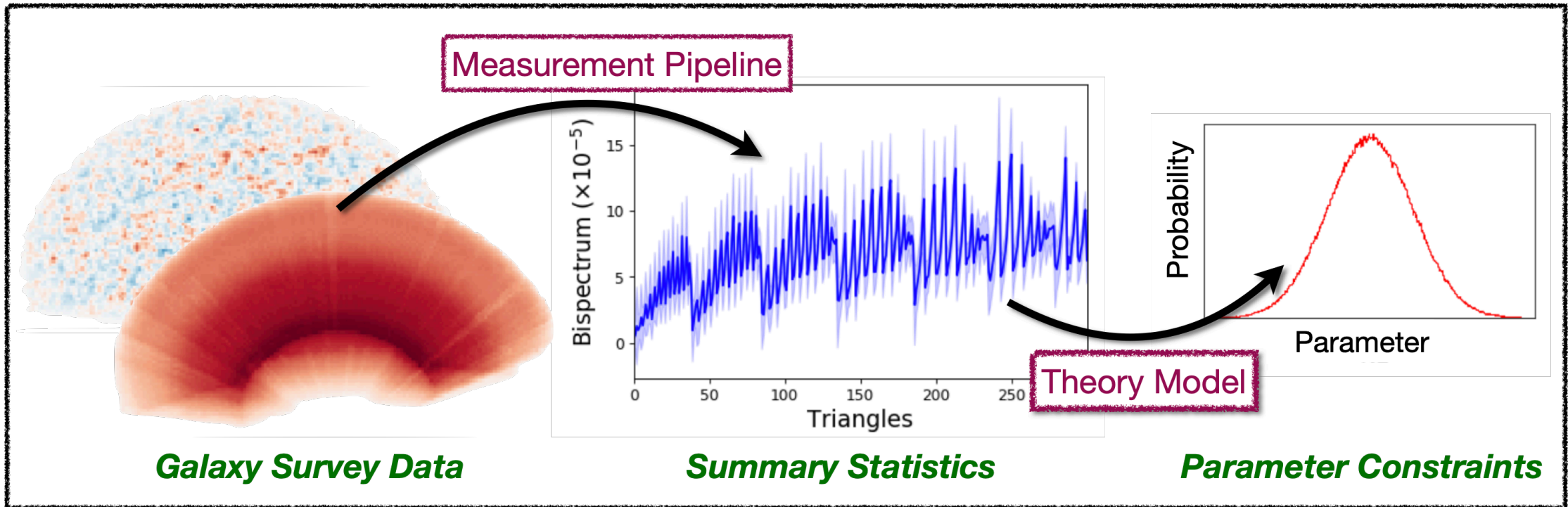


Cosmology With Galaxy Surveys

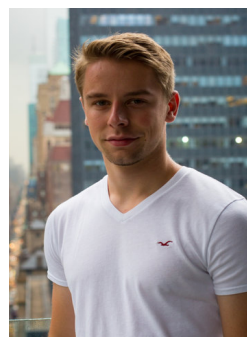
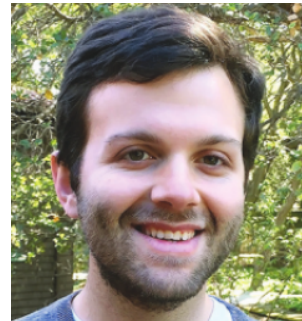
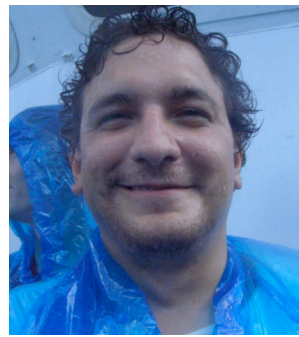


Oliver Philcox

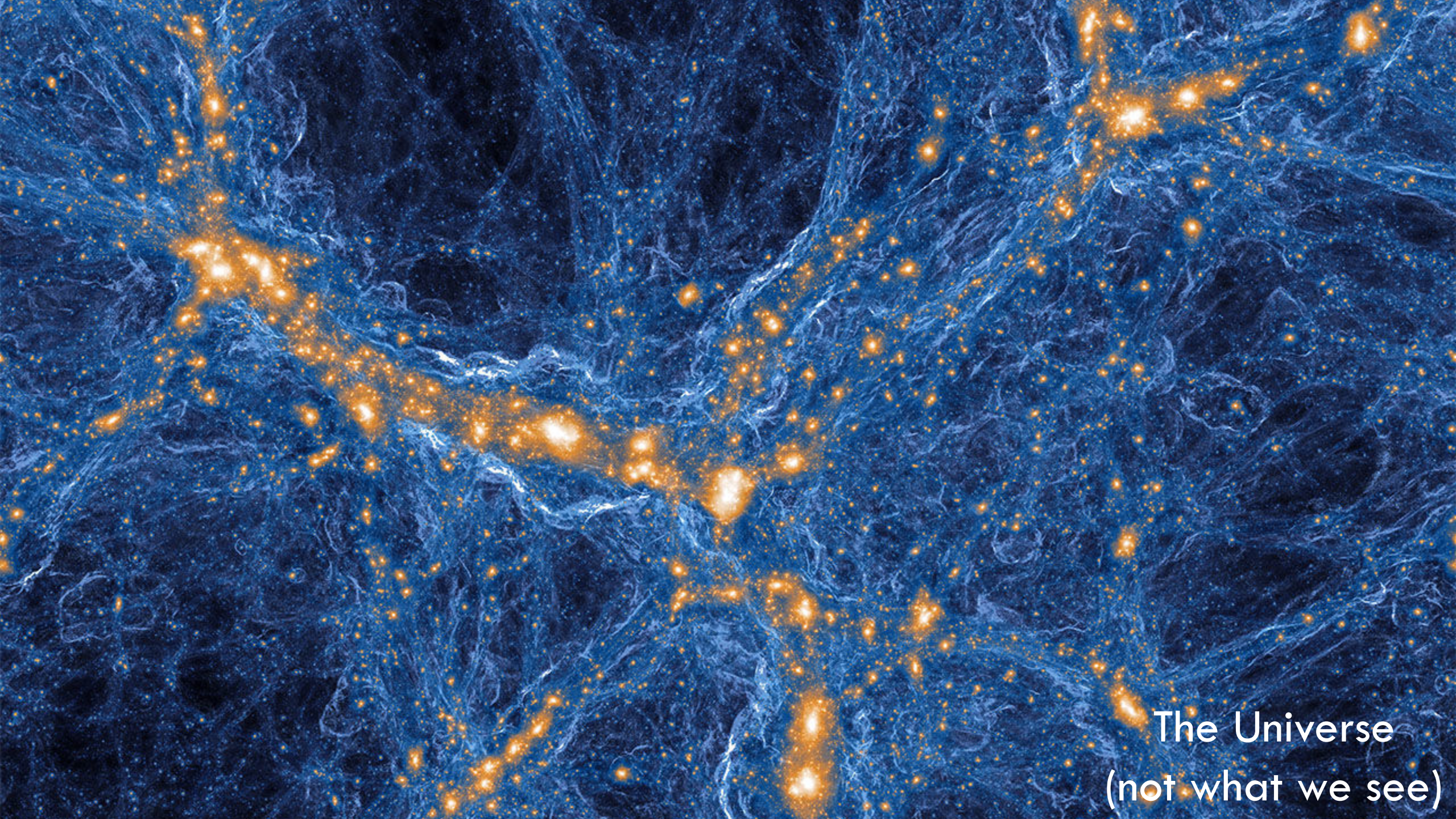
Advisors: David Spergel & Matias Zaldarriaga

Public Thesis Talk, August 31st 2022

* hopefully

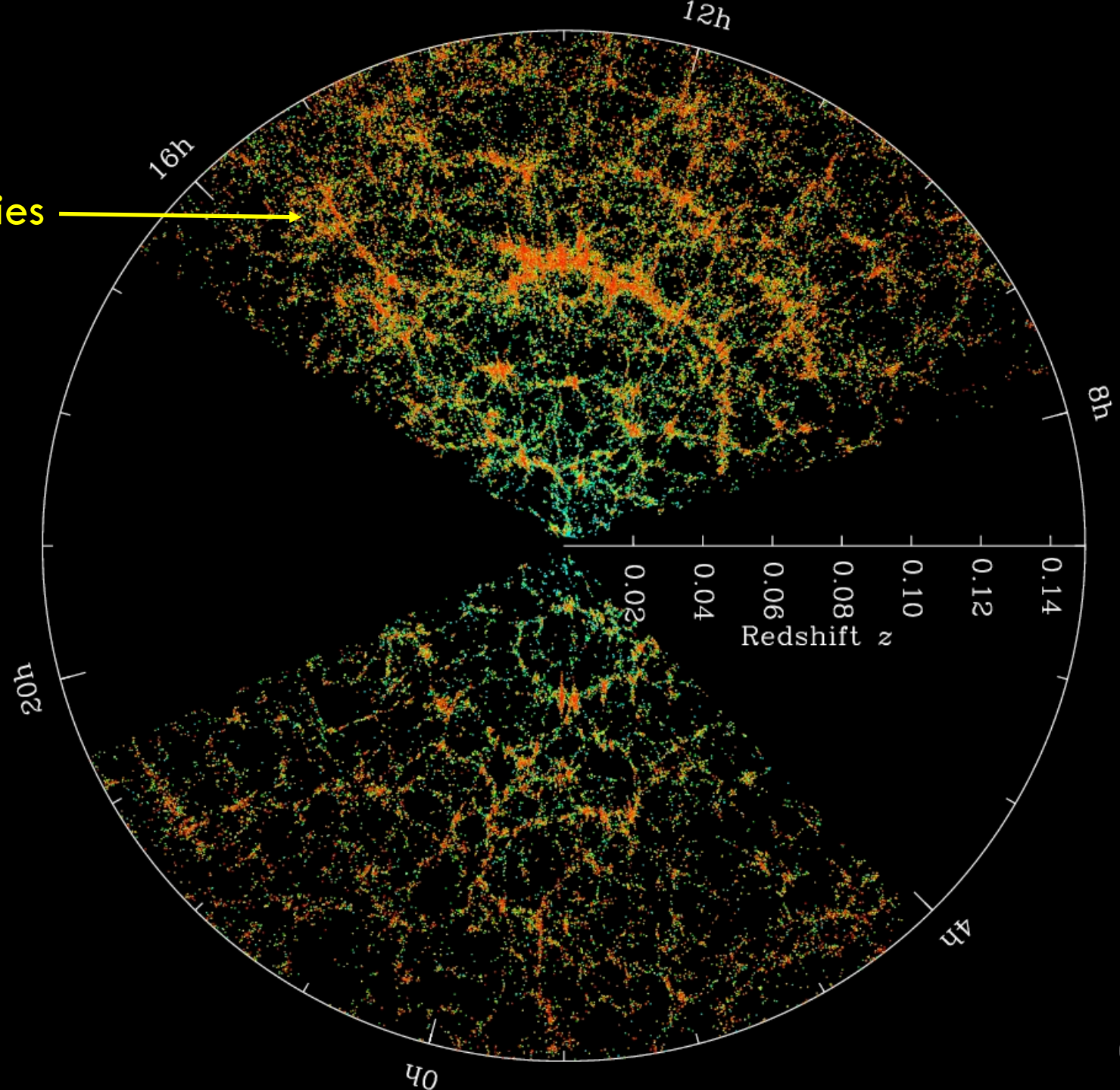


THANK YOU!!!



The Universe
(not what we see)

1 million galaxies



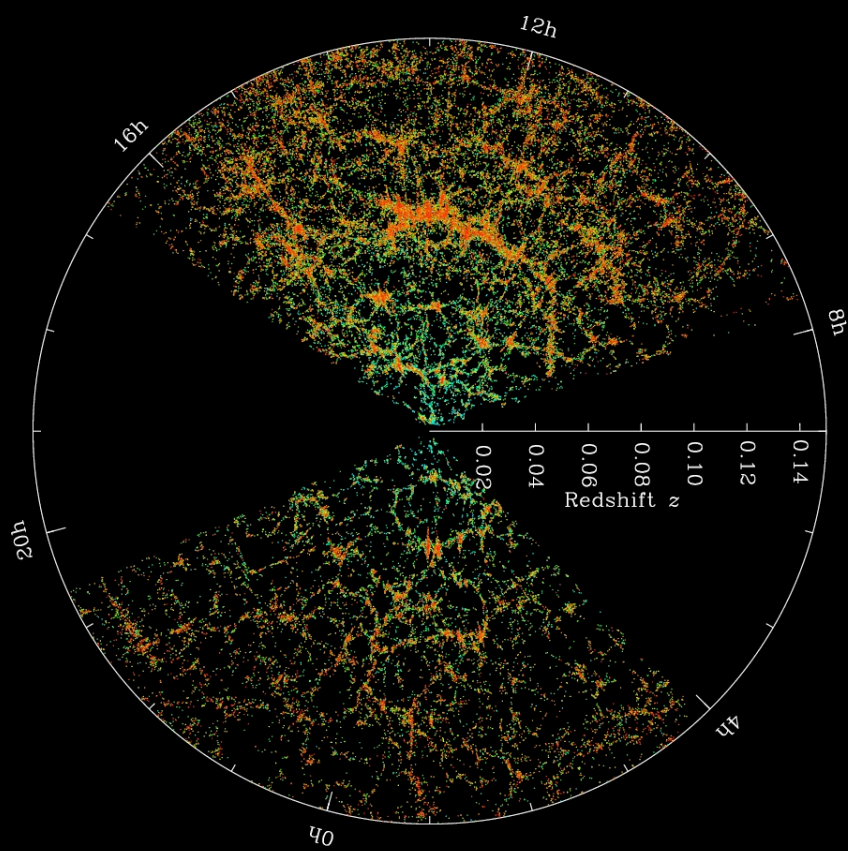
The Universe
(what we see)

1 million galaxies



What can we learn from this map?

