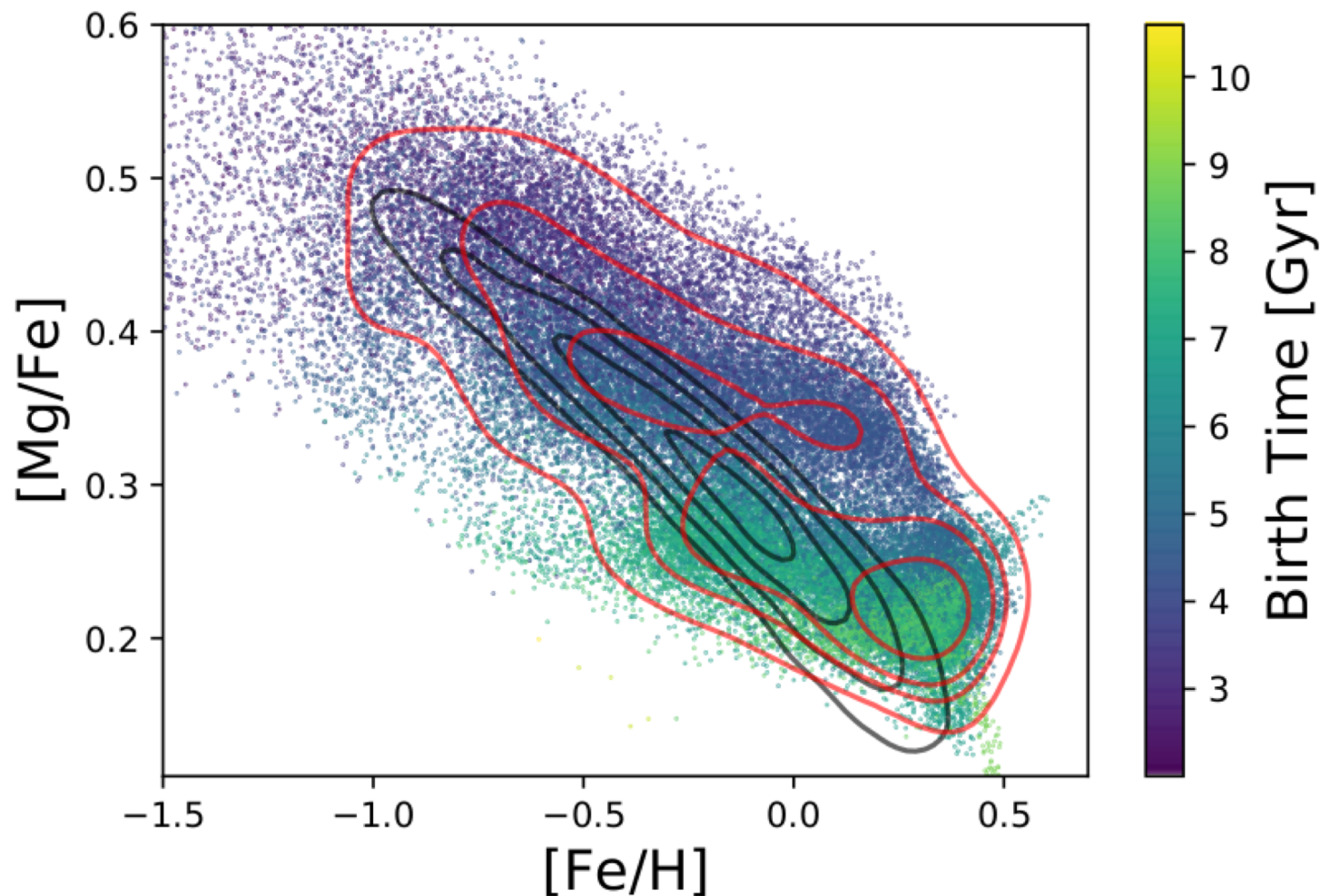




PRINCETON  
UNIVERSITY



# Inferring Galactic Parameters from Chemical Abundances:

A Multi-Star Approach

JAN RYBIZKI (MPIA)

OLIVER PHILCOX (PRINCETON)

JINA-CEE ONLINE SEMINAR

Nov 22, 2019

# Outline

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1. *Chempy*: A Fast and Flexible GCE Model

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2. Choosing Yield Tables for Hydrodynamical Simulations

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4. Inferring Galactic Parameters with Multi-Star Inference

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1. *Chempy*: A Fast and Flexible GCE Model
2. Choosing Yield Tables for Hydrodynamical Simulations
3. Scoring Nucleosynthetic Yield Tables
4. Inferring Galactic Parameters with Multi-Star Inference
5. Further Extensions

# Building a Fast and Flexible Galactic Chemical Evolution Model with *Chempy*

# Building a Fast and Flexible GCE: *Chempy*

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□ *Chempy* (including **chemical yields**, and **SSP** parameters):

**SSP = Simple Stellar Population**  
(A group of stars born at the same time in the same environment)



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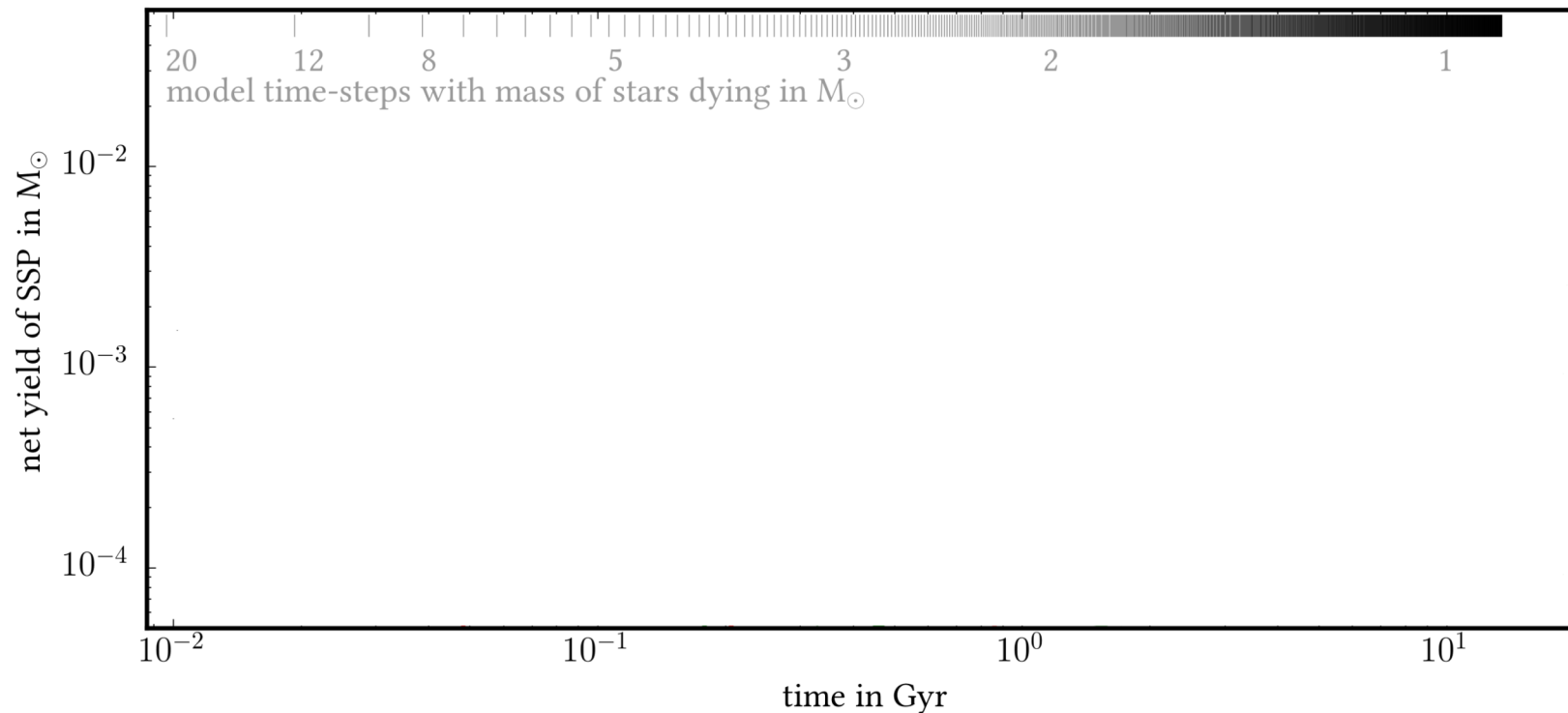
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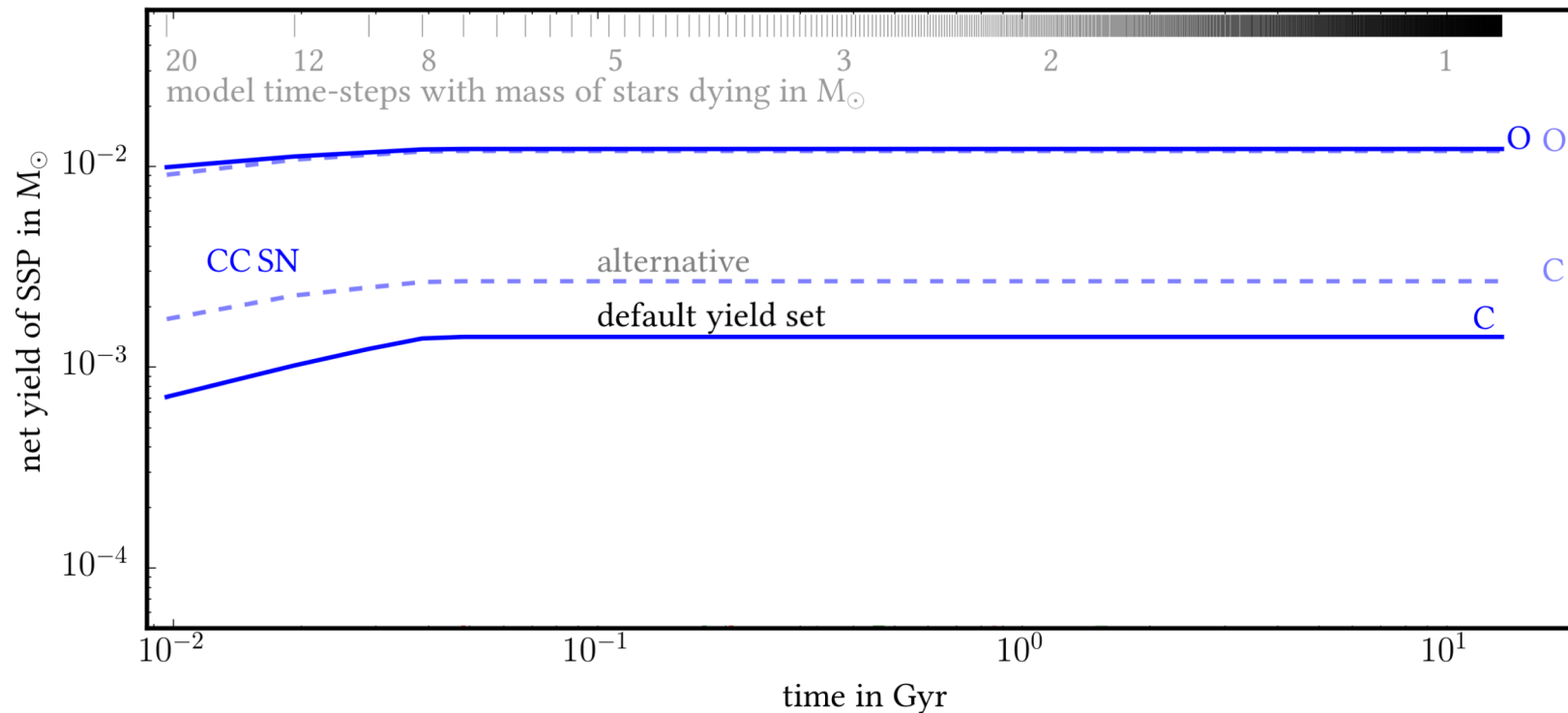


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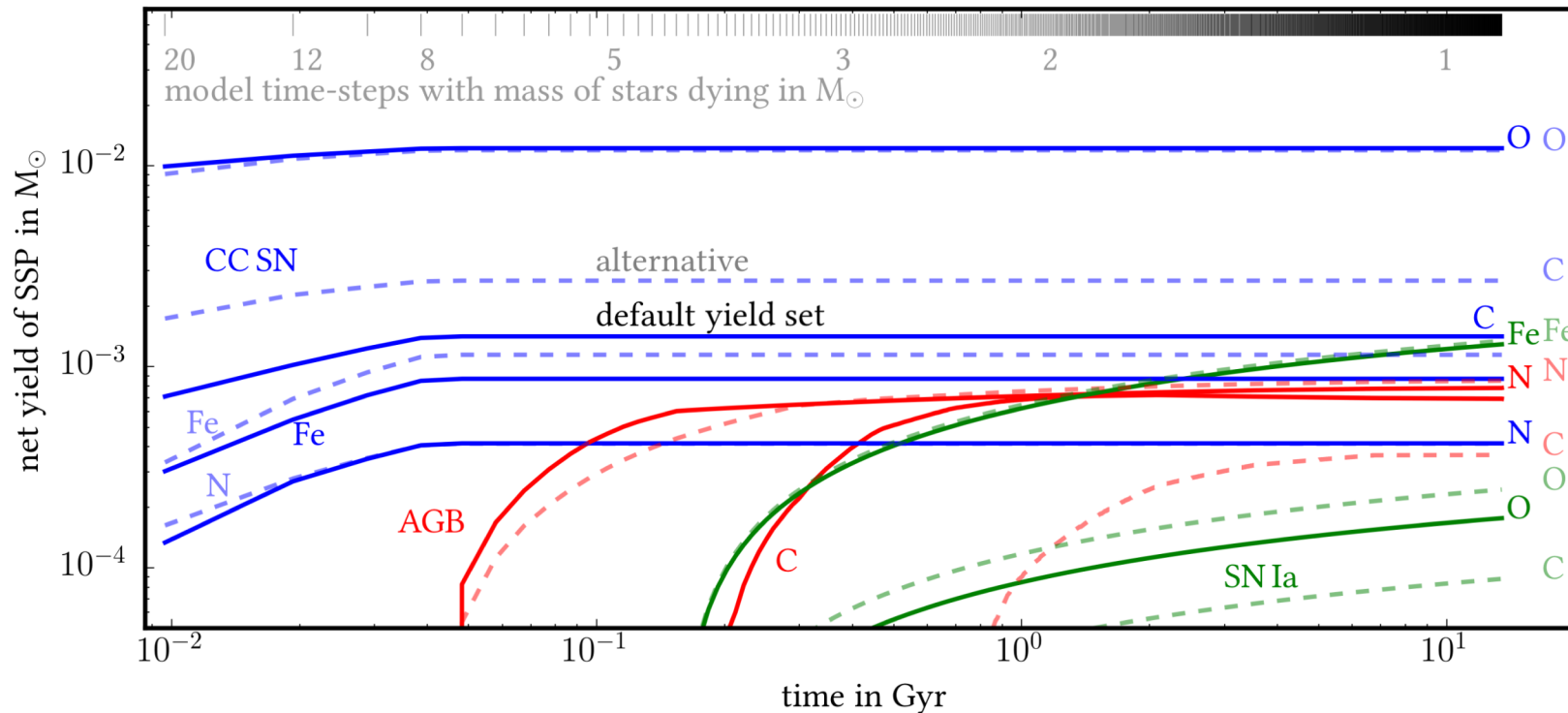


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*ISM (well-mixed)*

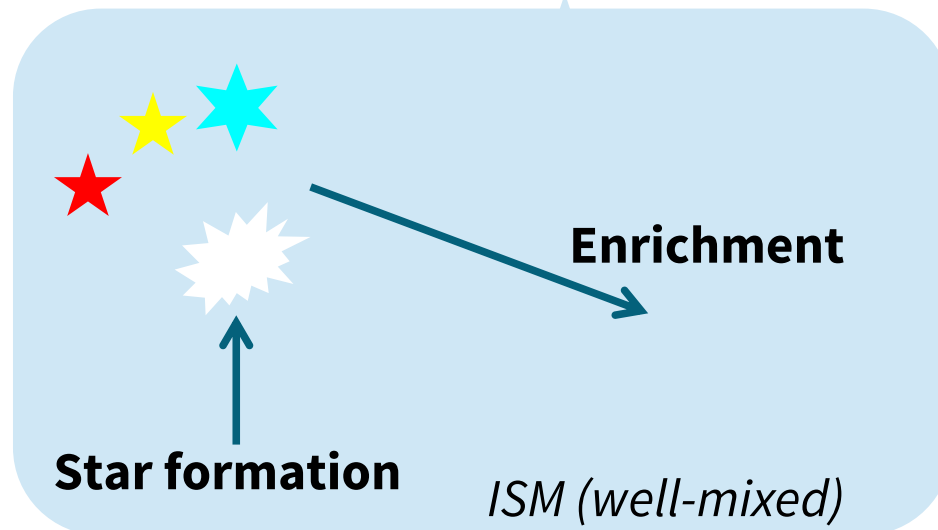
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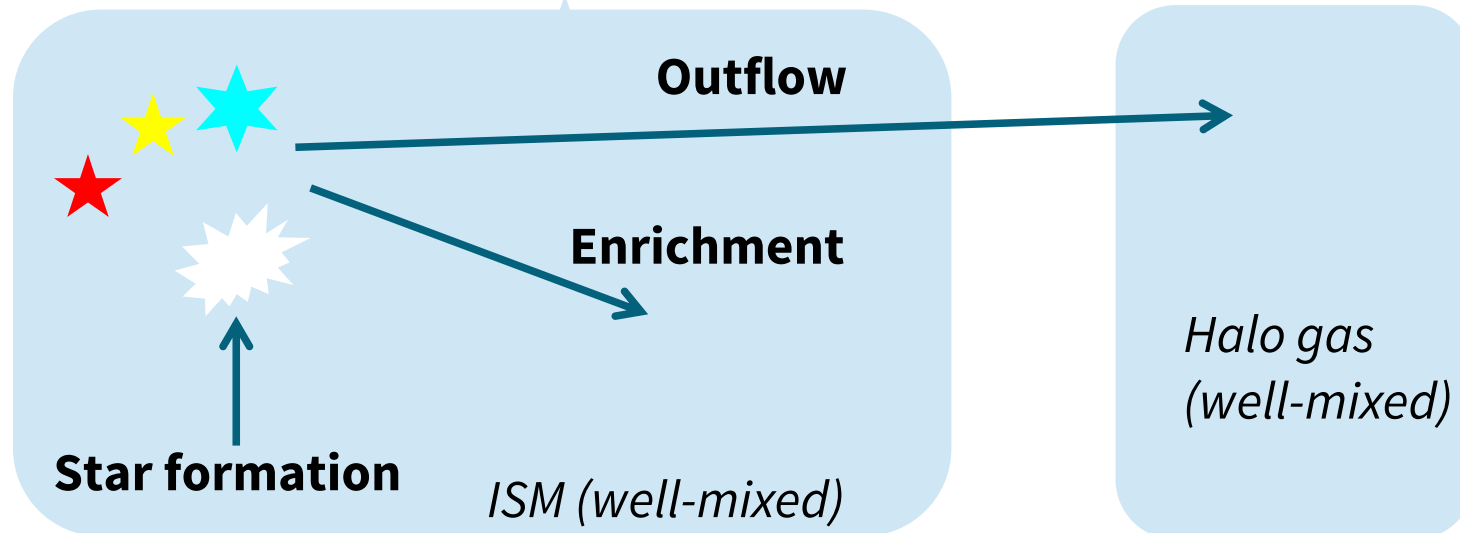
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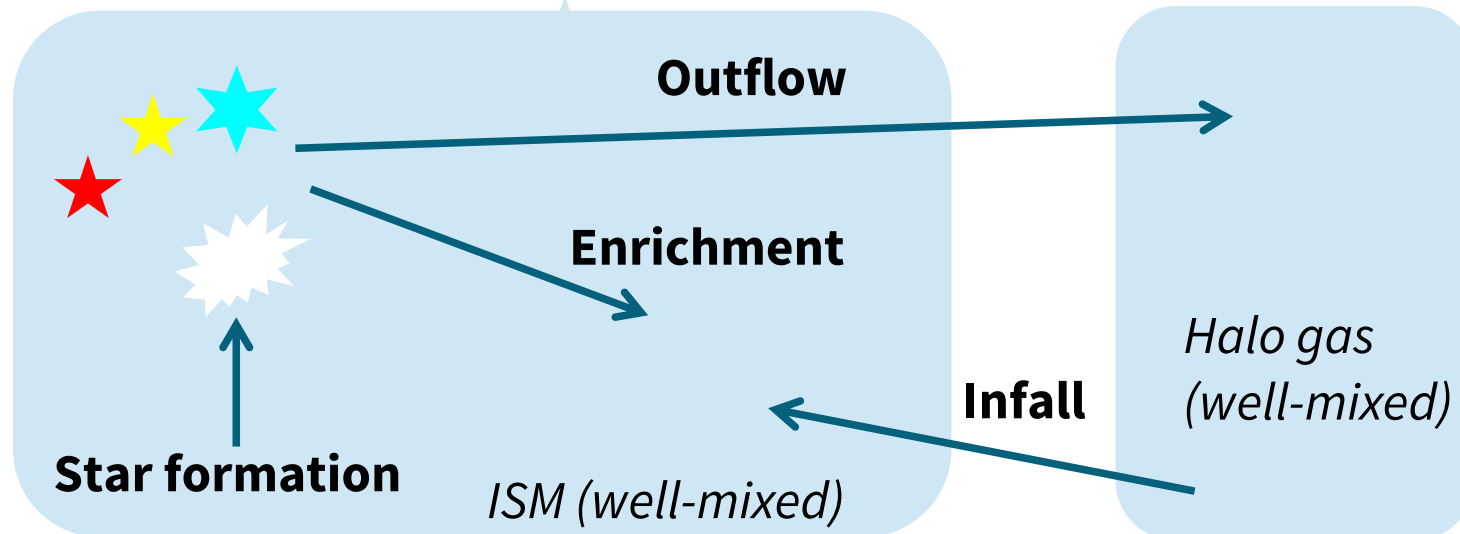
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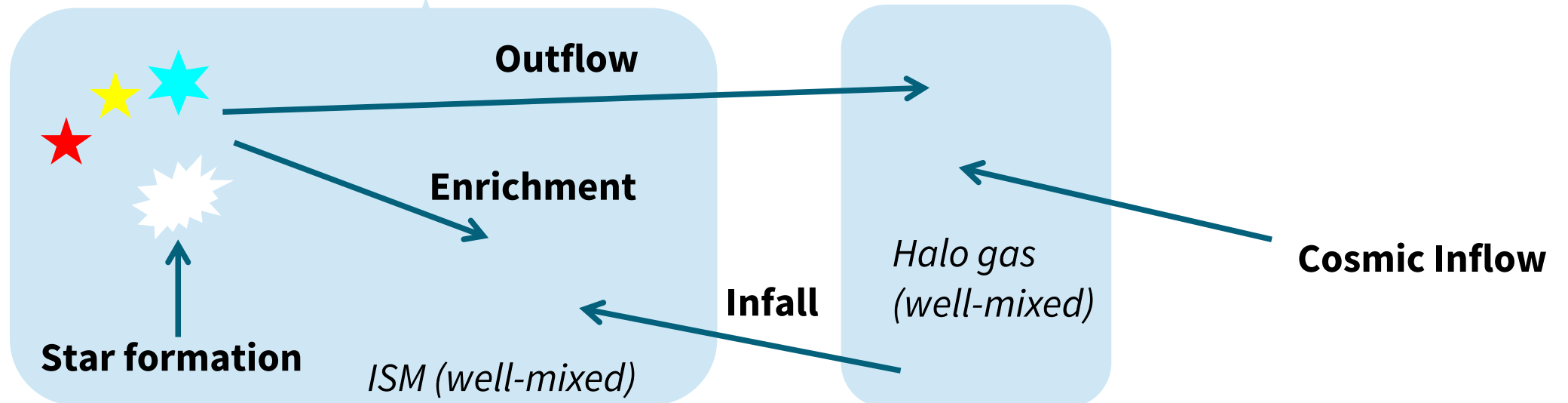
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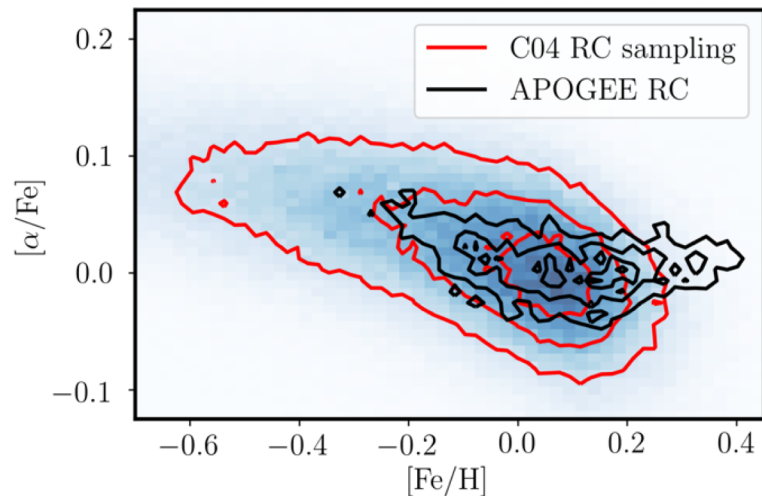
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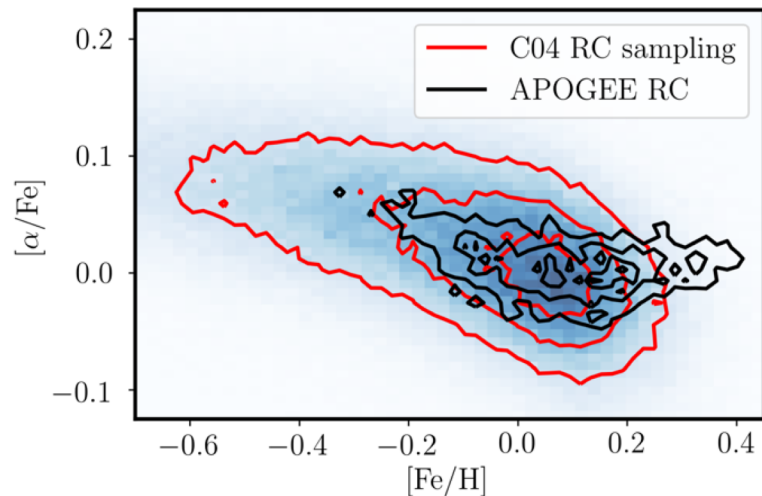
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*This needs **no fiducial model**,  
Input your data → Obtain **GCE parameters***

Rybizki, Just & Rix (2017)

# Parameter Inference with *Chempy*

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- ❑ *Chempy* can be inserted in a **Bayesian** framework to **infer** Galactic parameters.