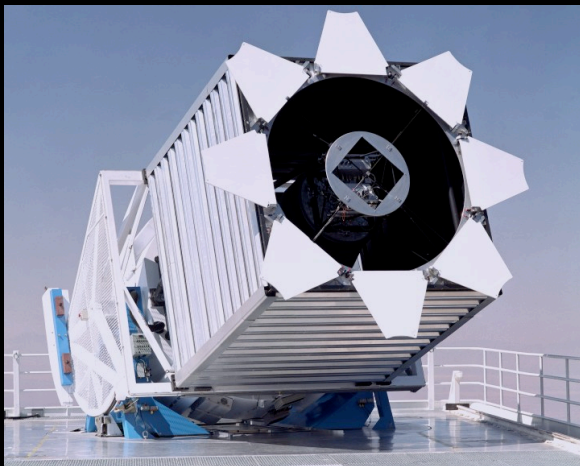
The Universe
(what we see)



What makes up the Universe?
[dark matter, dark energy, baryons, photons]

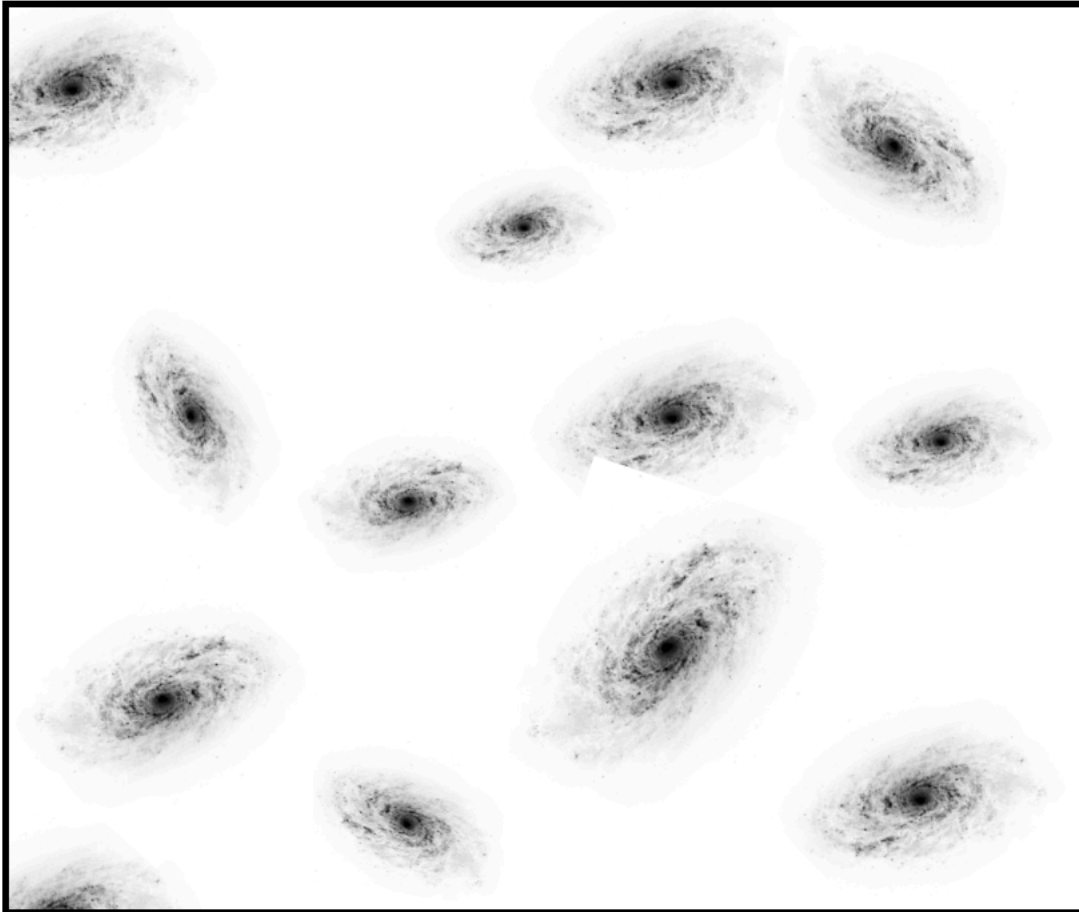
How is the Universe evolving?
[expansion rate, dark energy]

What happened in the early Universe?
[inflation and beyond]



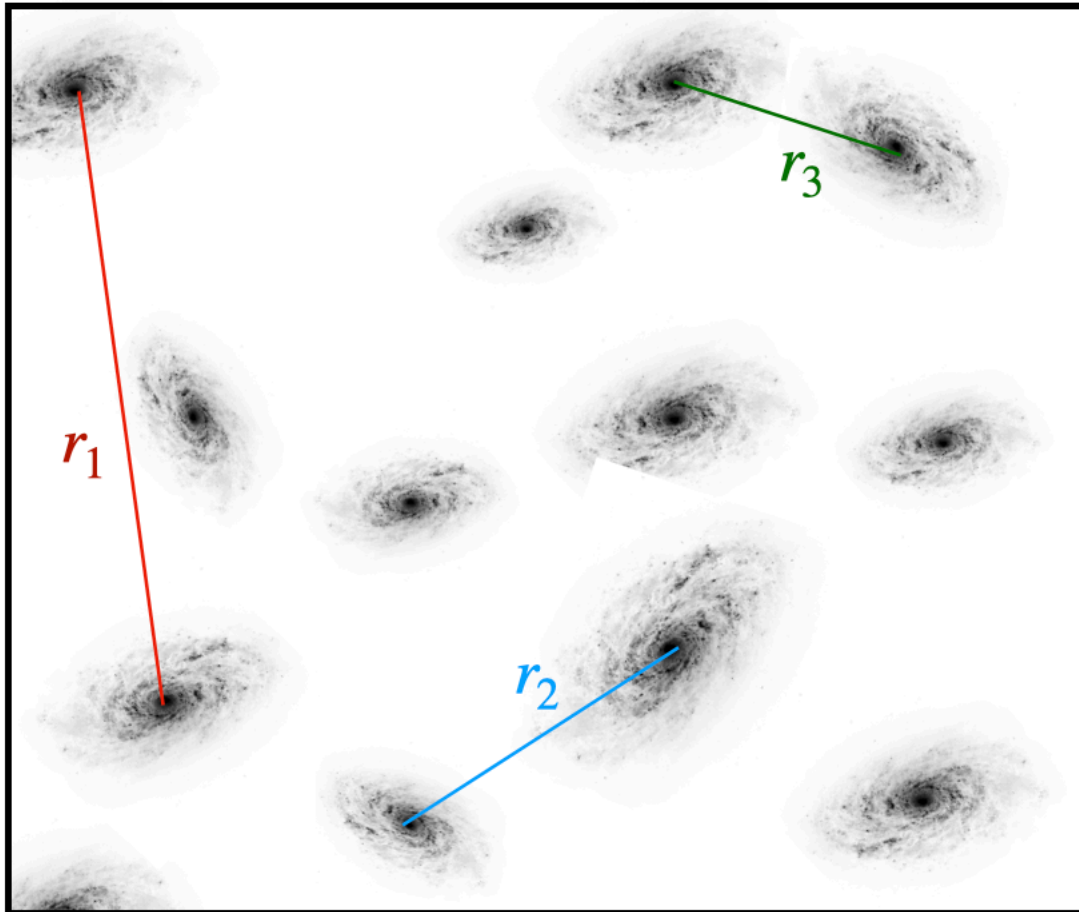
Kitt Peak Observatory

HOW DO WE DESCRIBE A GALAXY DISTRIBUTION?



We need a **statistical** description

HOW DO WE DESCRIBE A GALAXY DISTRIBUTION?



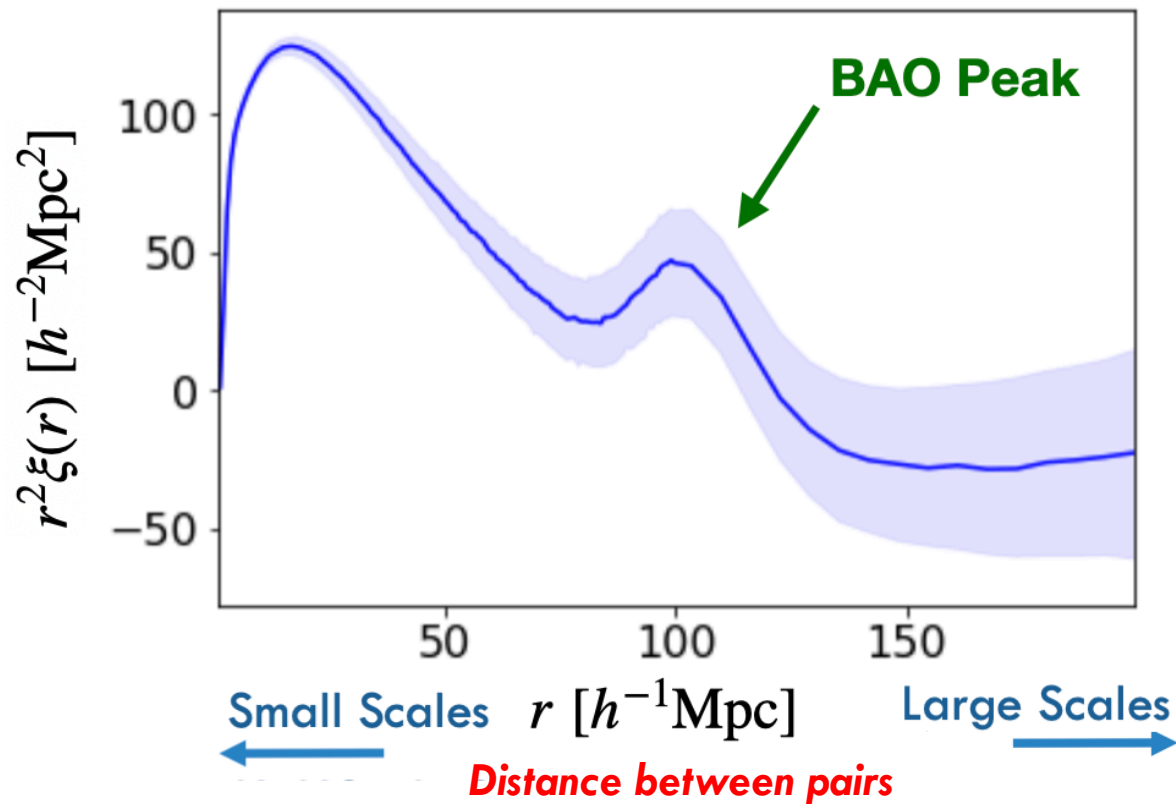
We need a **statistical** description

What's the **average distance**
between **pairs** of galaxies?

Larger distance \leftrightarrow **faster** expansion rate (H_0)

HOW DO WE DESCRIBE A GALAXY DISTRIBUTION?

Correlation Function



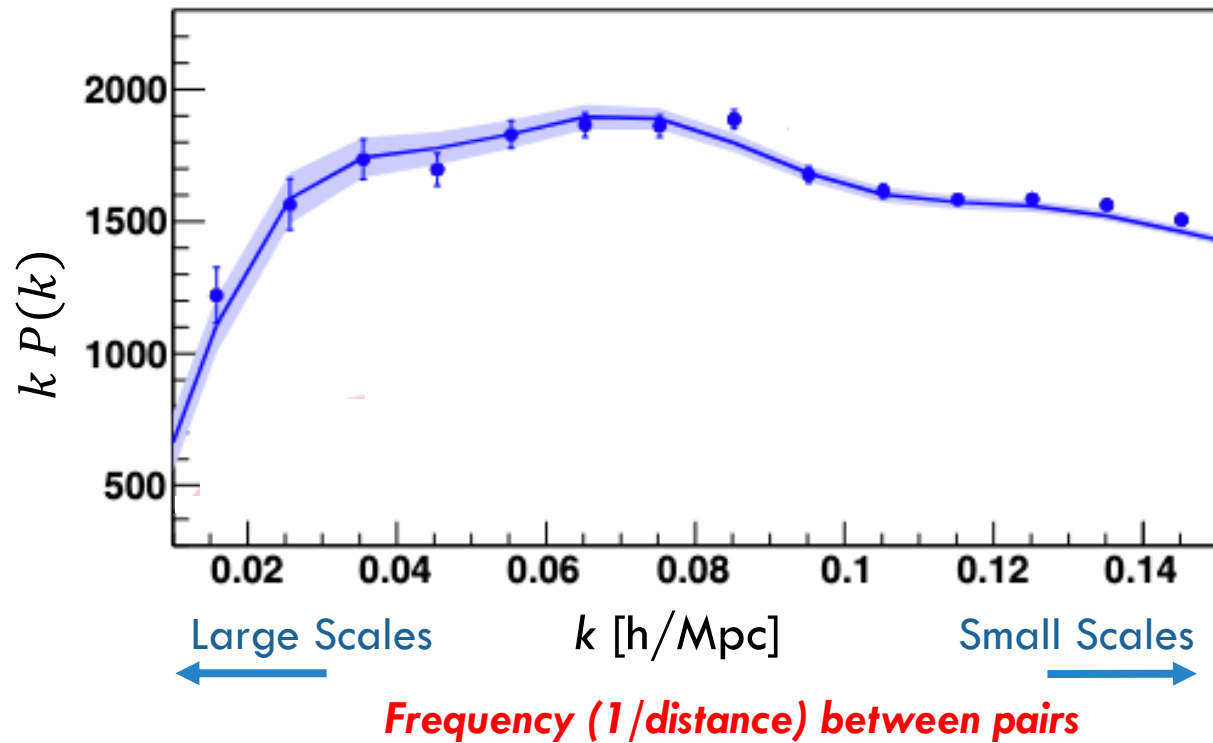
We need a **statistical** description

What's the **distribution** of distances between **pairs** of galaxies?