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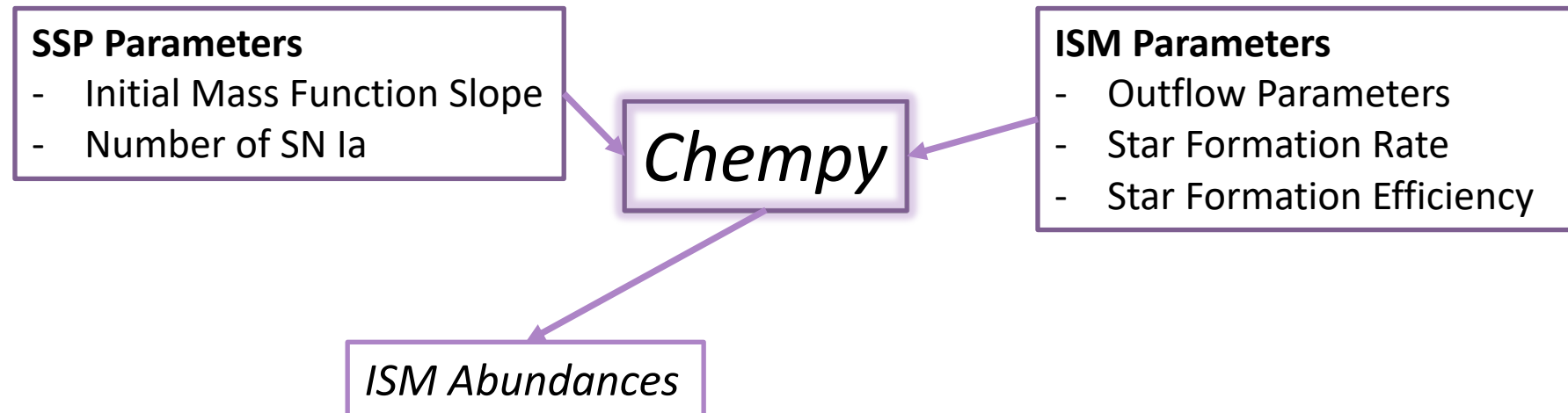
## ISM Parameters

- Outflow Parameters
- Star Formation Rate
- Star Formation Efficiency

Rybizki, Just & Rix (2017)

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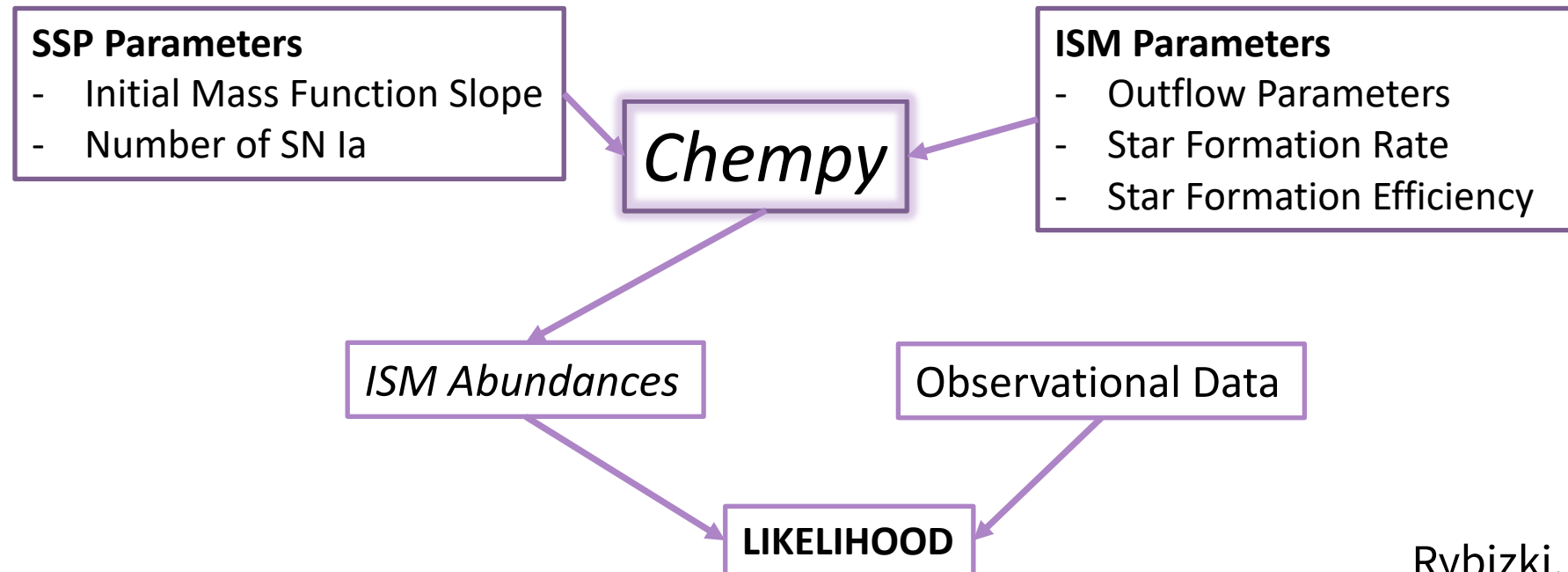
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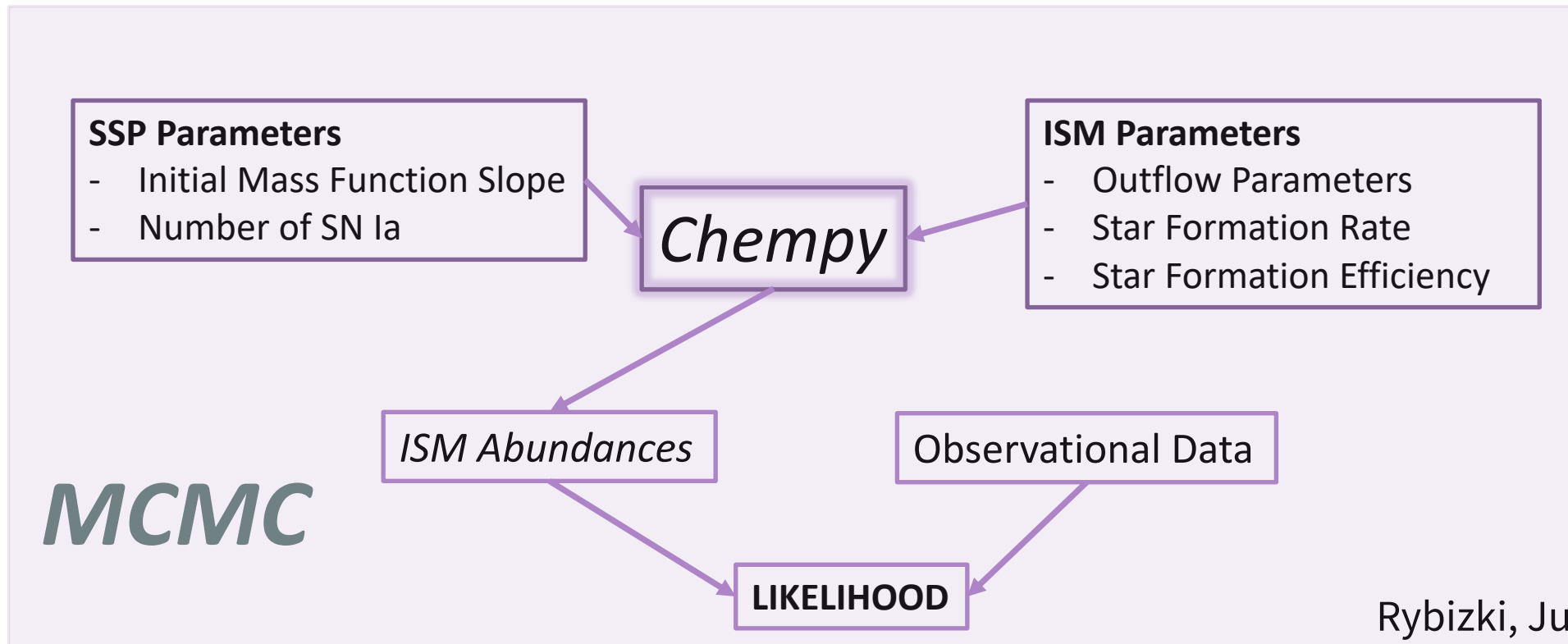
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Can *Chempy* be used to determine GCE parameters for hydrodynamical simulations?

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- **Goal:** Predict the best SSP parameters for hydrodynamical simulations to make sure they are consistent with observations

Philcox, Rybizki & Gutcke (2018)

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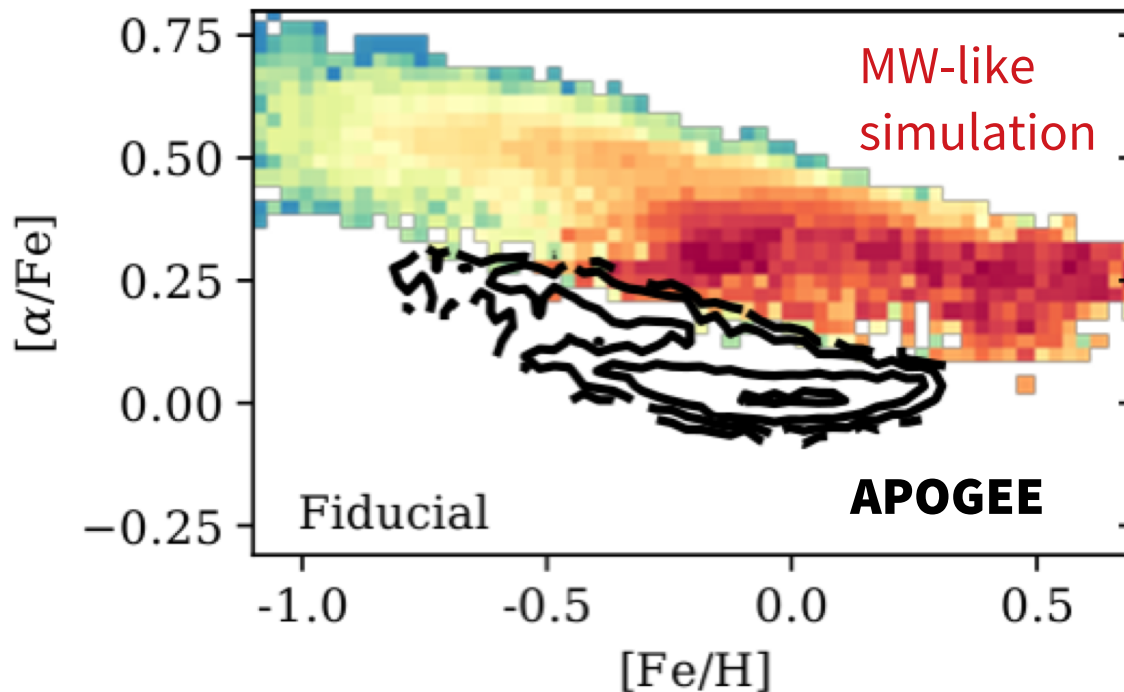
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  - ❑ Run simulation with **optimized** parameters and compare results!

Philcox, Rybizki & Gutcke (2018)



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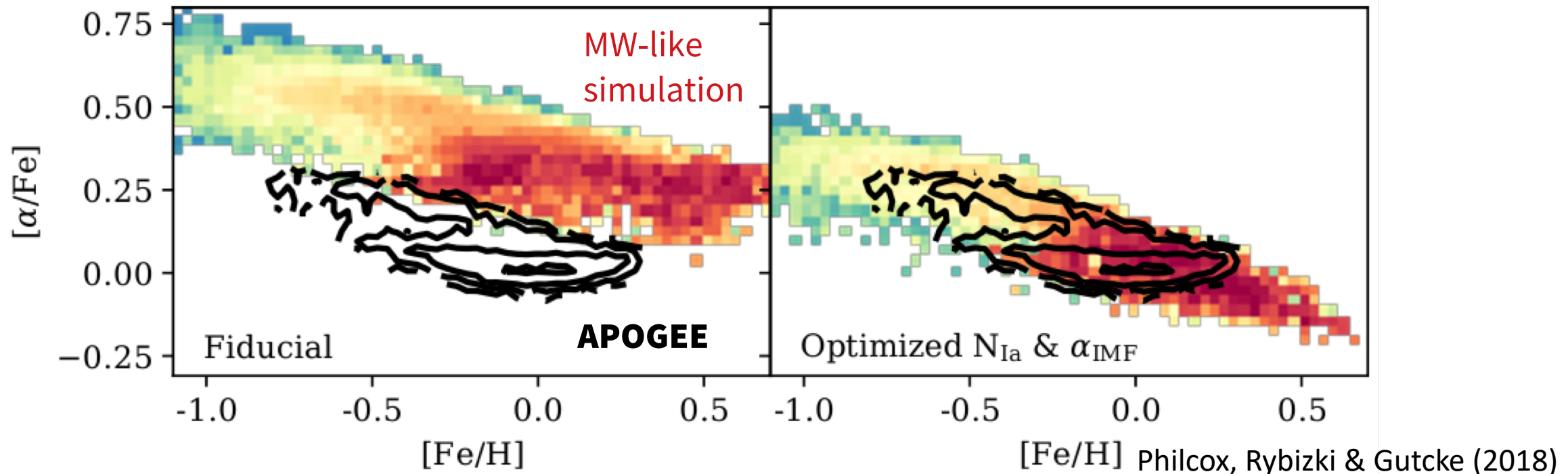
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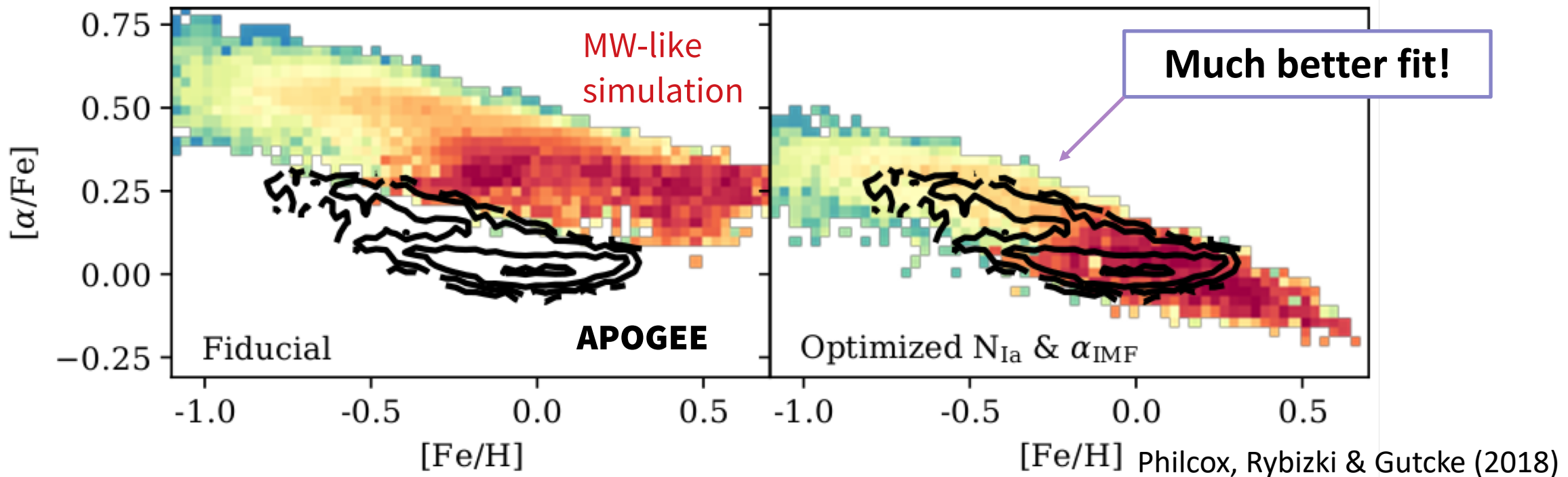
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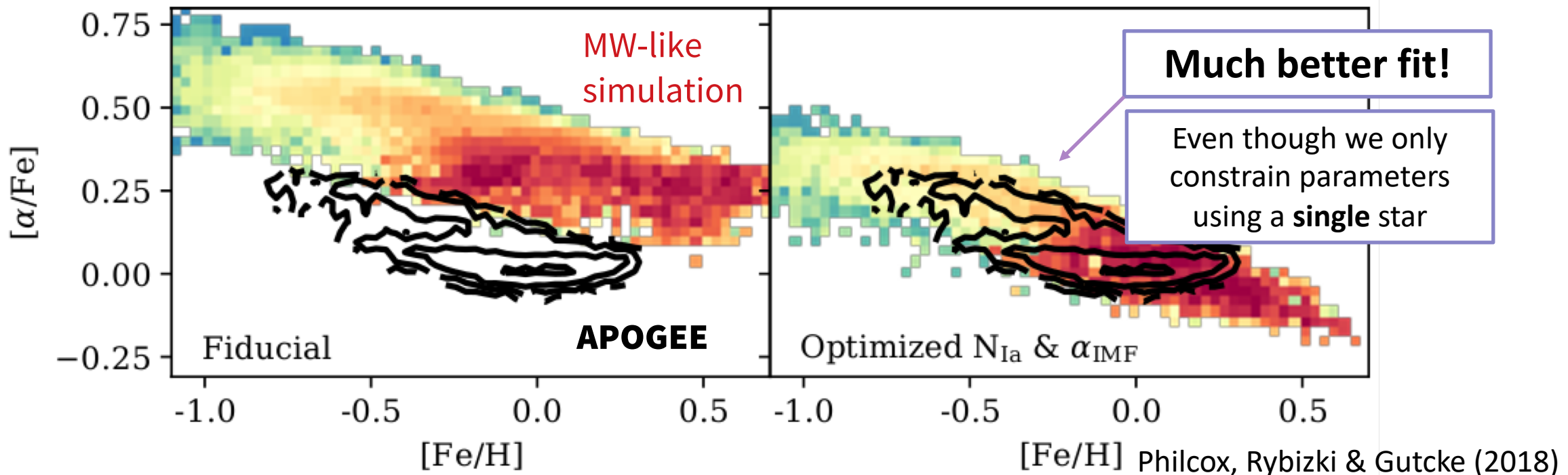
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# How well do our Yield Tables match Observational Data?

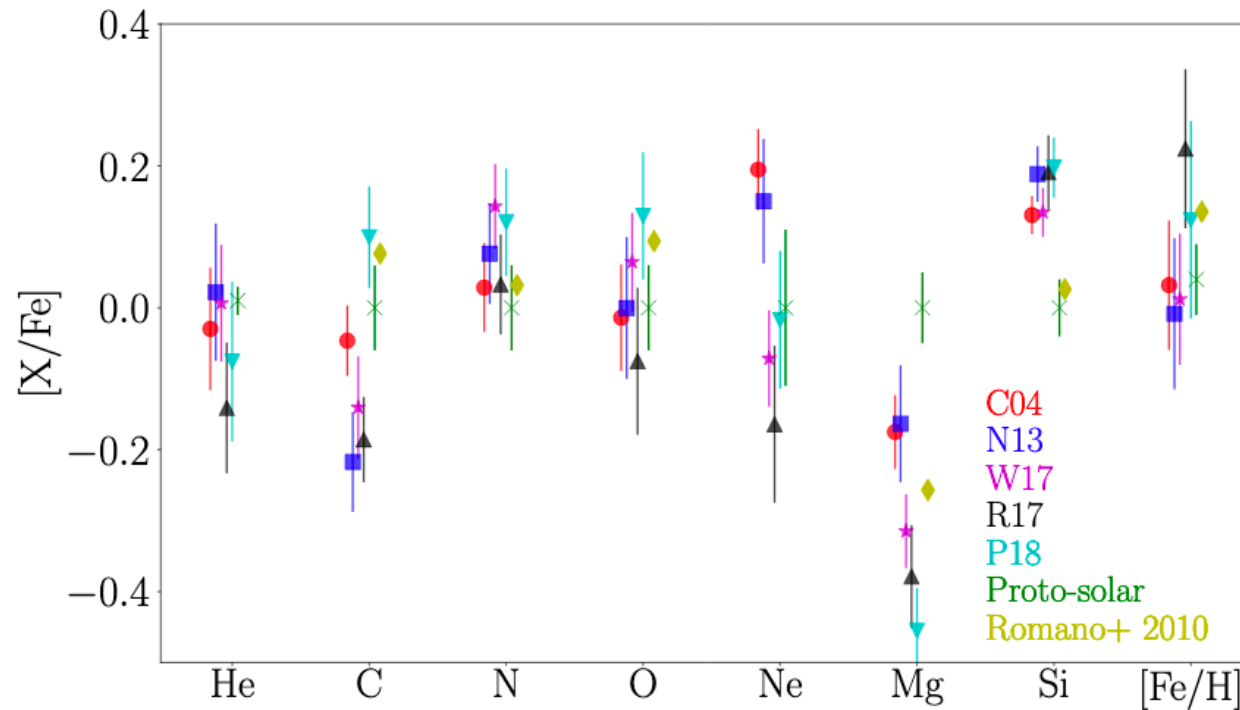
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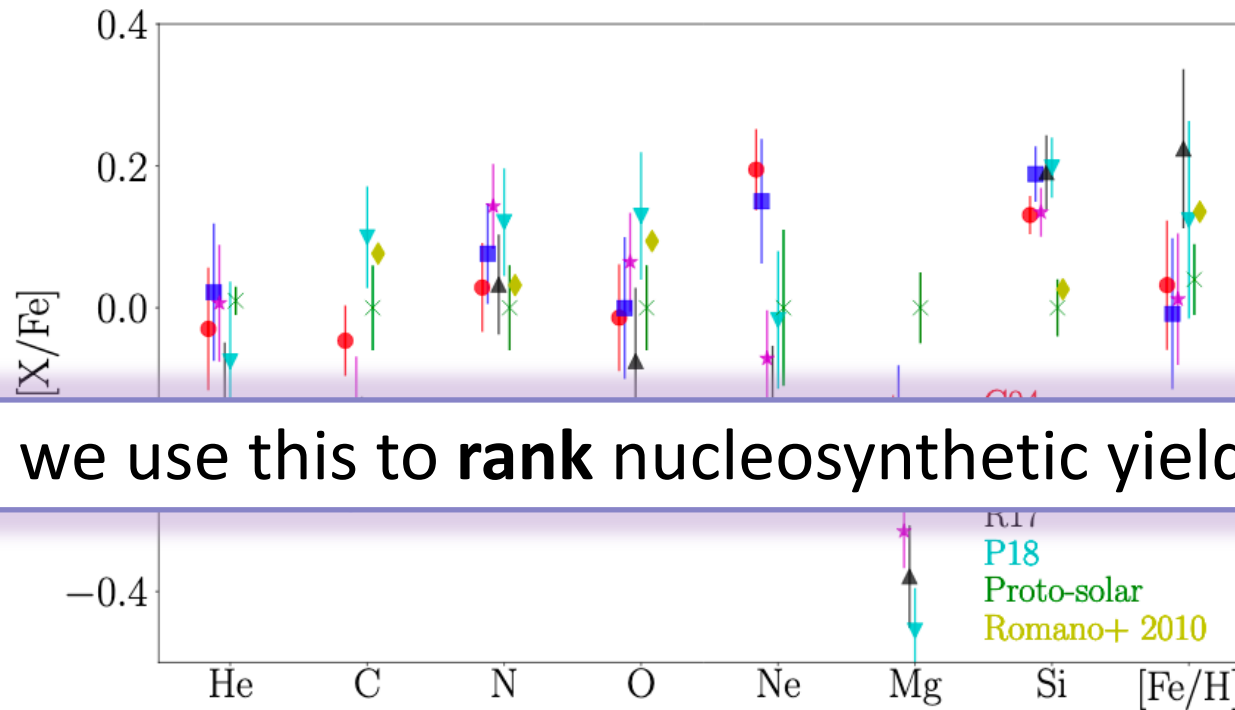
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Can we use this to **rank** nucleosynthetic yield tables?

Philcox, Rybizki & Gutcke (2018)



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  - ❑ Use  $n - 1$  elements to predict  $n$ -th element

Philcox, Rybizki & Gutcke (2018)

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Comparing Core-Collapse Supernovae Yield Tables using 28 Elements

Yield Set	Bayes Score
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Nikos Prantzos' yields perform best here!