This depends on **expansion history** and **initial conditions**

HOW DO WE DESCRIBE A GALAXY DISTRIBUTION?

Power Spectrum



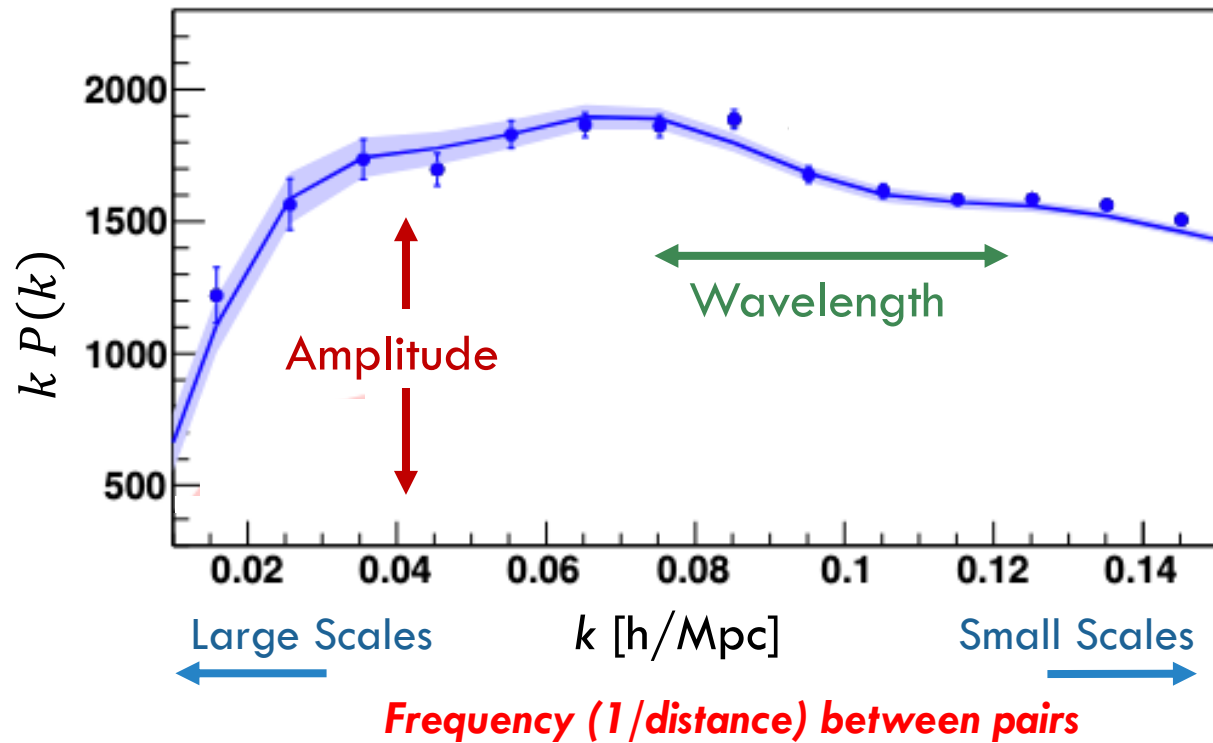
We need a **statistical** description

What's the **distribution** of distances between **pairs** of galaxies?

This depends on **expansion history** and **initial conditions**

HOW DO WE ANALYZE A GALAXY DISTRIBUTION?

Power Spectrum

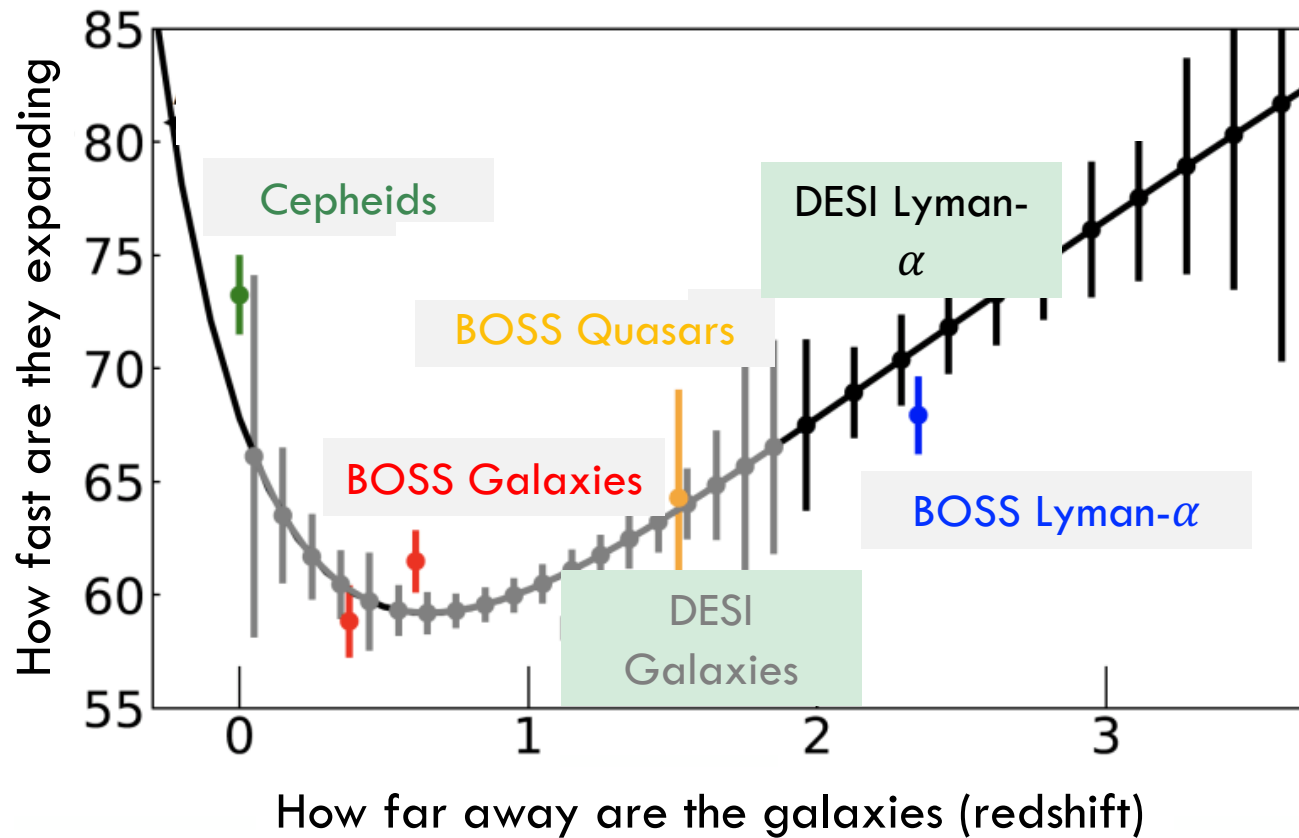


Analyze the galaxy **power spectrum** using a **scaling analysis**

This measures:

- ▷ Primordial **amplitude**
- ▷ **Wiggle** positions

HOW DO WE ANALYZE A GALAXY DISTRIBUTION?



Analyze the galaxy **power spectrum** using a **scaling analysis**

This measures:

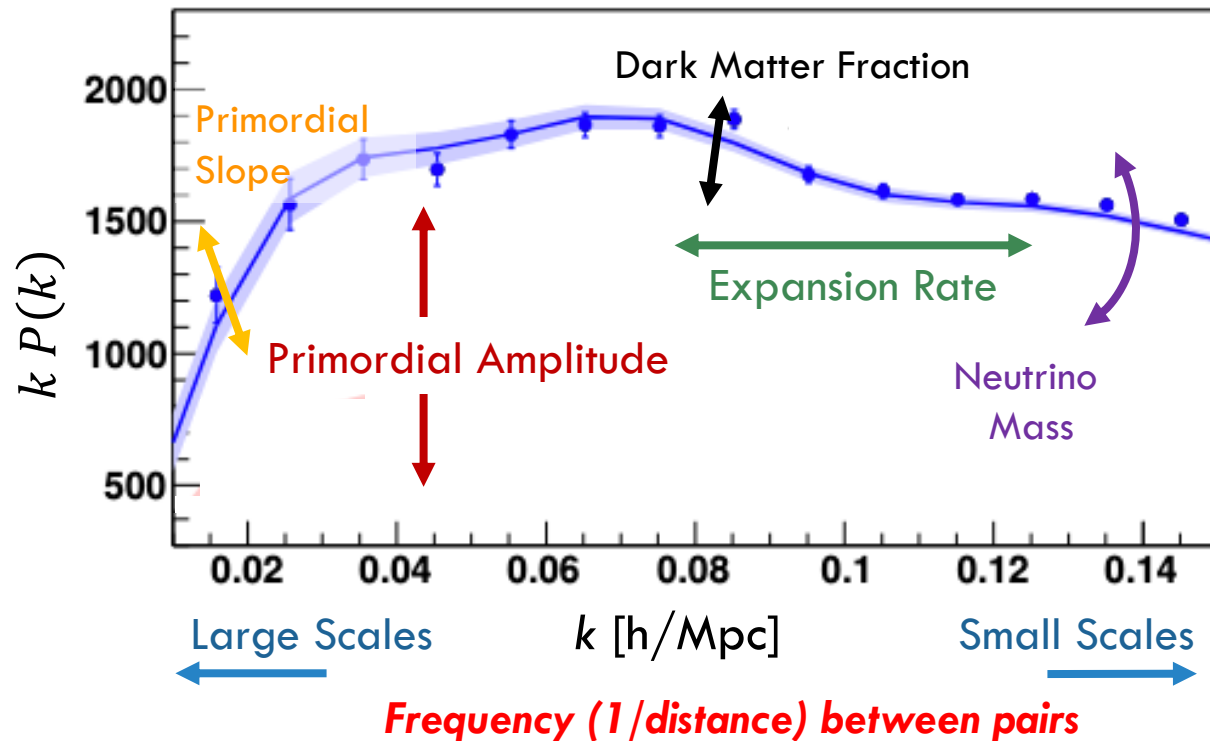
- ▷ Primordial **amplitude**
- ▷ **Wiggle** positions

Robust way to constrain:

- ▷ **Expansion** rate: $H(z), D_A(z)$
- ▷ **Clustering** amplitude: $f\sigma_8(z)$

HOW COULD WE DESCRIBE A GALAXY DISTRIBUTION?

Power Spectrum



We can do **more** with the available data!

The power spectrum depends **directly** on cosmological parameters

THEORETICAL MODELS

Data: observed power spectrum

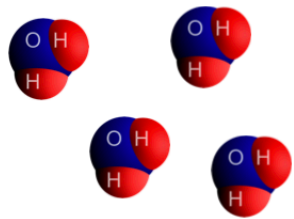
+

Model:

$P = P(\text{dark energy, dark matter, expansion, } \dots)$

=

Constraints



large
scales

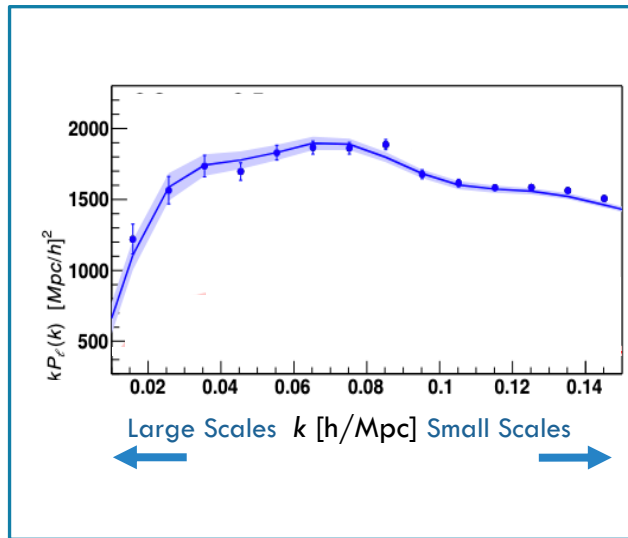
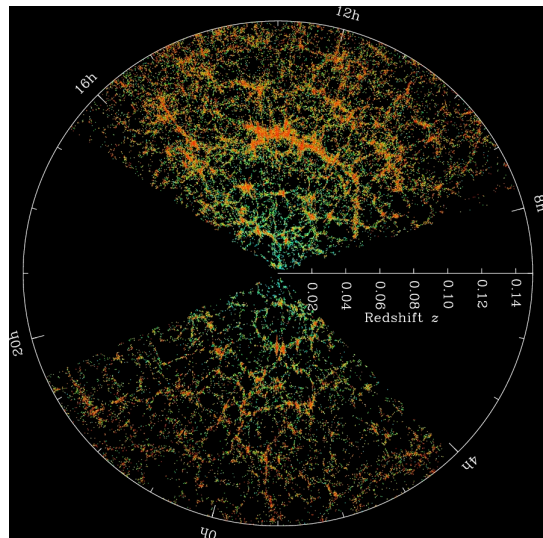