Philcox, Rybizki & Gutcke (2018)



# Inferring SSP Parameters from Large Stellar Datasets with *Chempy*

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Philcox & Rybizki (2019)

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Philcox & Rybizki (2019)

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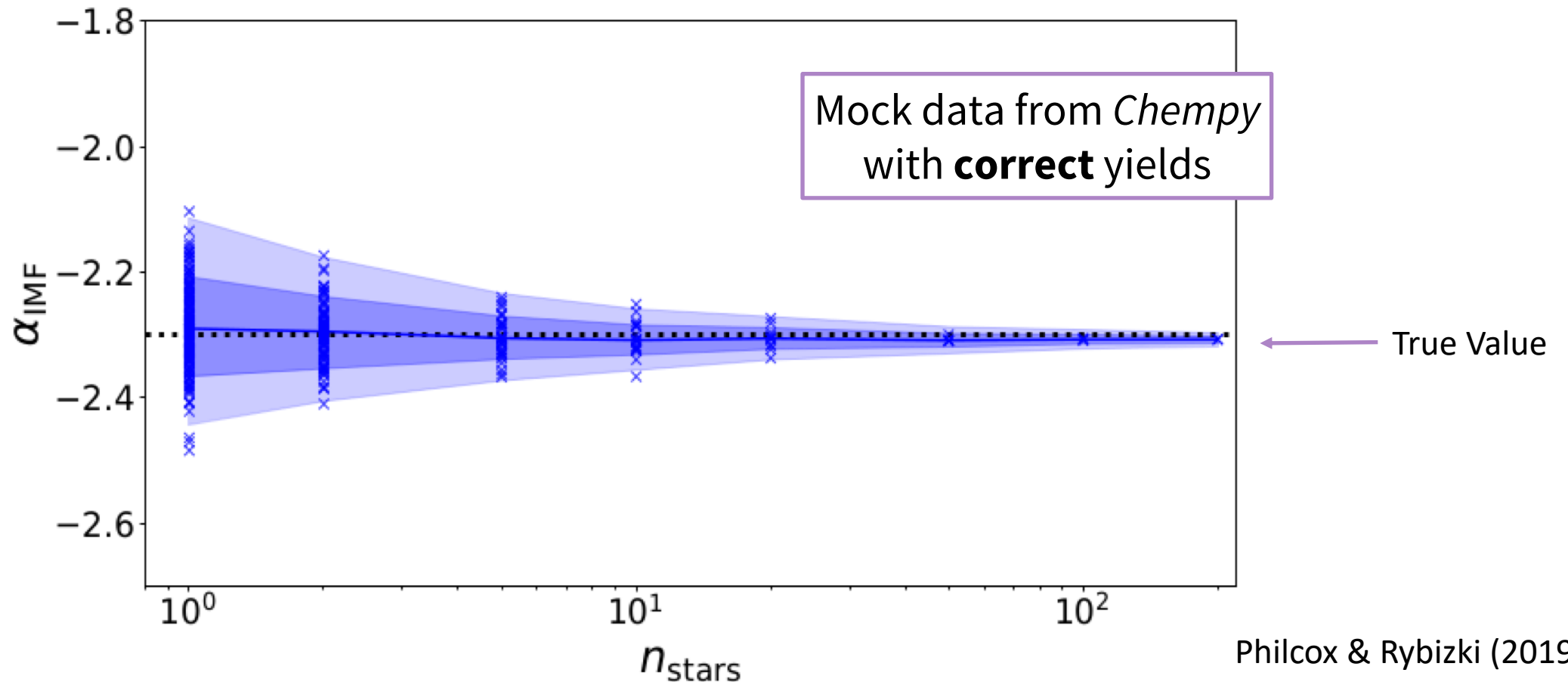
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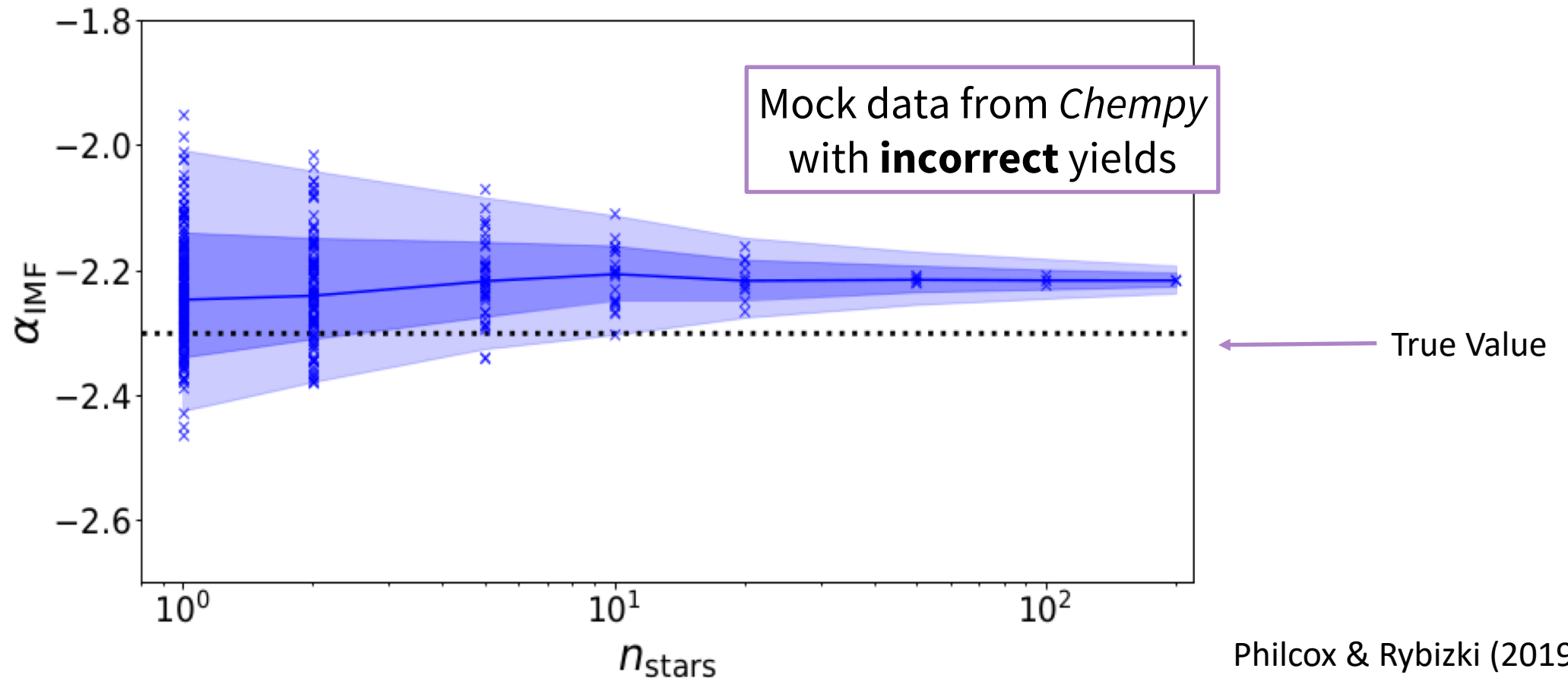
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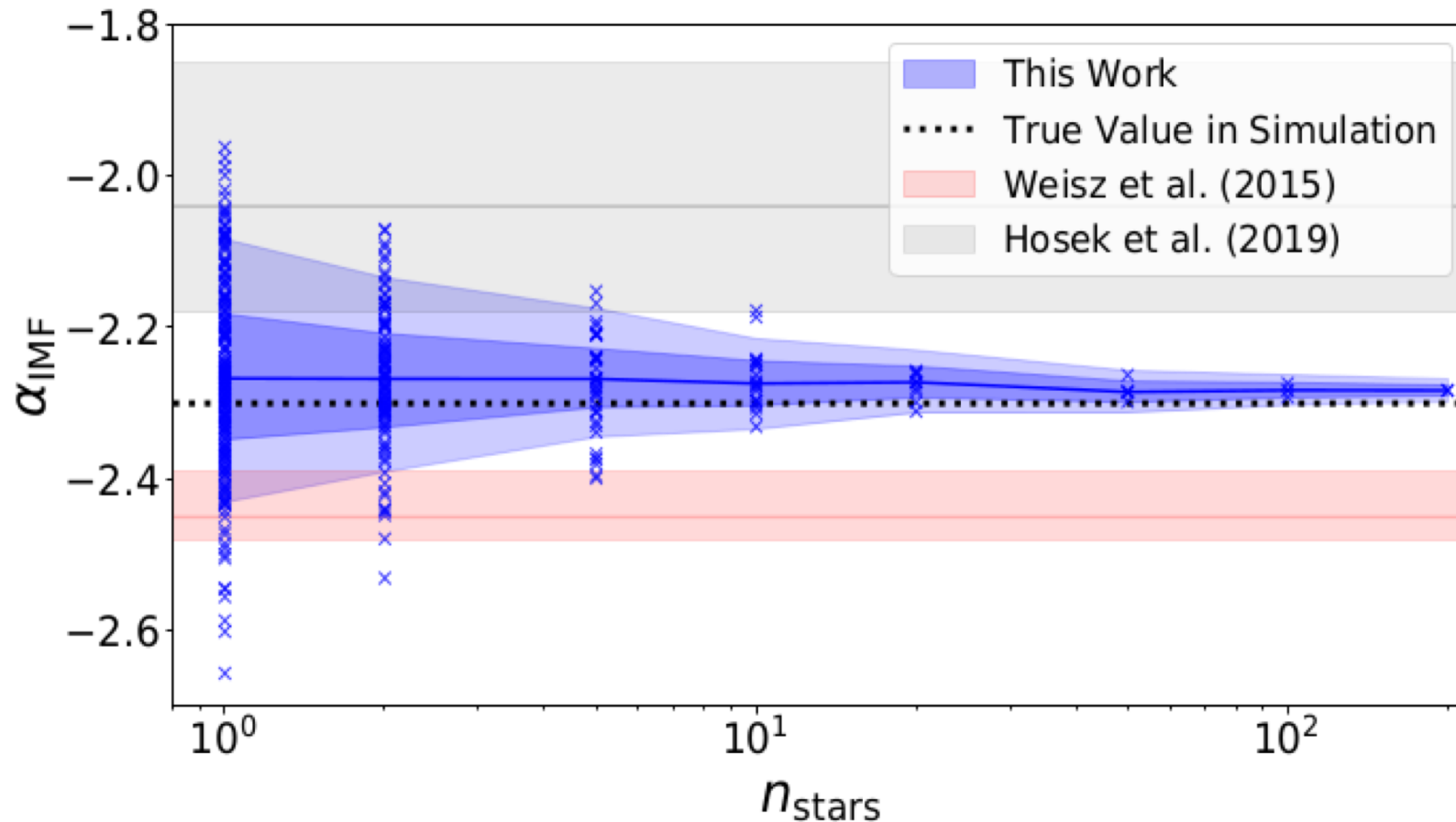
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Philcox & Rybizki (2019)

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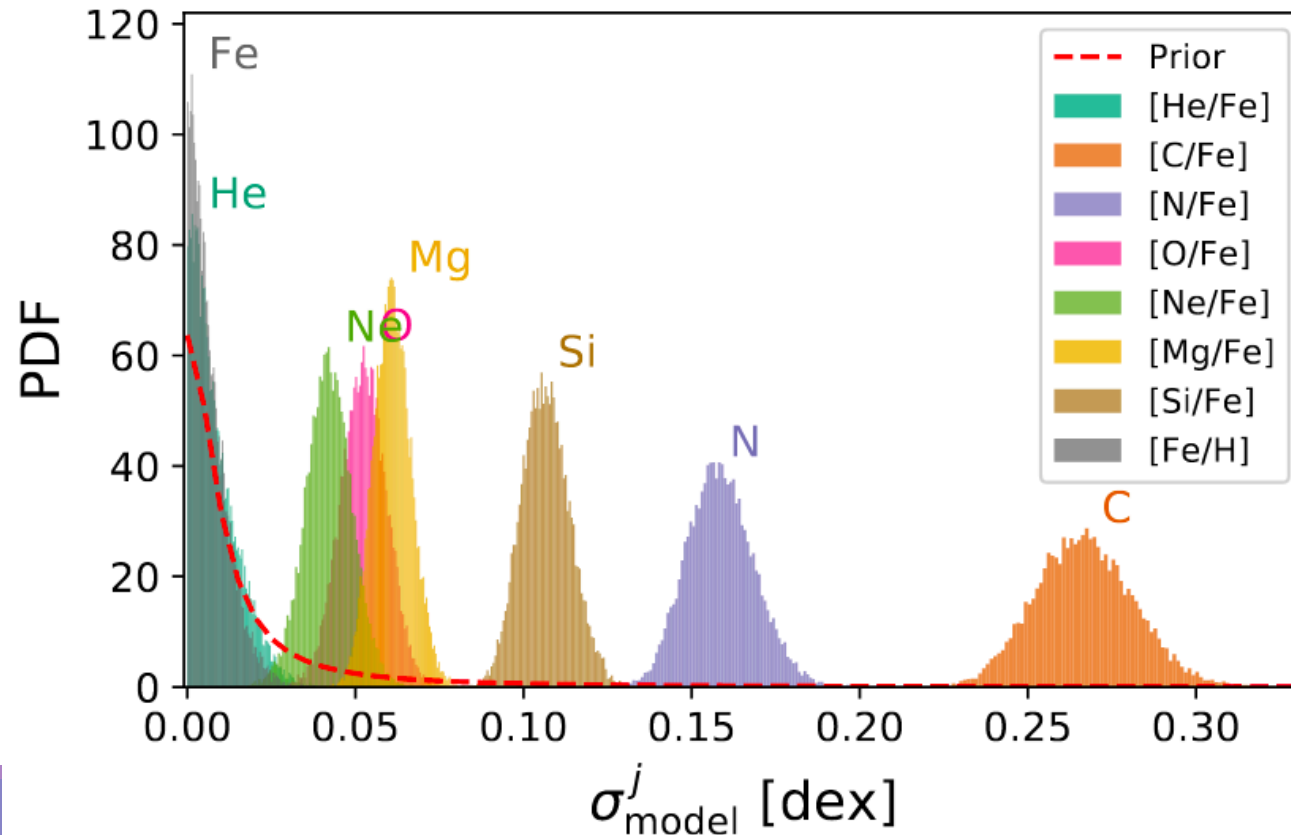
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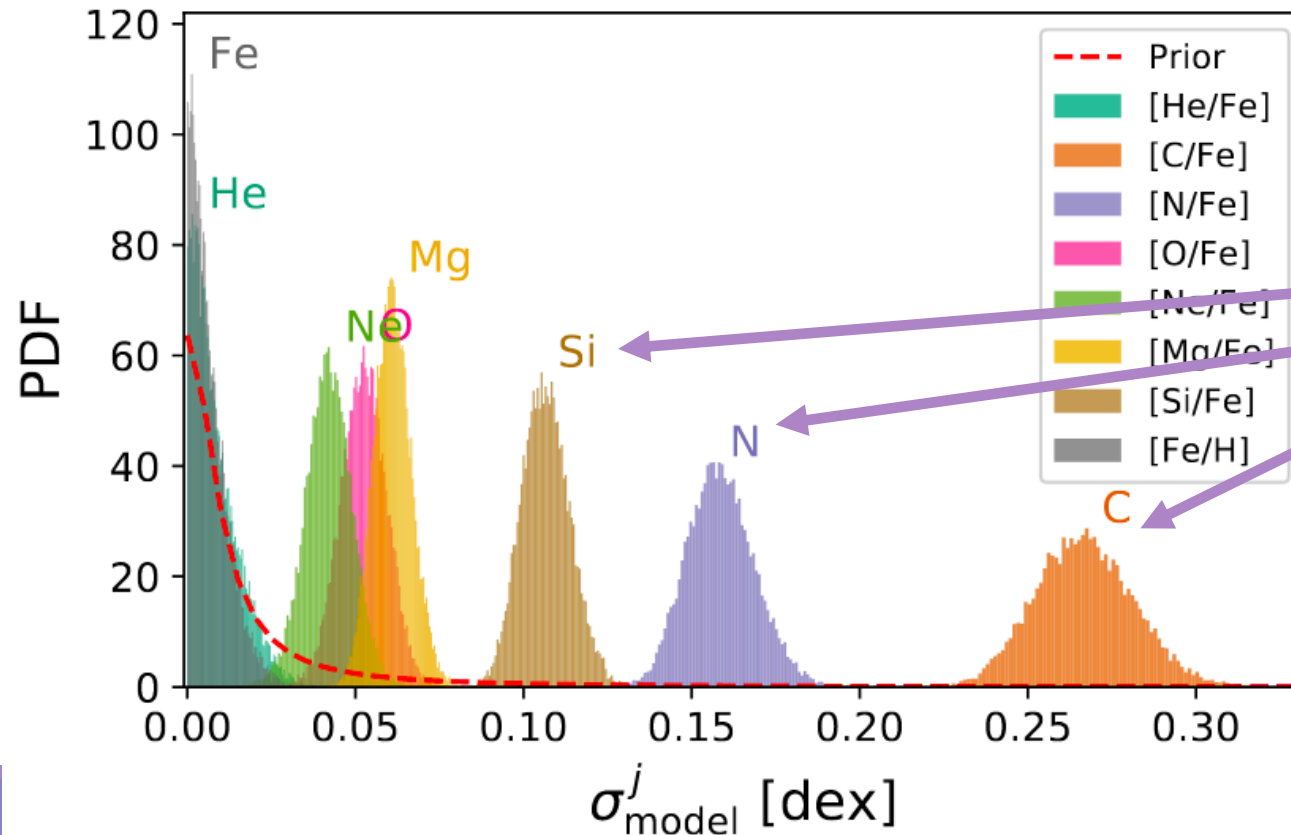


Philcox & Rybizki (2019)

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*Si, N and C are the most discrepant elements between our yield sets!*

Philcox & Rybizki (2019)

# What's Next For *Chempy*?

# Extensions to the *Chempy* model

---

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  - ❑ Additional nucleosynthetic processes (e.g. Neutron star mergers, Hypernovae)
- ❑ Addition of **yield table uncertainties** into the GCE model
- ❑ What do you want to see GCE models incorporating?

# Future Projects

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- ❑ Run the multi-star inference on **real data** to compute Milky Way SSP parameters

# Future Projects

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- ❑ Parameter optimization of chemical evolution for hydrodynamical simulations including **SSP** parameters and **yield tables**.

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- ❑ Infer the **yield tables** empirically from observational data.

# Summary

- ❑ *Chempy* is a **fast** and **flexible** GCE model, allowing for Bayesian exploration of parameter space.
- ❑ Using *Chempy* we can optimize SSP parameters for **hydrodynamical simulations** to ensure they match observational data.
- ❑ By extending to **multiple stars** we can precisely constrain global Galactic parameters
- ❑ And maybe even yield tables...

Thank you  
for your  
attention!



# Additional Slides

# Neural Networks

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# Neural Networks

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- ❑ Use neural networks to **predict** output chemical elements from input parameters.

# Neural Networks

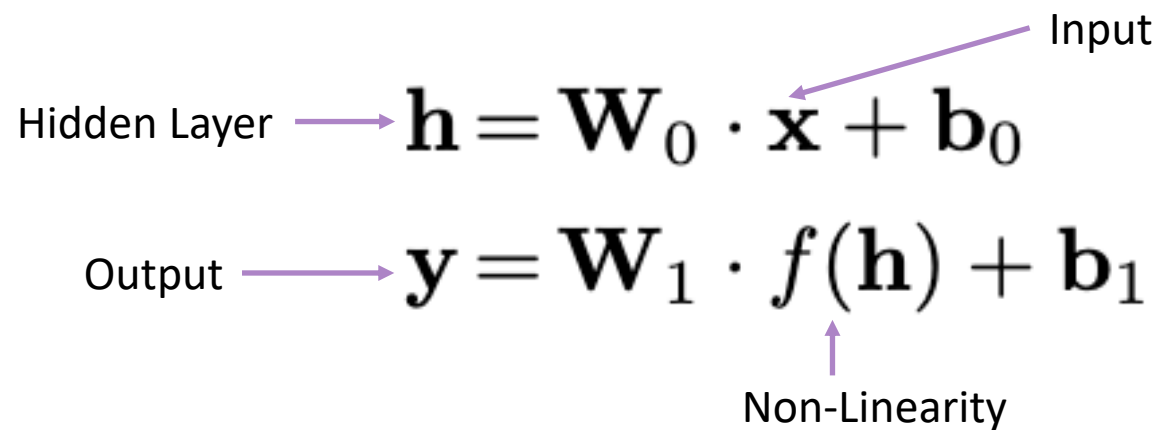
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- ❑ This acts as a **fast, non-linear** interpolator, which is **differentiable**.

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Hidden Layer  $\longrightarrow \mathbf{h} = \mathbf{W}_0 \cdot \mathbf{x} + \mathbf{b}_0$

Output  $\longrightarrow \mathbf{y} = \mathbf{W}_1 \cdot f(\mathbf{h}) + \mathbf{b}_1$

Input

Non-Linearity

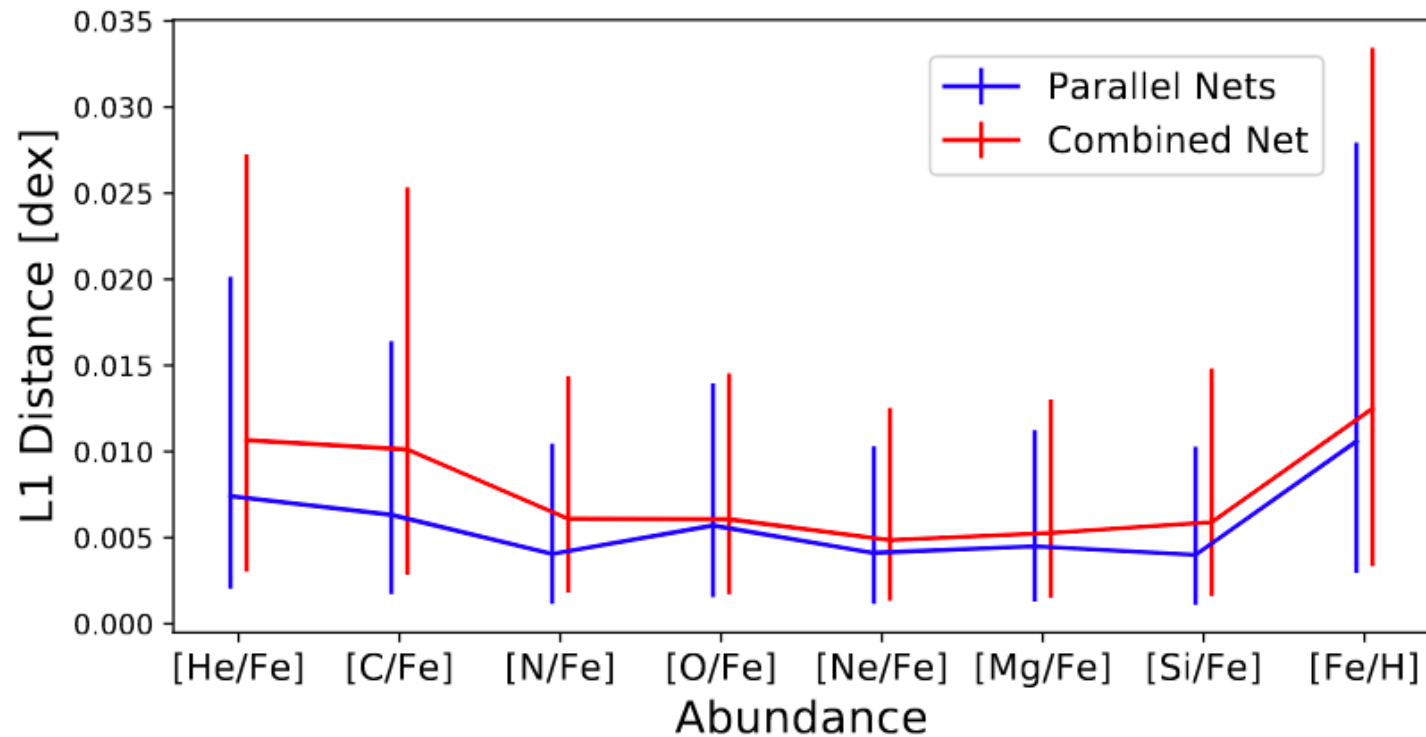
# Neural Networks

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- This is trained by running *Chempy* on  $\sim 10^4$  points in parameter space.

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**Errors are much below observational error**

Philcox & Rybizki (2019)

# Hamiltonian Monte Carlo (HMC)

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- ❑ Markov Chain Monte Carlo (MCMC) is **slow** and **unsuitable** for high-dimensional problems.
- ❑ MCMC works by jumping between points in parameter space at random.
- ❑ HMC preferentially samples where the posterior is **large**.
- ❑ It's **much more efficient** but requires a **differentiable** model.

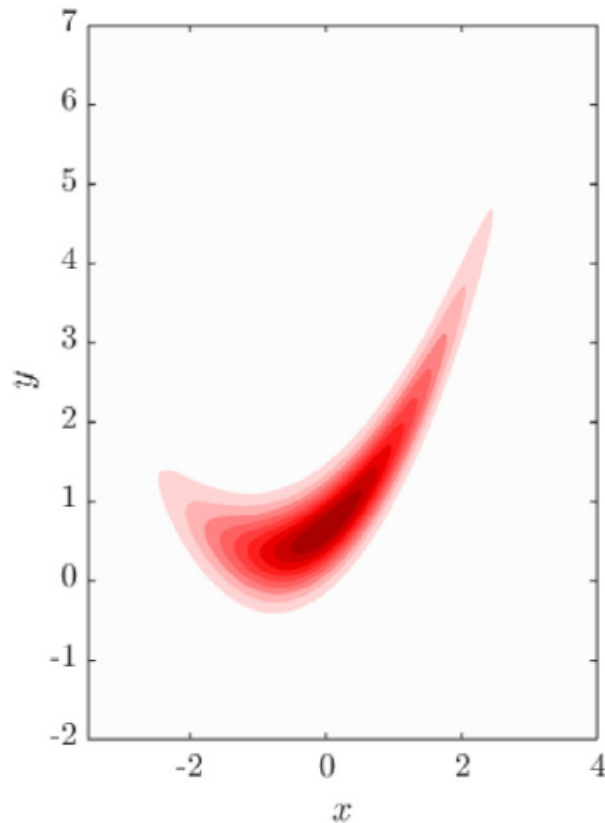
Betancourt (2017)



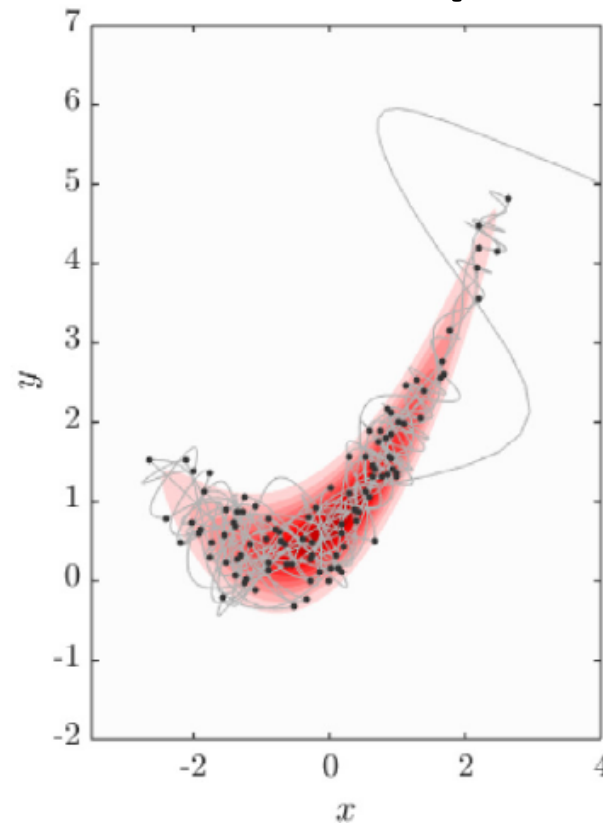
# Hamiltonian Monte Carlo (HMC)

□ HMC preferentially samples where the posterior is **large**.