Predict statistics using **Effective Field Theory** of Large Scale Structure

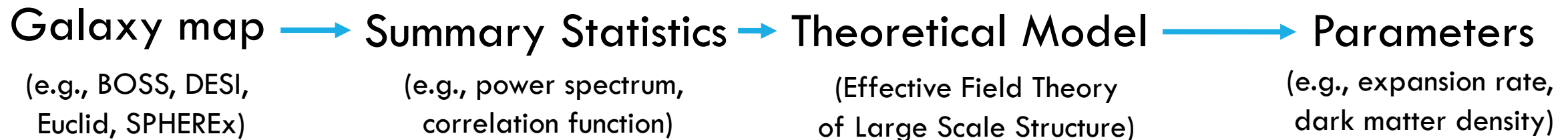
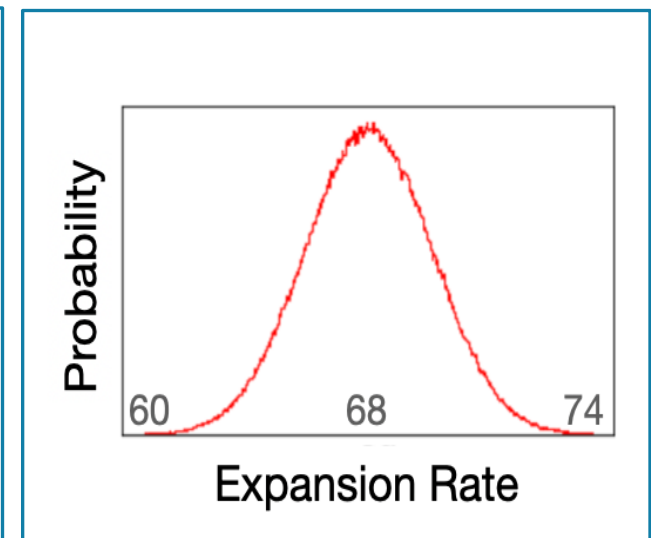
▷ Treats the Universe as an **imperfect** fluid

▷ Includes **back-reaction** of small-scale physics on large-scale modes

LARGE-SCALE STRUCTURE ROADMAP



$$\begin{aligned}
 Z_1(q_1) &= K_1 + f\mu_1^2, & (A.3) \\
 Z_2(q_1, q_2) &= K_2(q_1, q_2) + f\mu_{12}^2 G_2(q_1, q_2) + \frac{f\mu_{12}q_{12}}{2} K_1 \left[\frac{\mu_1}{q_1} + \frac{\mu_2}{q_2} \right] + \frac{(f\mu_{12}q_{12})^2}{2} \frac{\mu_1 \mu_2}{q_1 q_2}, \\
 Z_3(q_1, q_2, q_3) &= K_3(q_1, q_2, q_3) + f\mu_{123}^2 G_3(q_1, q_2, q_3) \\
 &\quad + (f\mu_{123}q_{123}) \left[\frac{\mu_{12}}{q_{12}} K_1 G_2(q_1, q_2) + \frac{\mu_3}{q_3} K_2(q_1, q_2) \right] \\
 &\quad + \frac{(f\mu_{123}q_{123})^2}{2} \left[2 \frac{\mu_{12} \mu_3}{q_{12} q_3} G_2(q_1, q_2) + \frac{\mu_1 \mu_2}{q_1 q_2} K_1 \right] + \frac{(f\mu_{123}q_{123})^3}{6} \frac{\mu_1 \mu_2 \mu_3}{q_1 q_2 q_3}, \\
 Z_4(q_1, q_2, q_3, q_4) &= K_4(q_1, q_2, q_3, q_4) + f\mu_{1234}^2 G_4(q_1, q_2, q_3, q_4) \\
 &\quad + (f\mu_{1234}q_{1234}) \left[\frac{\mu_{123}}{q_{123}} K_1 G_3(q_1, q_2, q_3) + \frac{\mu_4}{q_4} K_3(q_1, q_2, q_3) \right. \\
 &\quad \left. + \frac{\mu_{12}}{q_{12}} G_2(q_1, q_2) K_2(q_3, q_4) \right] \\
 &\quad + \frac{(f\mu_{1234}q_{1234})^2}{2} \left[2 \frac{\mu_{123} \mu_4}{q_{123} q_4} G_3(q_1, q_2, q_3) + \frac{\mu_{12} \mu_{34}}{q_{12} q_{34}} G_2(q_1, q_2) G_2(q_3, q_4) \right. \\
 &\quad \left. + 2 \frac{\mu_{12} \mu_3}{q_{12} q_3} K_1 G_2(q_1, q_2) + \frac{\mu_1 \mu_2}{q_1 q_2} K_2(q_3, q_4) \right] \\
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 &\quad + \frac{(f\mu_{1234}q_{1234})^4}{24} \frac{\mu_1 \mu_2 \mu_3 \mu_4}{q_1 q_2 q_3 q_4},
 \end{aligned}$$

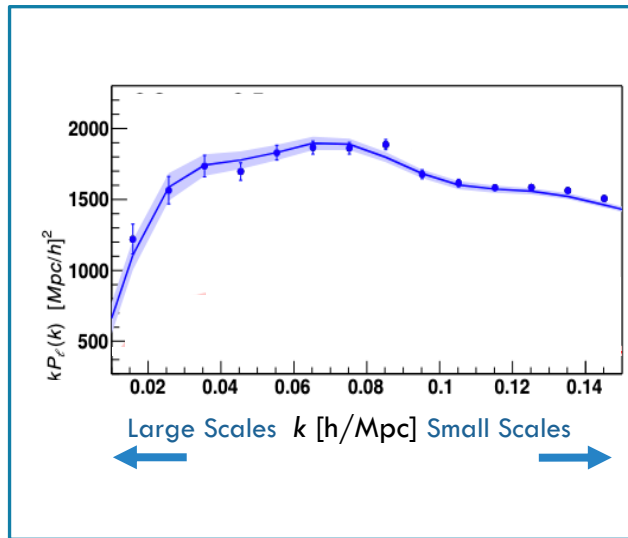
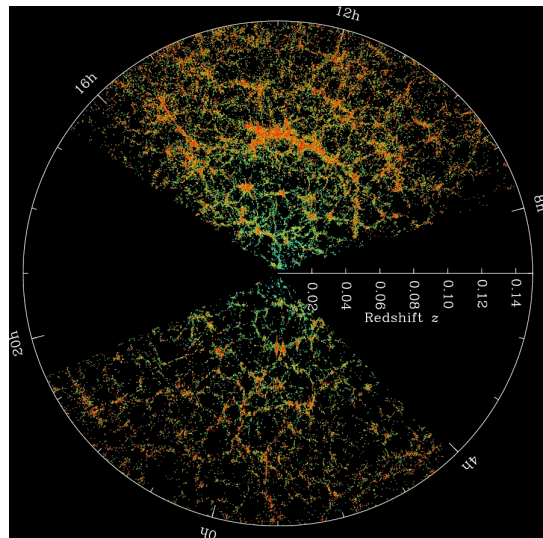


LARGE-SCALE STRUCTURE ROADMAP

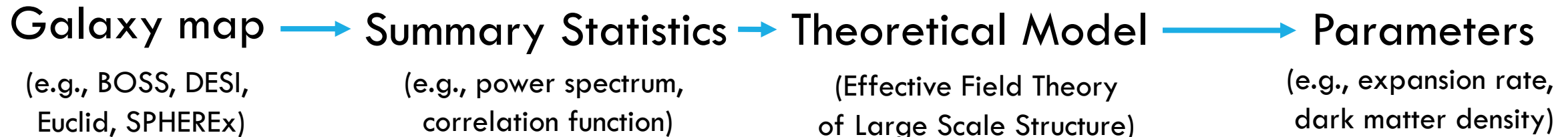
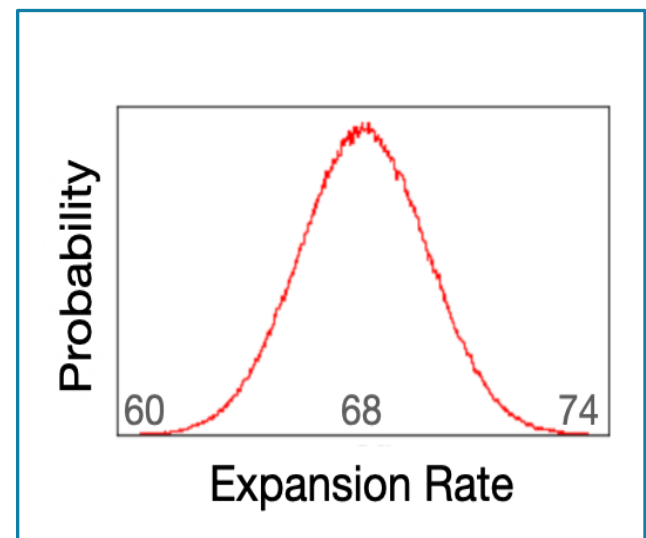
More Statistics!

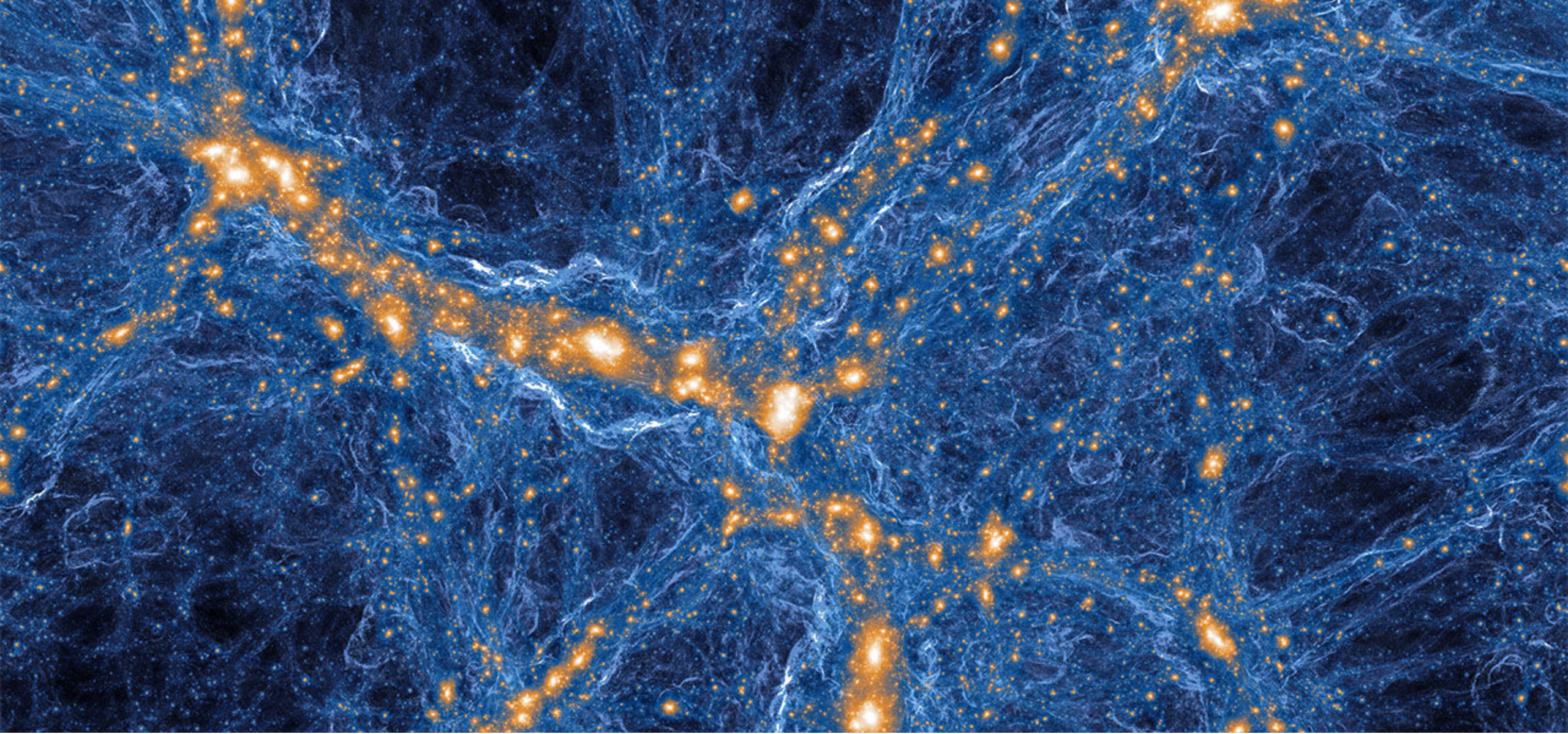
Better Theories!

New Physics!



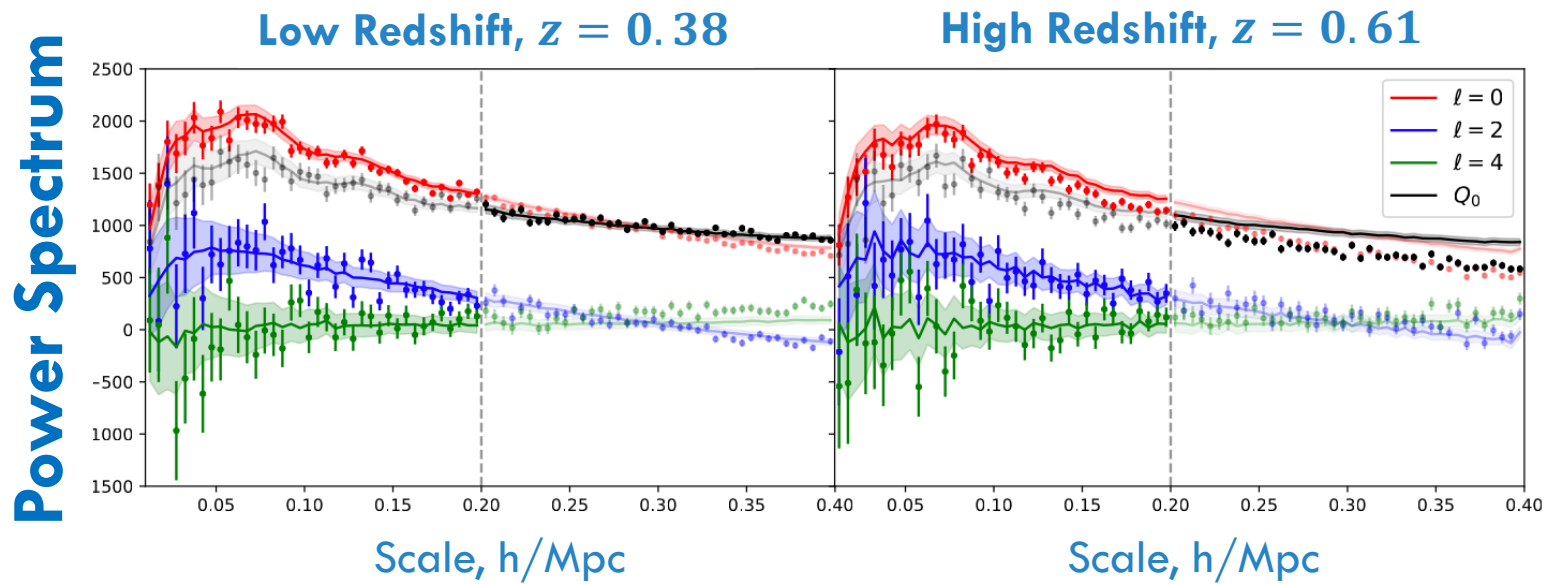
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 \end{aligned}$$



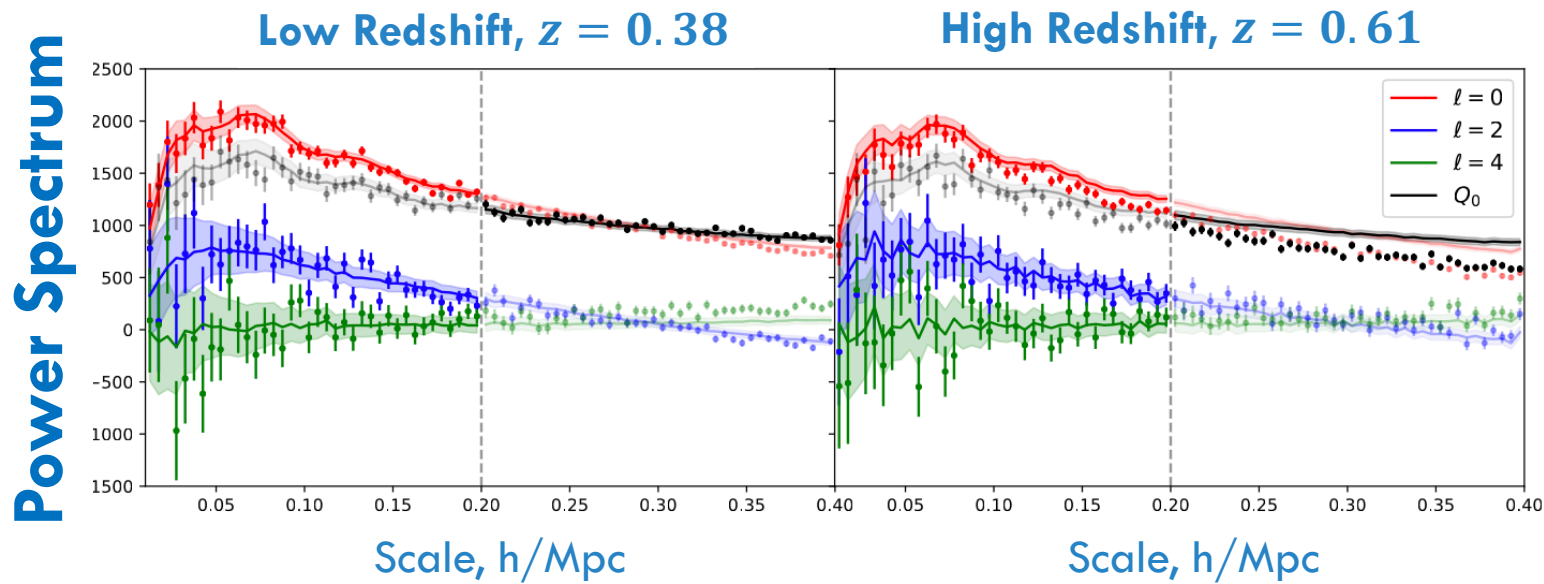


PART I: Cosmology with Galaxy Pairs

THE *UNOFFICIAL* BOSS DR12 ANALYSIS

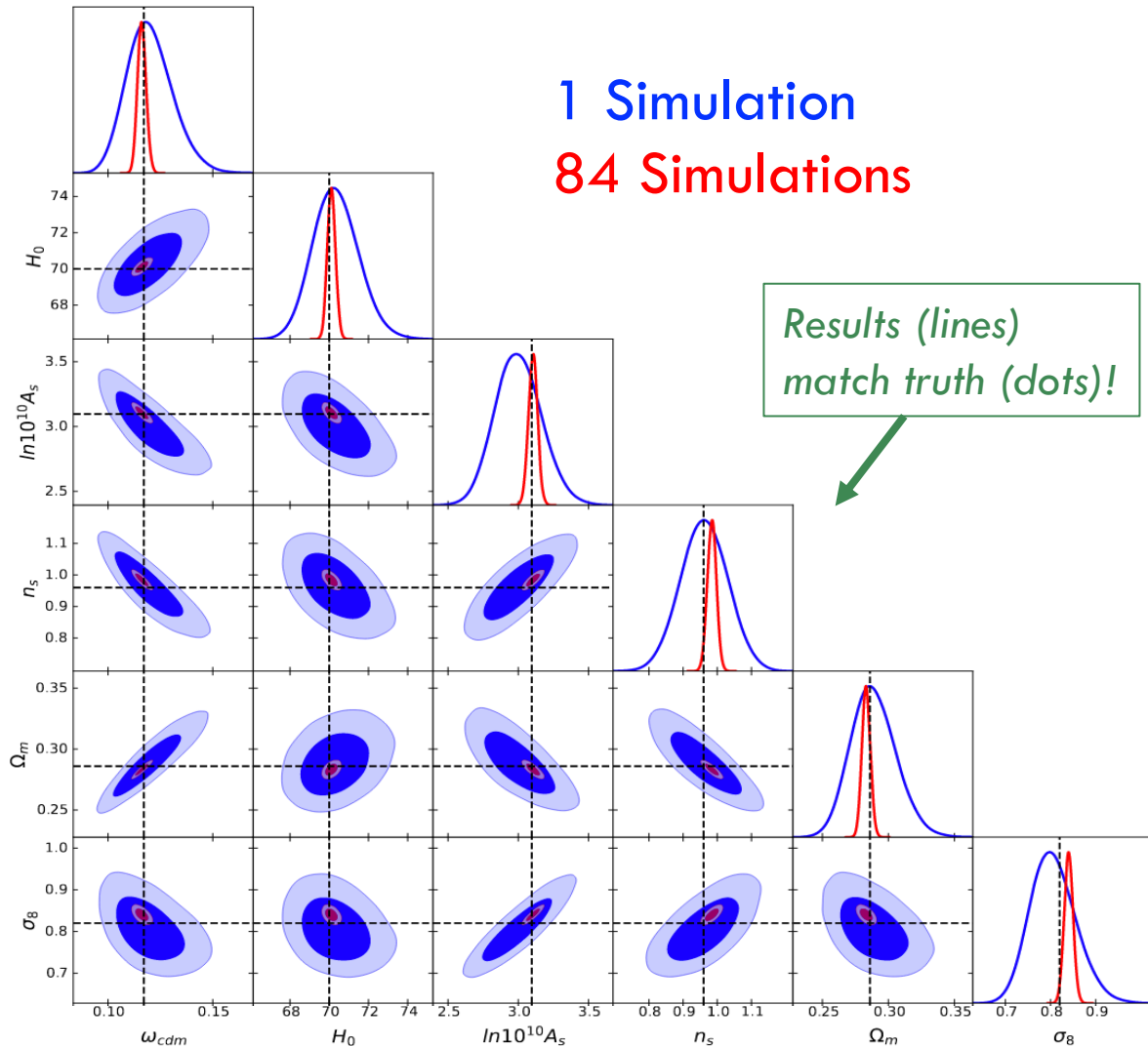


THE *UNOFFICIAL* BOSS DR12 ANALYSIS



Cosmological
Parameters

MODEL VALIDATION



Need to test if the analysis works!

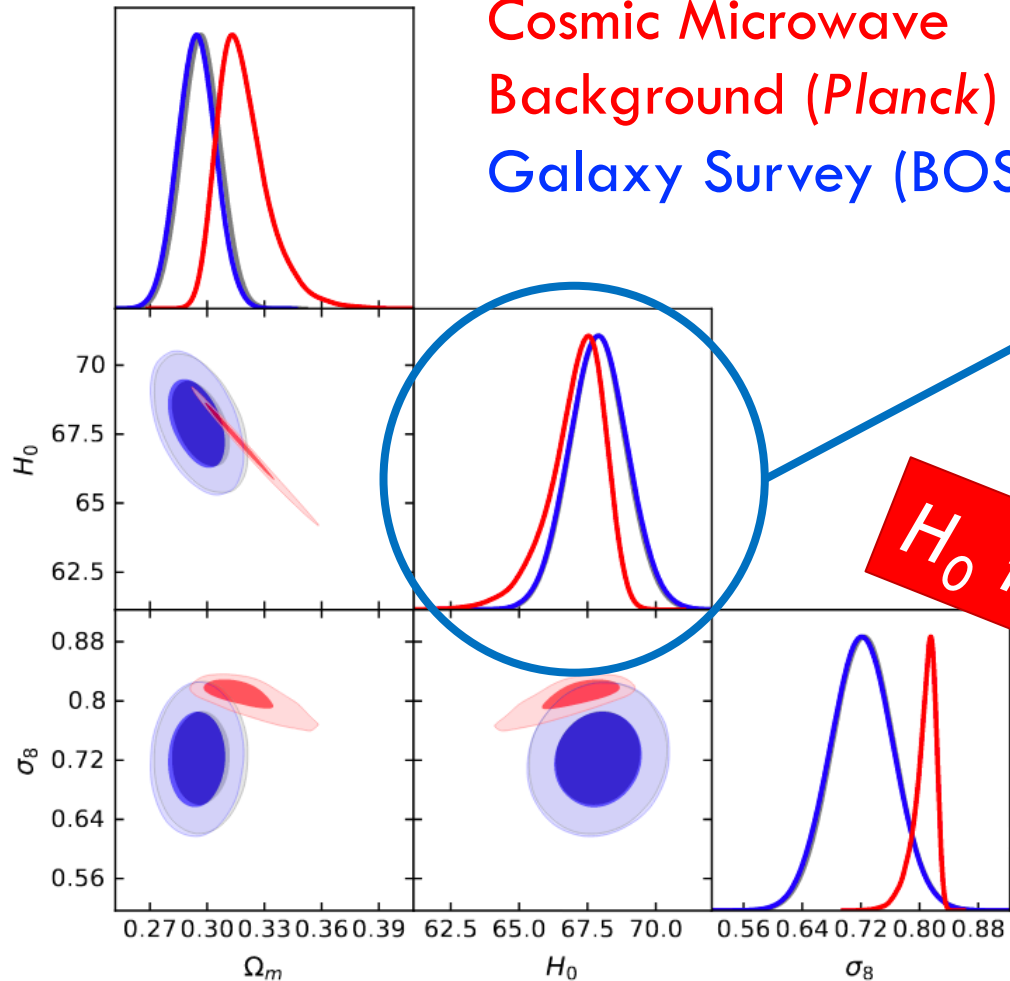
Run pipeline on **simulated** Universes

All parameters recovered at $\ll 1\sigma$

See [GitHub.com/oliverphilcox/full_shape_likelihoods](https://github.com/oliverphilcox/full_shape_likelihoods)

HOW FAST IS THE UNIVERSE EXPANDING?

Cosmic Microwave
Background (*Planck*)
Galaxy Survey (BOSS)



H₀ tension?