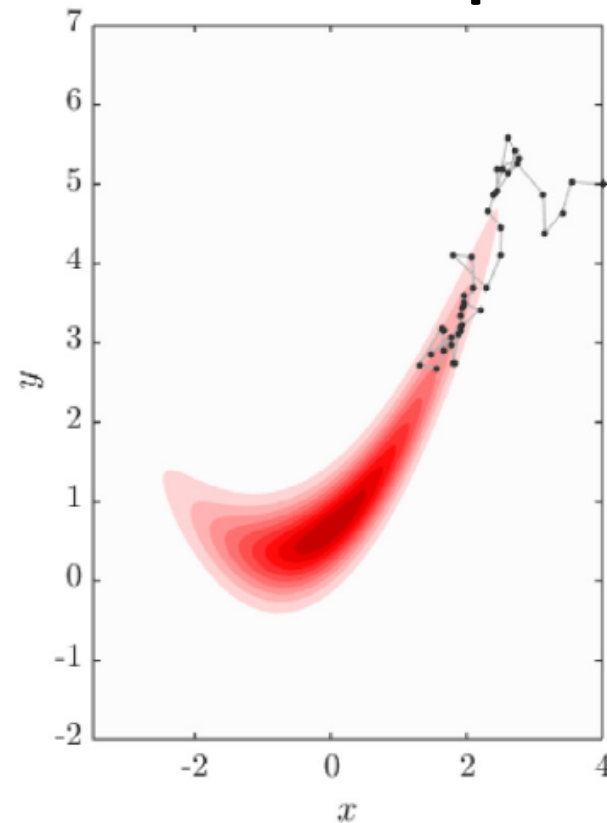
**Posterior**



**HMC Samples**

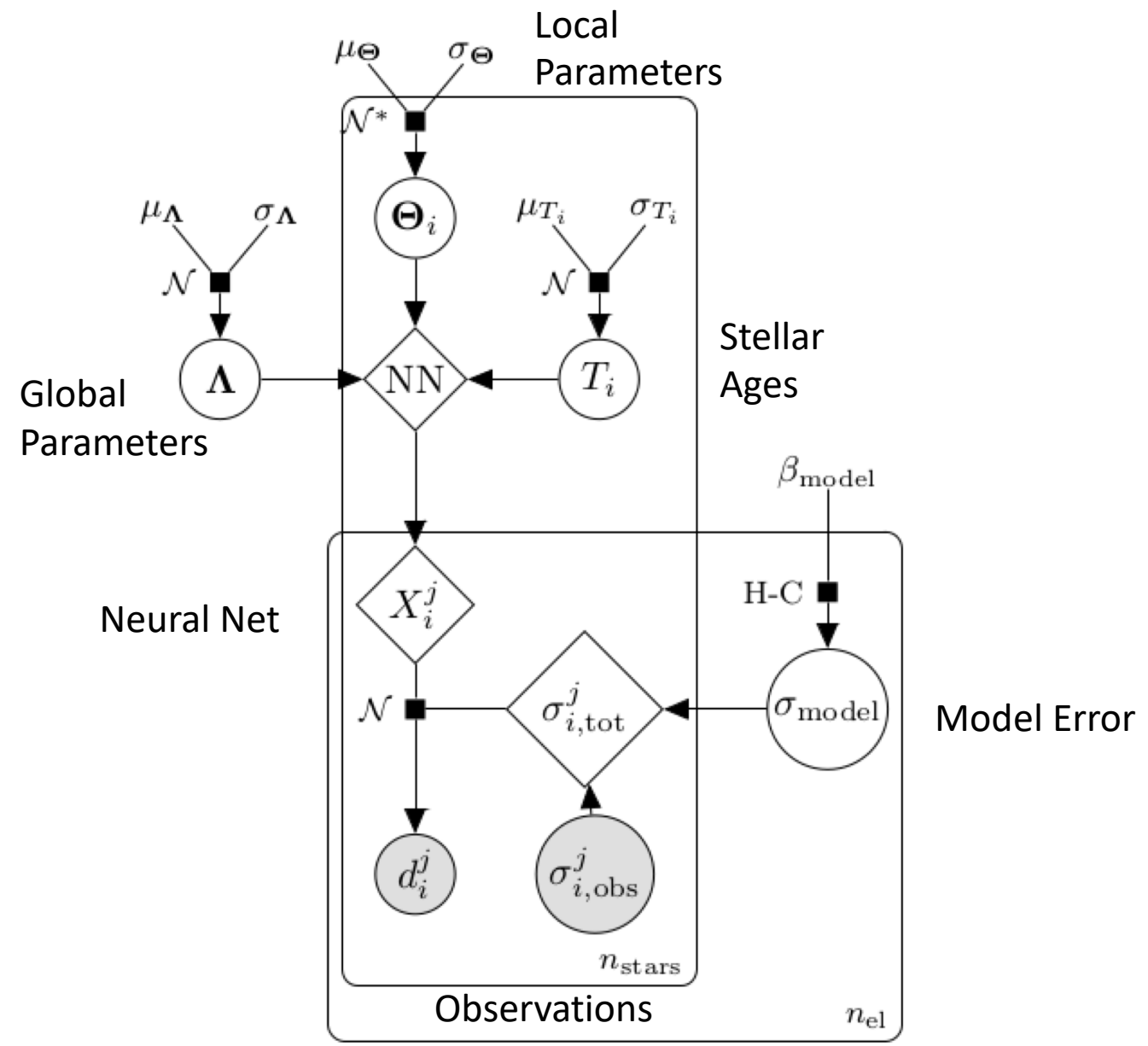


**MCMC Samples**

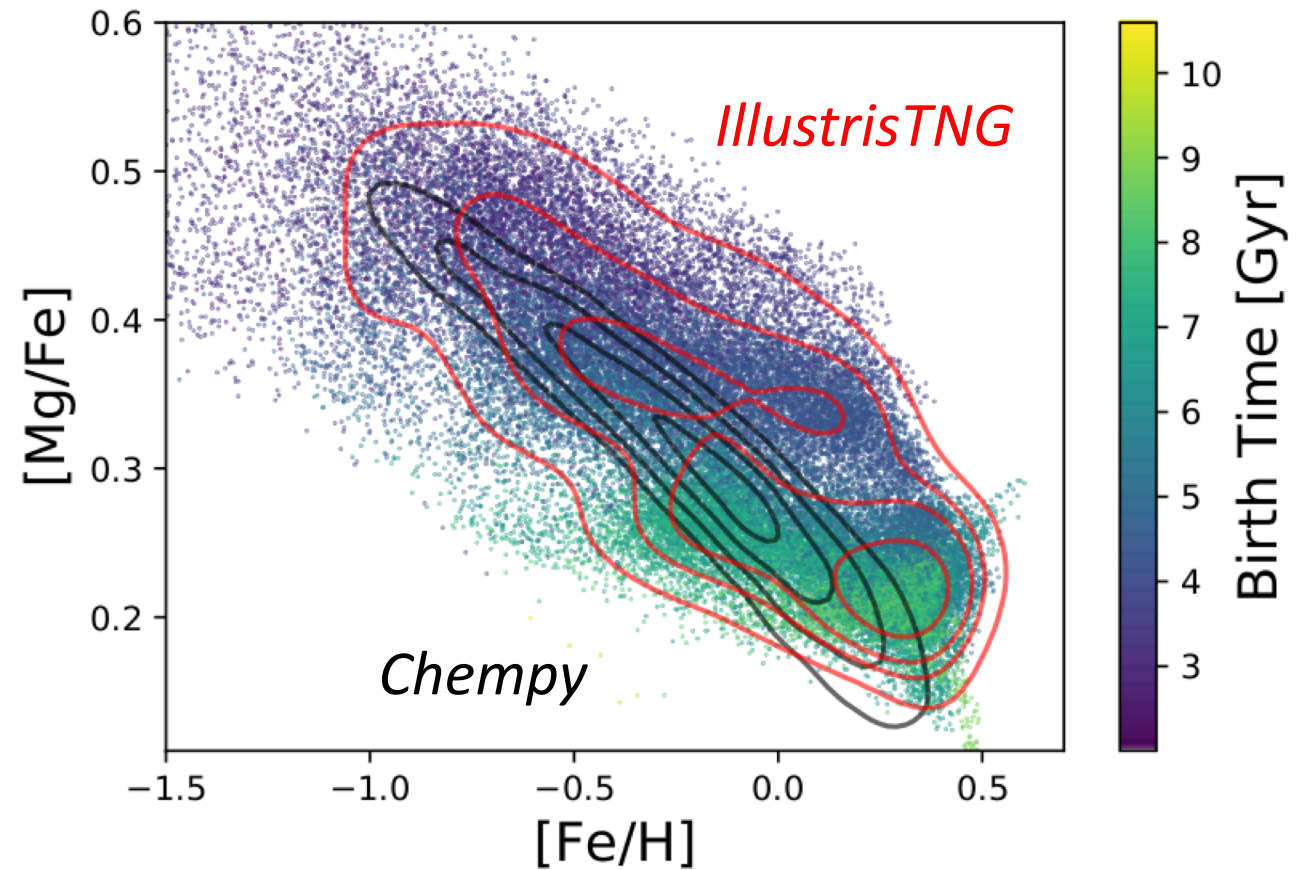


Wang+ (2019)