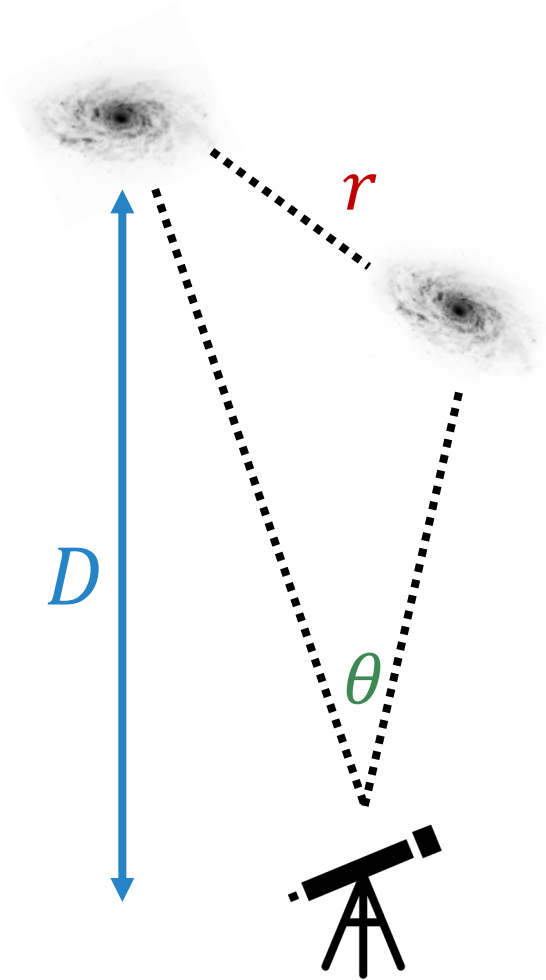
We find the following expansion rate:

$$H_0 = 68.3 \pm 0.8 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

- Galaxies agree with the **Cosmic Microwave Background** (*Planck*, $H_0 \approx 68$)
- Galaxies do **not** agree with observations of **Supernovae** (*SHOES*, $H_0 \approx 74$)

How do we make this measurement?

COSMIC RULERS



To measure the **expansion rate** using galaxies we need to know their **distance**

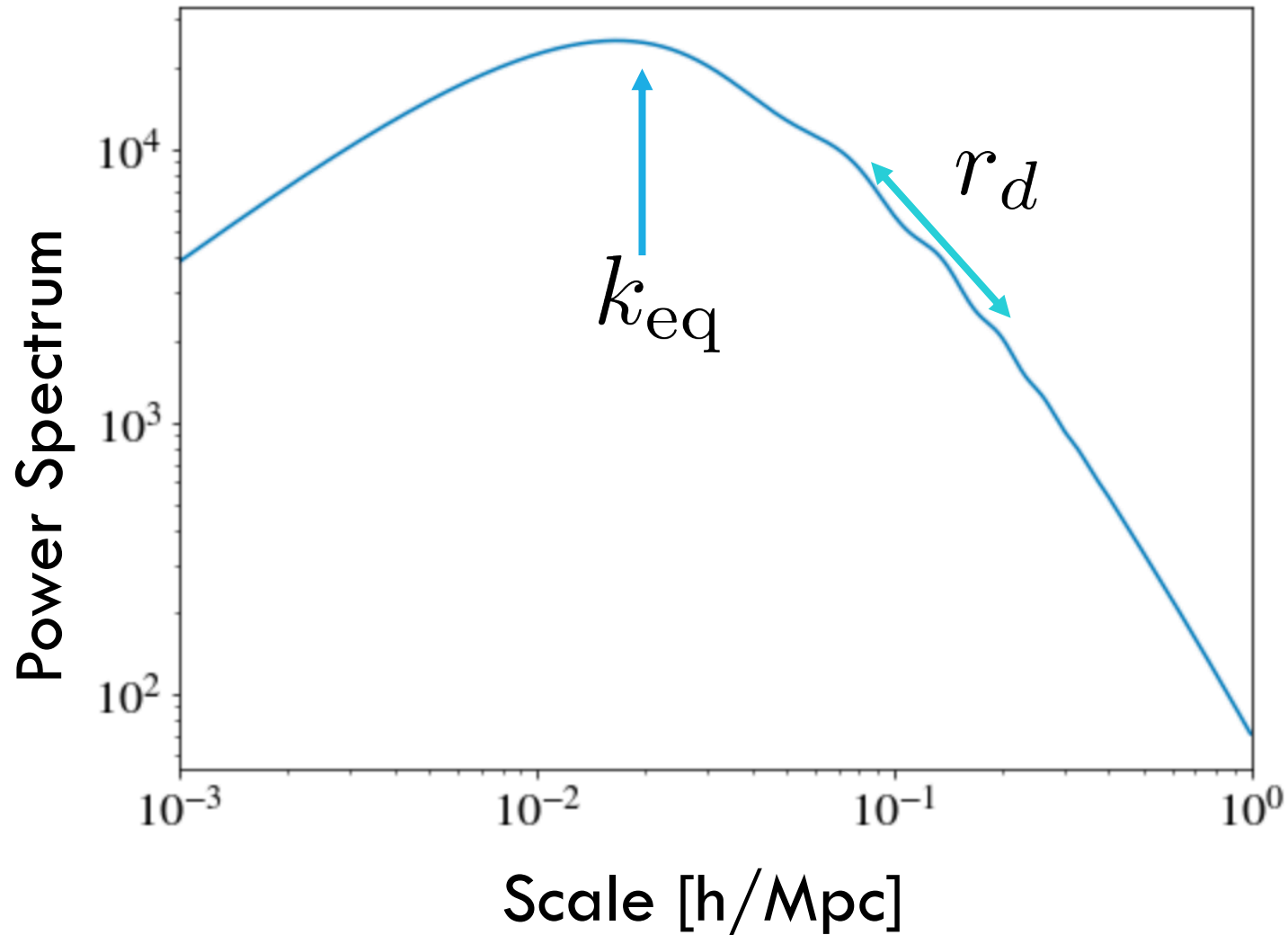
If we know the **angular** and **physical** separation of pairs, we can measure this!

$$D = r / \theta$$

$$D \propto 1 / H_0$$

What **physical scale** should we use?

TWO COSMIC RULERS FOR H_0



1. Sound Horizon: r_d

- ▷ Distance **sound waves** travelled in the early Universe (redshift $z \sim 1100$)

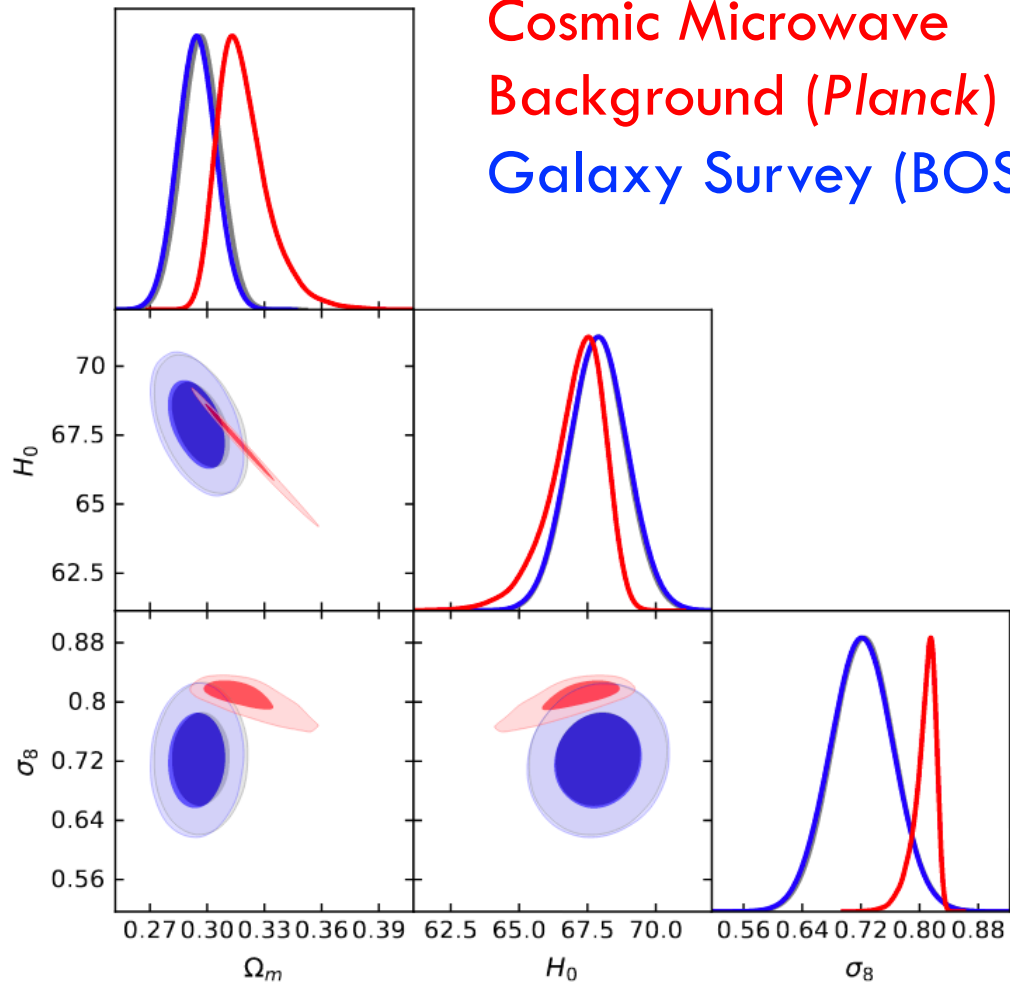
2. The Equality Scale: k_{eq}^{-1}

- ▷ Distance **light** travelled at radiation-matter equality (redshift $z \sim 3600$)

Both can be used to extract H_0

TESTING EARLY UNIVERSE PHYSICS

Cosmic Microwave
Background (*Planck*)
Galaxy Survey (BOSS)



Full data (sound horizon + equality) :

$$(z \approx 1100) \quad H_0 = 68.3 \pm 0.8 \text{ km s}^{-1} \text{Mpc}^{-1}$$

Sound-horizon-marginalized (equality) :

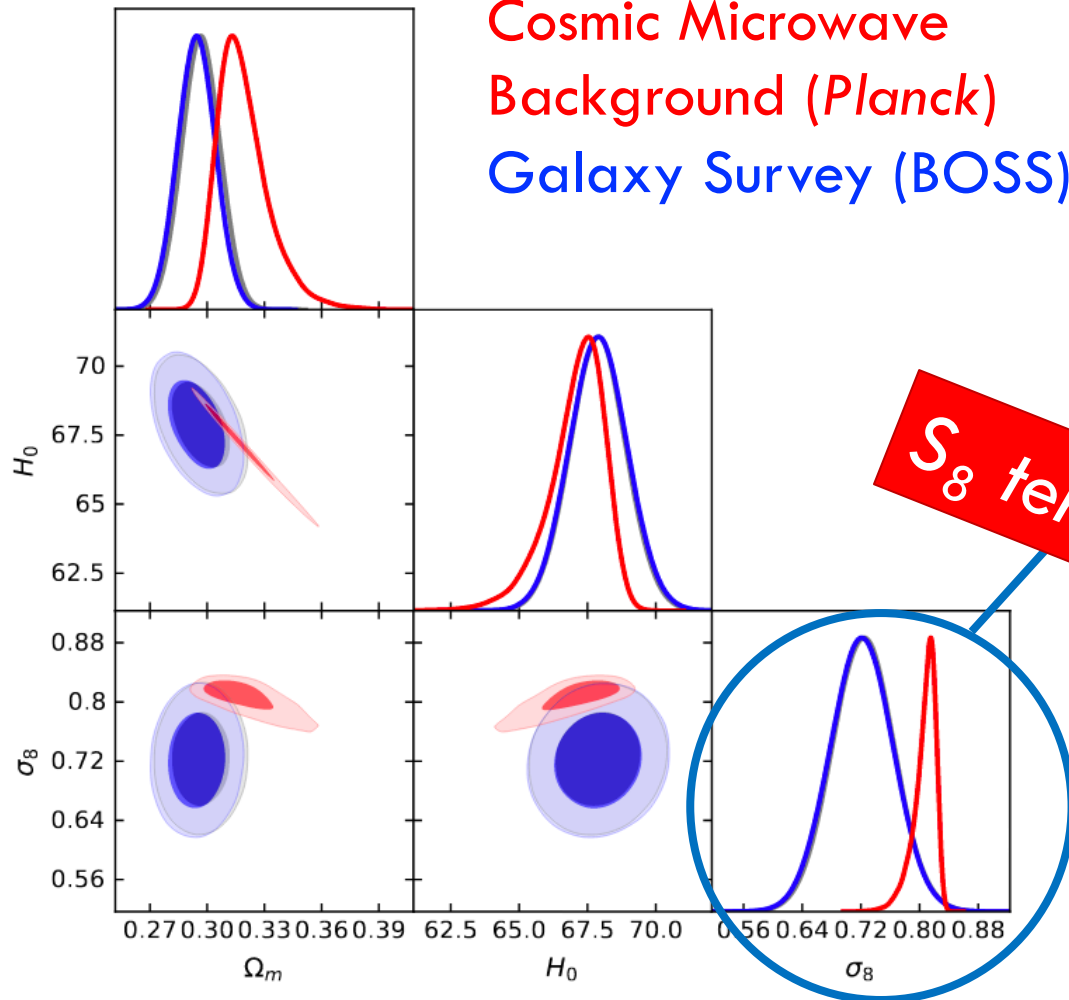
$$(z \approx 3500) \quad H_0 = 67.1 \pm 2.7 \text{ km s}^{-1} \text{Mpc}^{-1}$$

The two results are **consistent**

\Rightarrow **No evidence** for new early Universe physics!