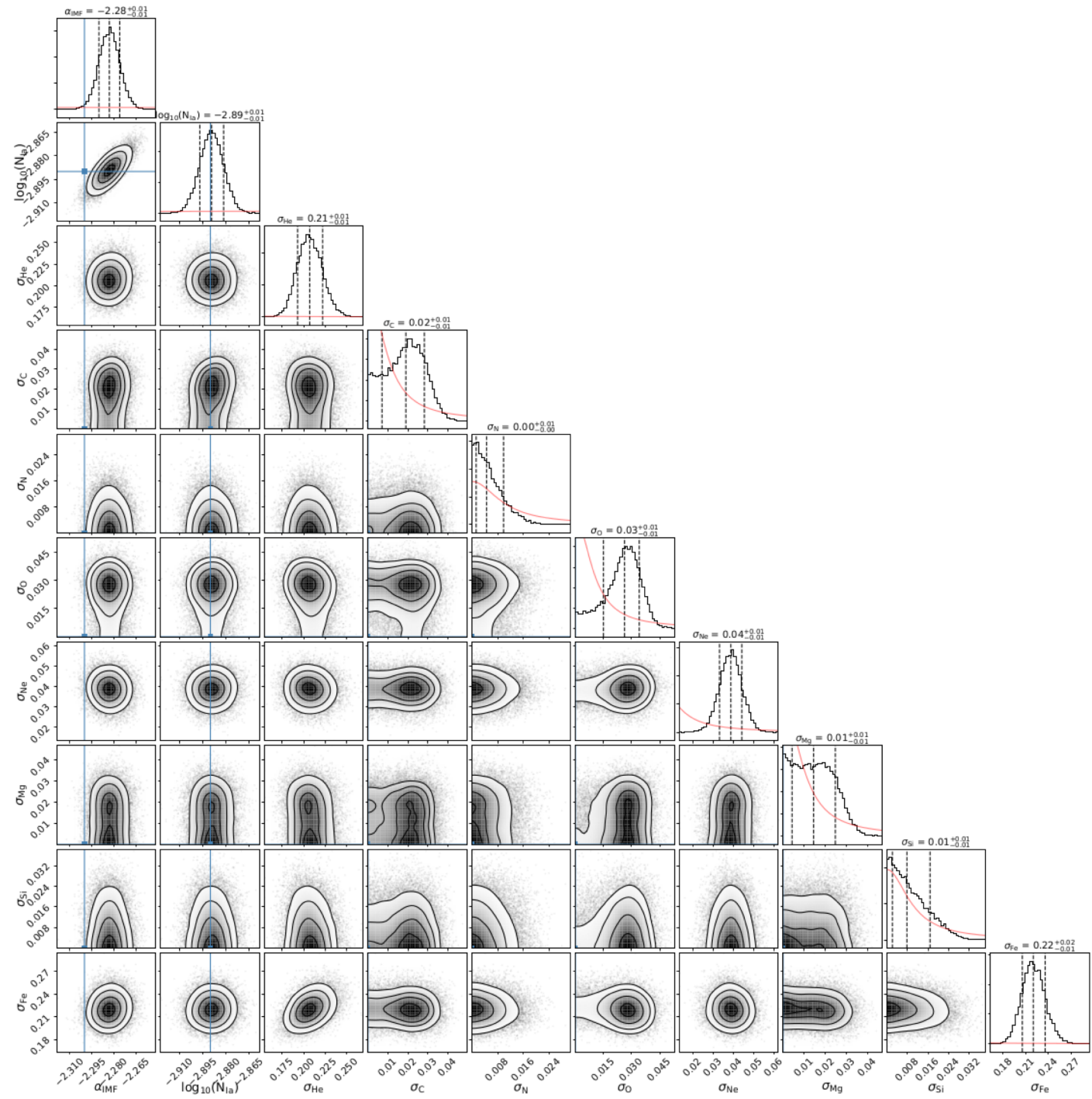
# ChempyMulti Architecture



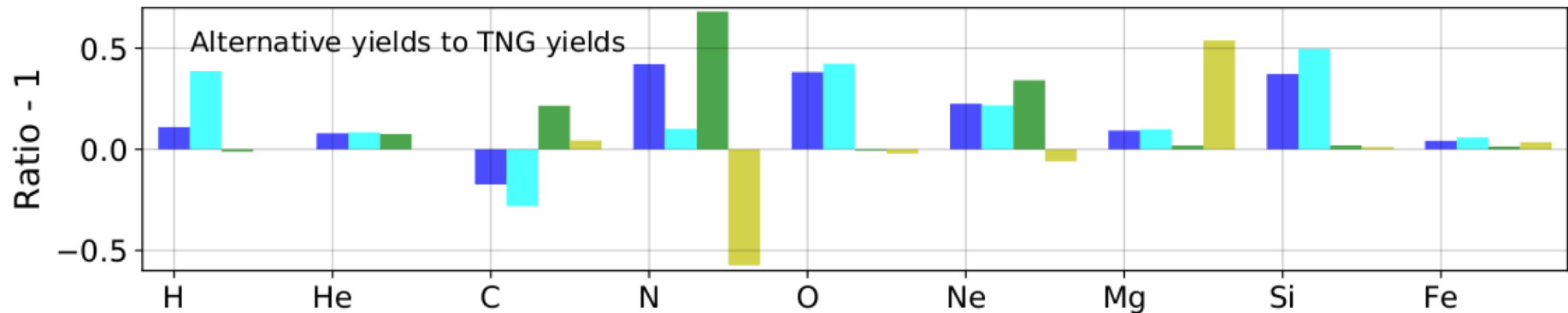
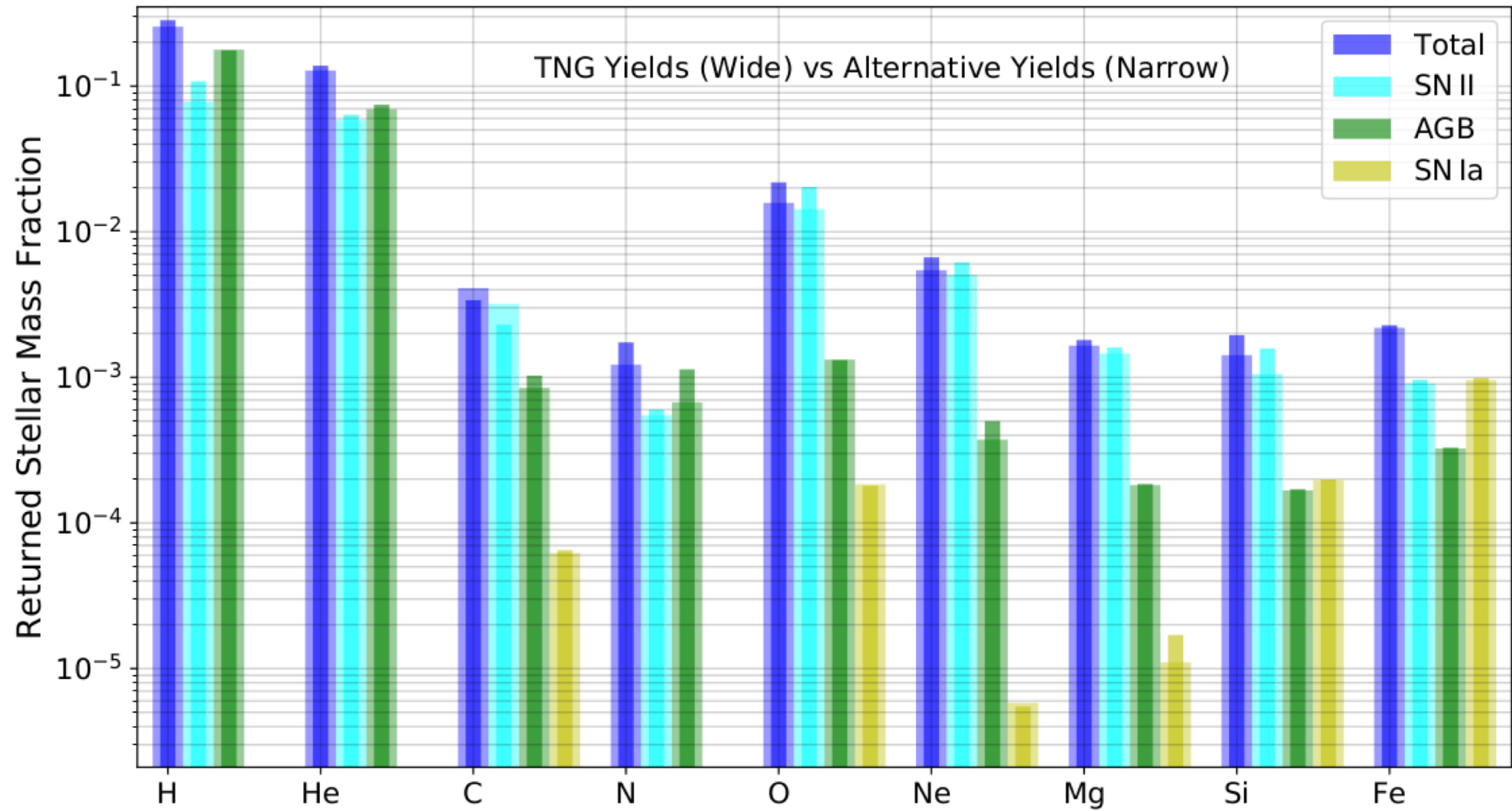
# Abundance Diagrams



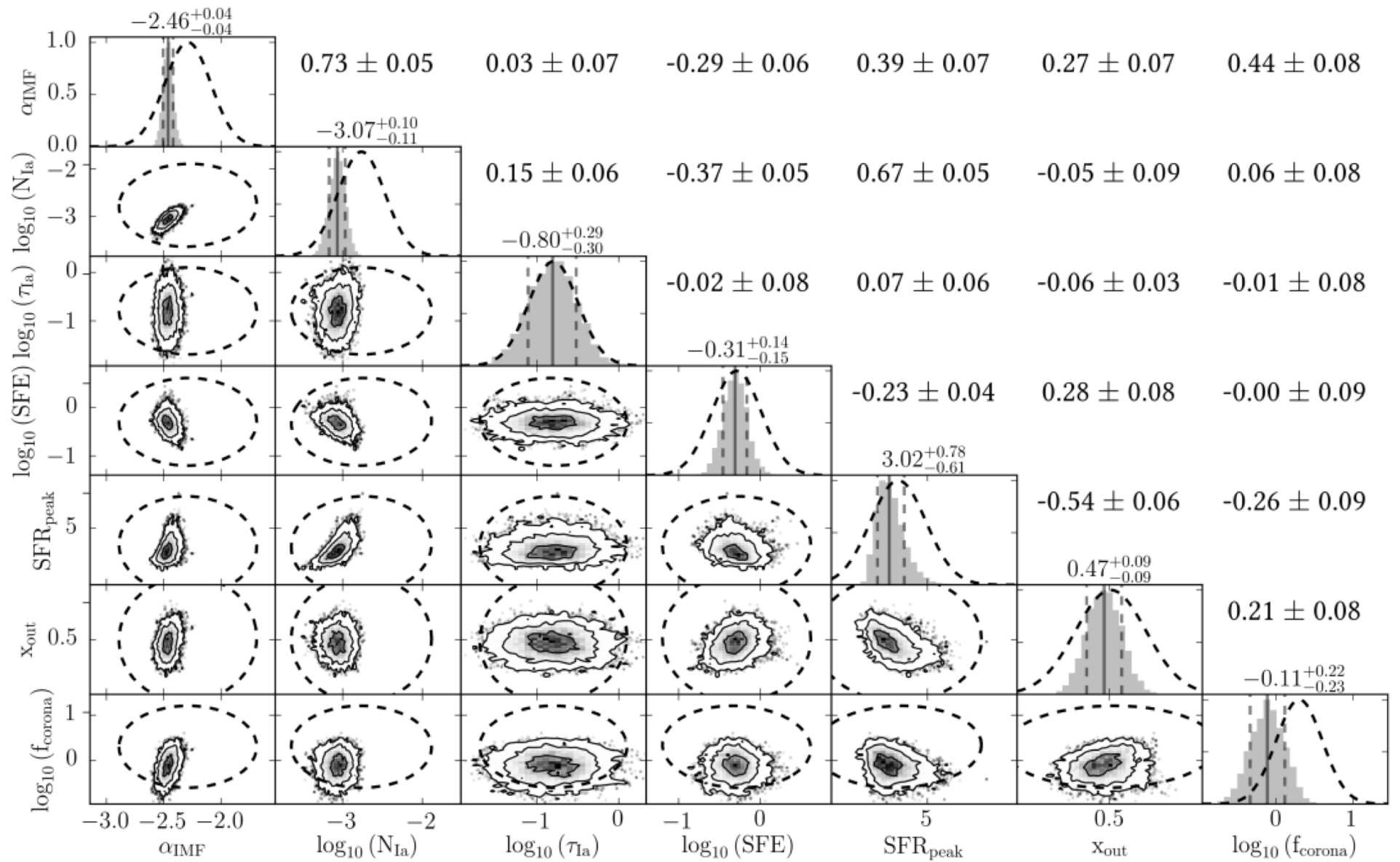
# Full Corner Plot



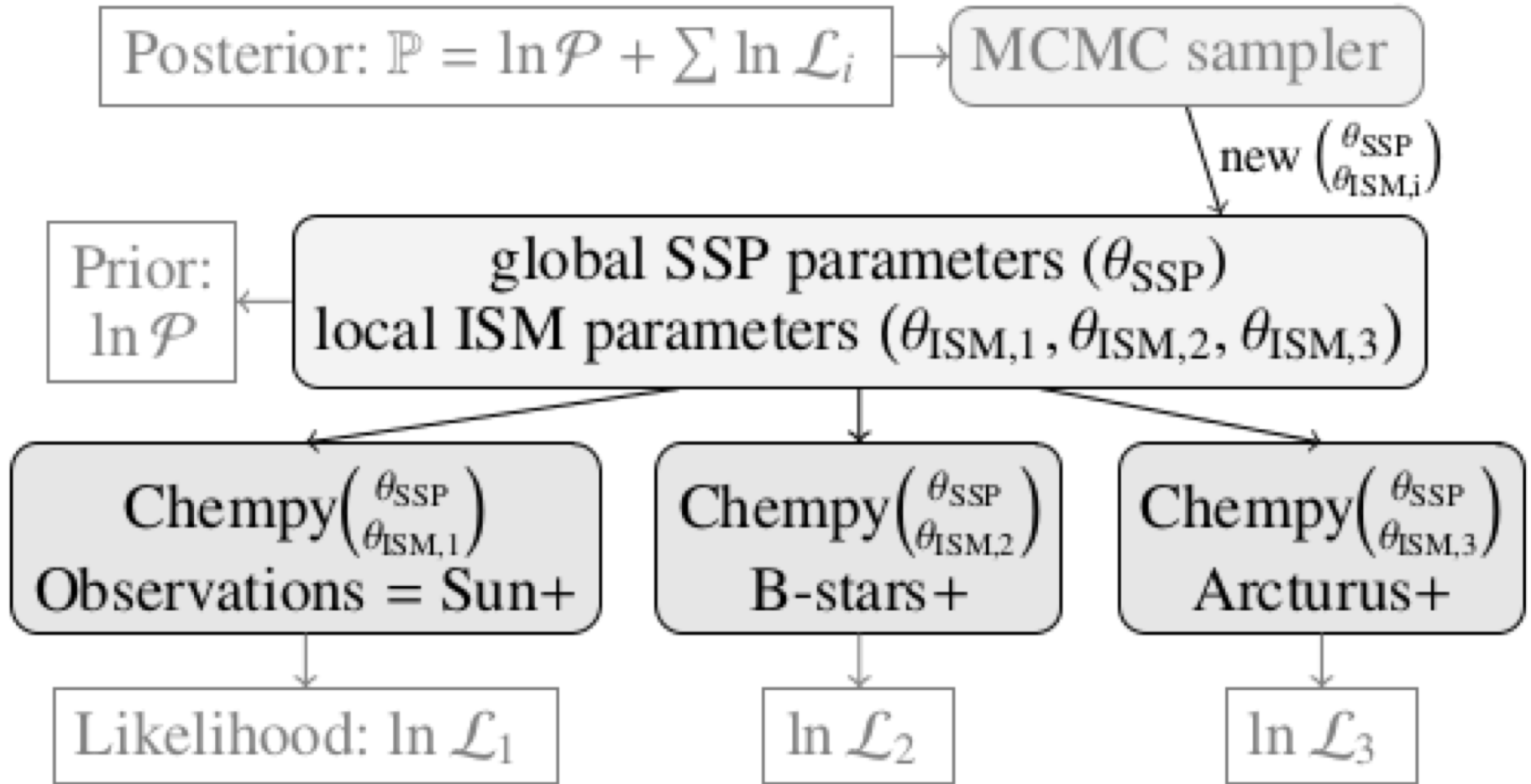
# Default and Alternative Yields



# Single Star Corner Plots



**The  
*Chempy*  
Model**



# Full Hydrodynamical Simulation Optimization