HOW MUCH STRUCTURE IS THERE IN THE UNIVERSE?

Cosmic Microwave
Background (*Planck*)
Galaxy Survey (BOSS)



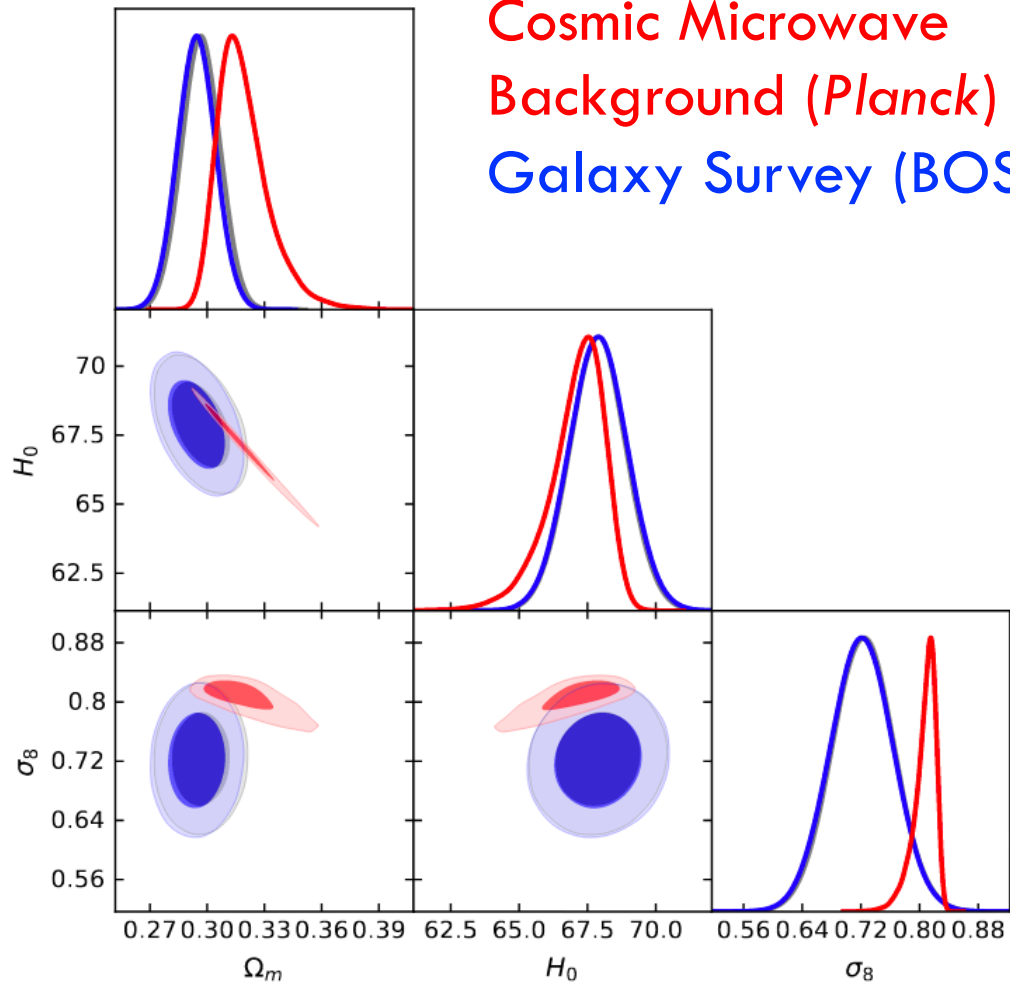
We find the following clustering
amplitude:

$$S_8 = 0.73 \pm 0.04$$

- Galaxies agree with **gravitational lensing**
(DES, $S_8 \approx 0.78 \pm 0.02$)
- Galaxies are a **bit lower** than the **cosmic microwave background**
(*Planck*, $S_8 \approx 0.83 \pm 0.01$)

WHAT ELSE CAN WE LEARN?

Cosmic Microwave
Background (*Planck*)
Galaxy Survey (BOSS)



What fraction of the Universe is matter?

$$\Omega_m = 0.34 \pm 0.02$$

Consistent with supernova observations

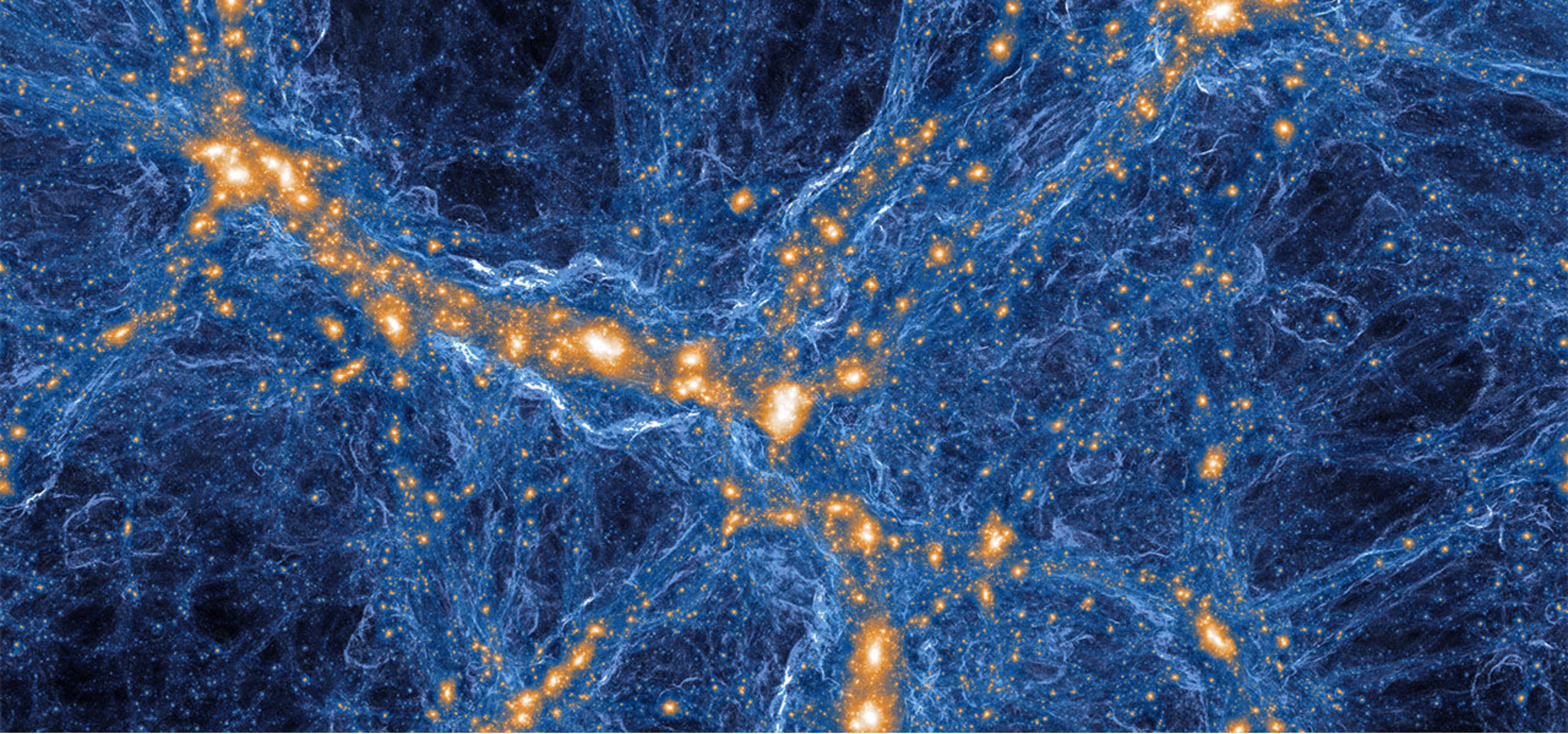
What was the early Universe like?

$$n_s = 0.87 \pm 0.07$$

Consistent with *Planck*

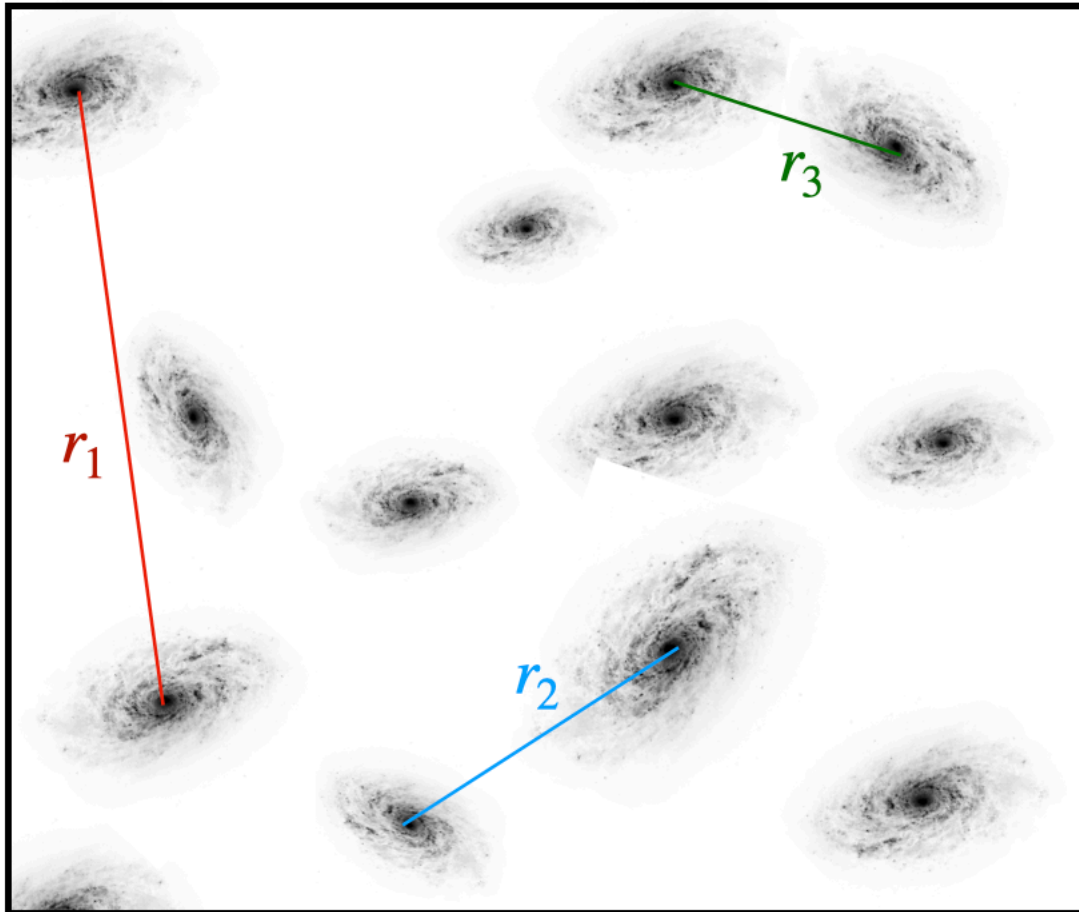
How heavy are neutrinos?

$$\sum m_\nu < 0.14 \text{ eV (95\% CL)}$$



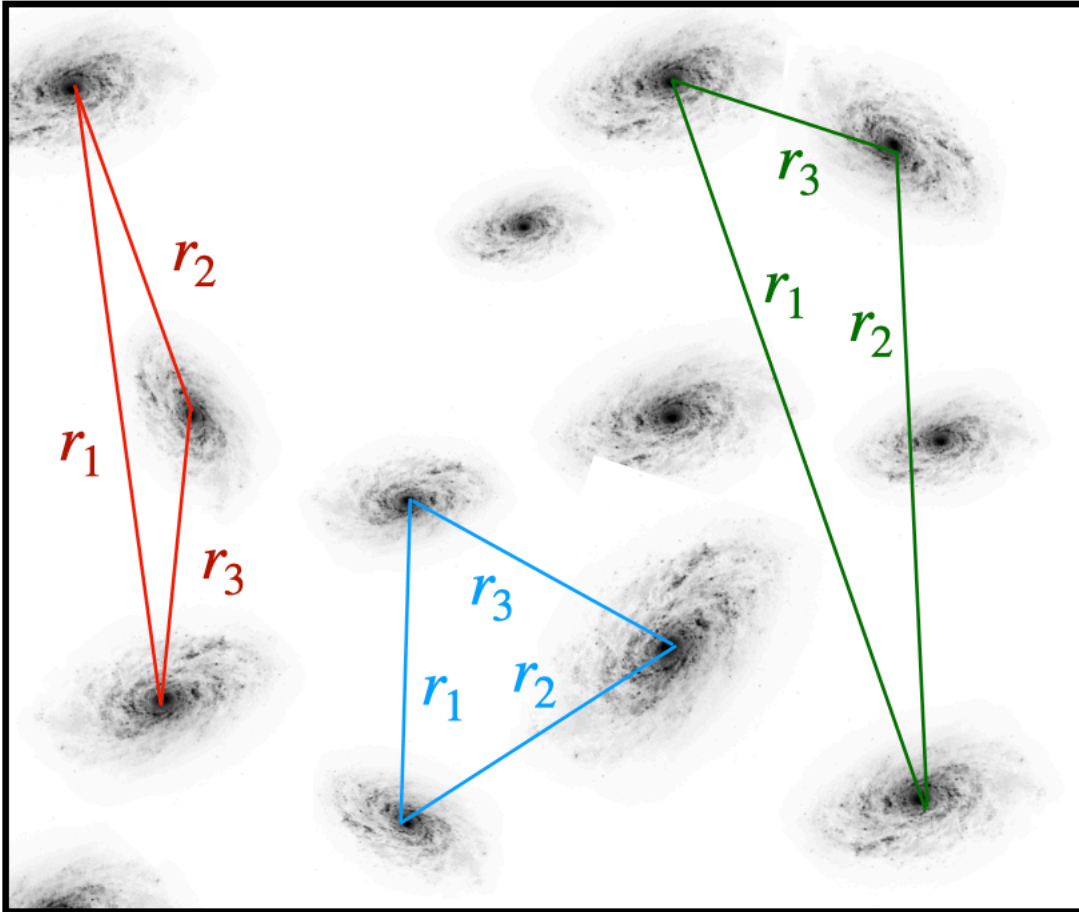
PART II: Cosmology with Galaxy Triplets

HOW DO WE DESCRIBE A GALAXY DISTRIBUTION?



The galaxy distribution is **not** fully described by **pairs** of points

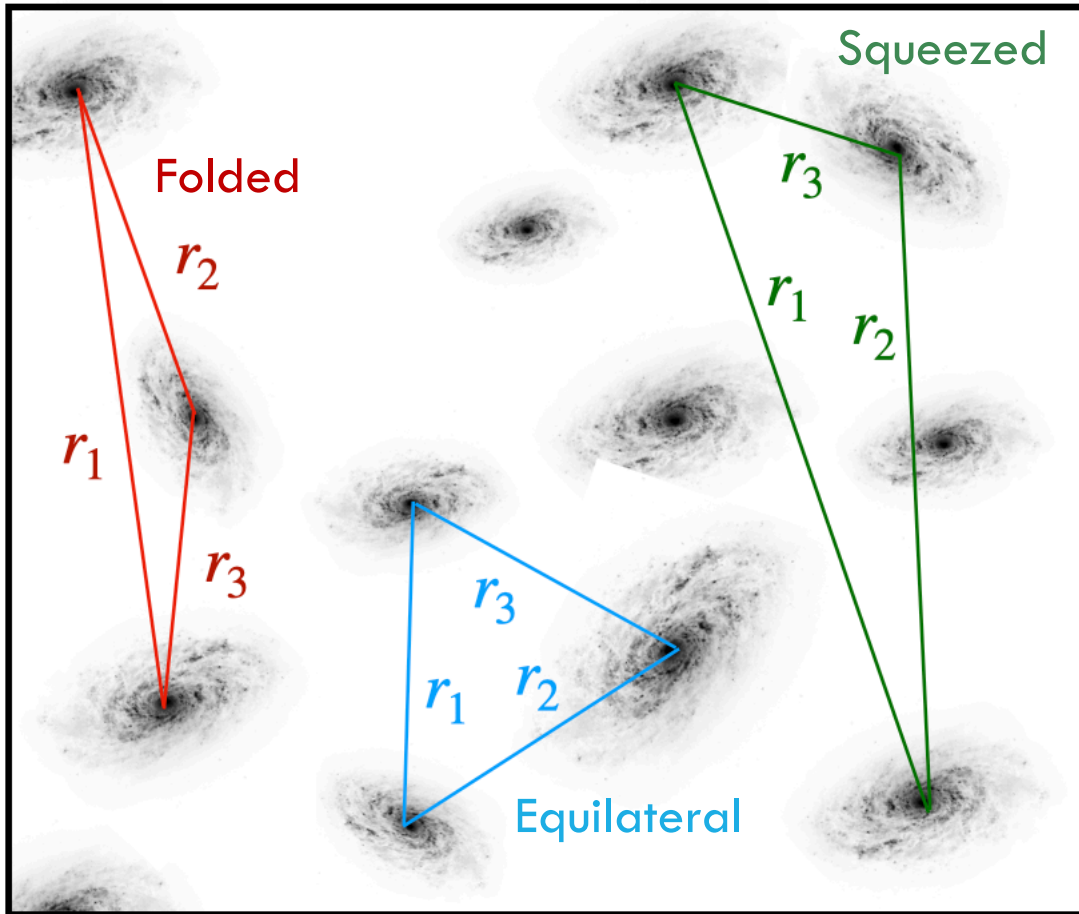
HOW DO WE DESCRIBE A GALAXY DISTRIBUTION?



The galaxy distribution is **not** fully described by **pairs** of points

What's the **distribution** of distances between **triplets** of galaxies?

HOW DO WE DESCRIBE A GALAXY DISTRIBUTION?



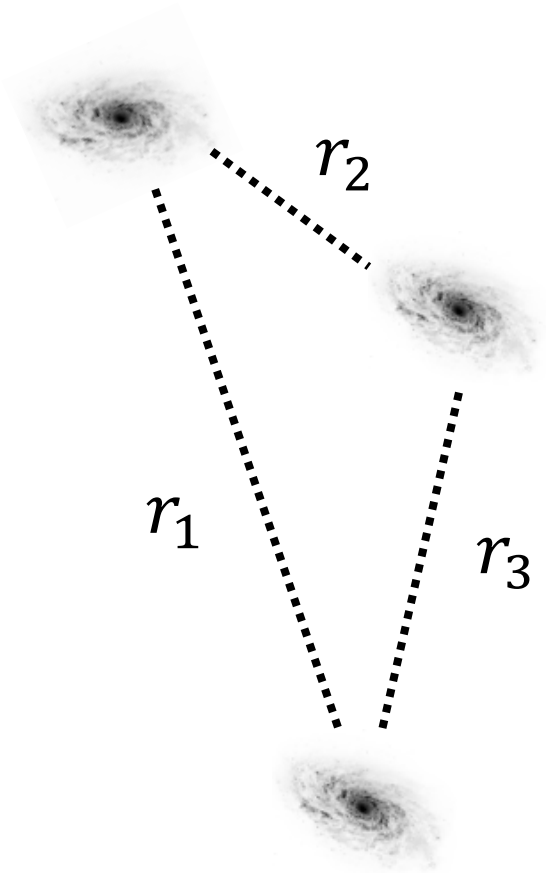
The galaxy distribution is **not** fully described by **pairs** of points

What's the **distribution** of distances between **triplets** of galaxies?

This also depends on **expansion history** and **initial conditions**

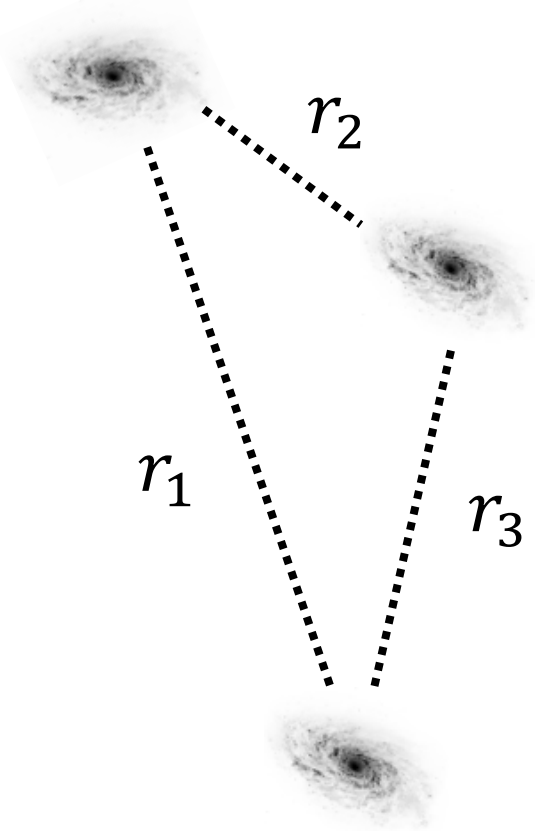
More constraining power for free!

THREE-POINT STATISTICS



The **three-point correlation function** (or **bispectrum**)
=
Probability three galaxies make a **triangle** with sides r_1, r_2, r_3

THREE-POINT STATISTICS

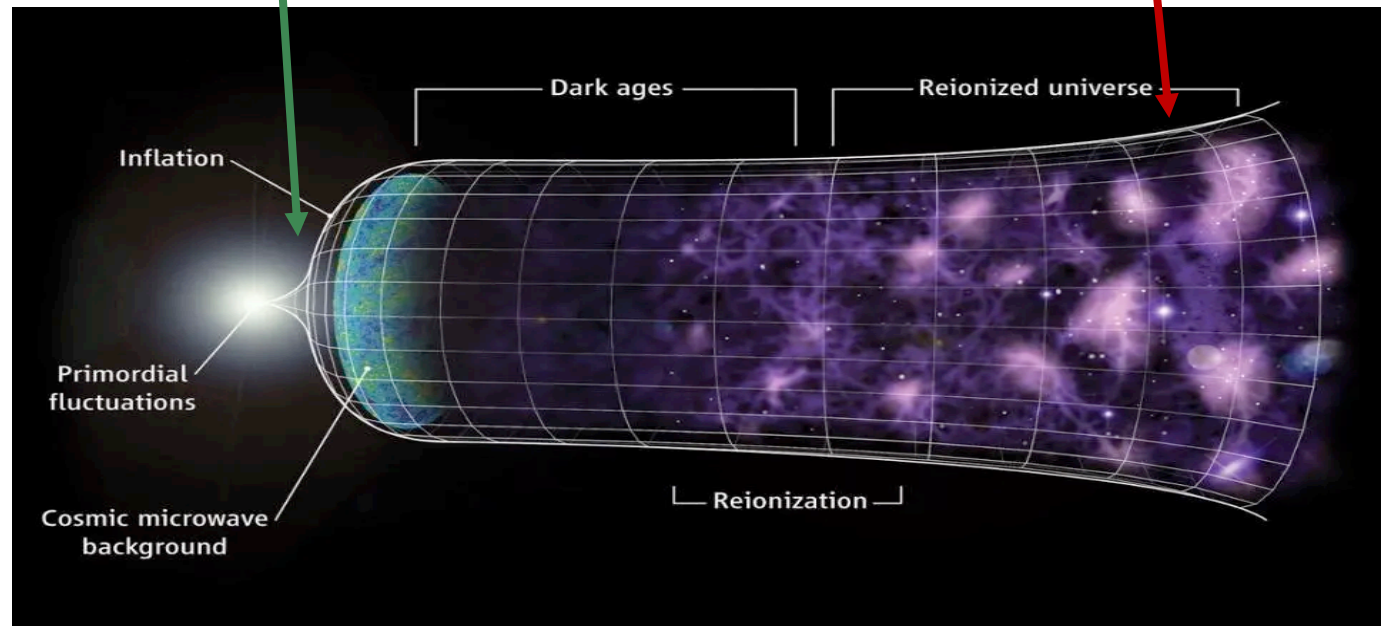


The **three-point correlation function** (or **bispectrum**)
=
Probability three galaxies make a **triangle** with sides r_1, r_2, r_3

Bispectra from inflation

Bispectra from gravity

THE BEGINNING



TODAY

BISPECTRA ARE HARD (PART I)

Problem: We don't measure the **true** distribution of galaxies

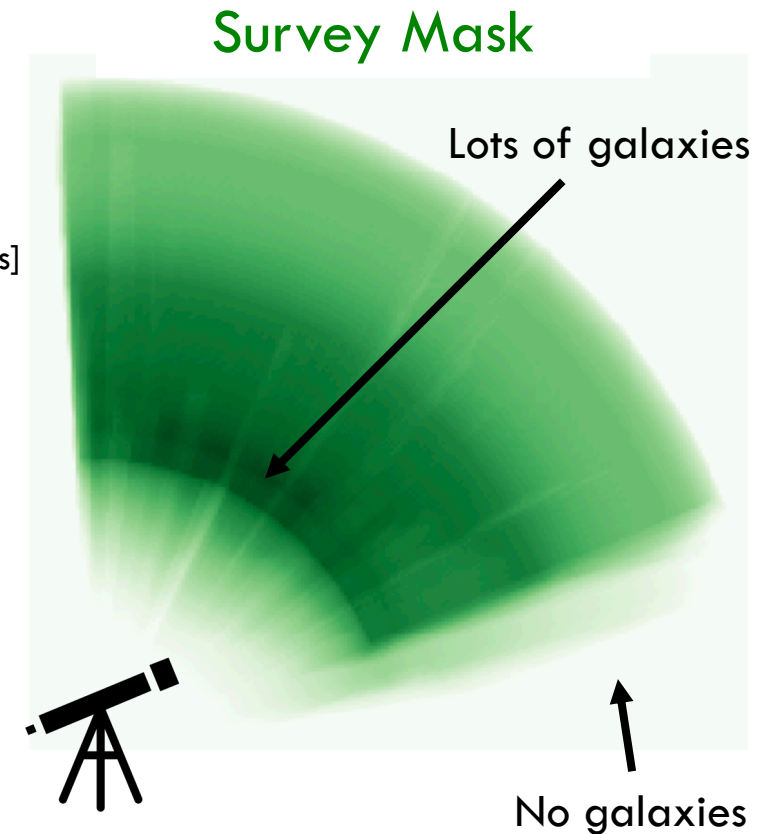
$$\text{Observed distribution} = \text{true distribution} \times \text{mask}$$

This propagates to the **power spectrum** and **bispectrum** [via 6D convolutions]

$$\text{Observed bispectrum} = \text{true bispectrum} * \text{mask} * \text{mask} * \text{mask}$$

Solution: account for the **mask** in the **theory** model

This is hard for the bispectrum and beyond!



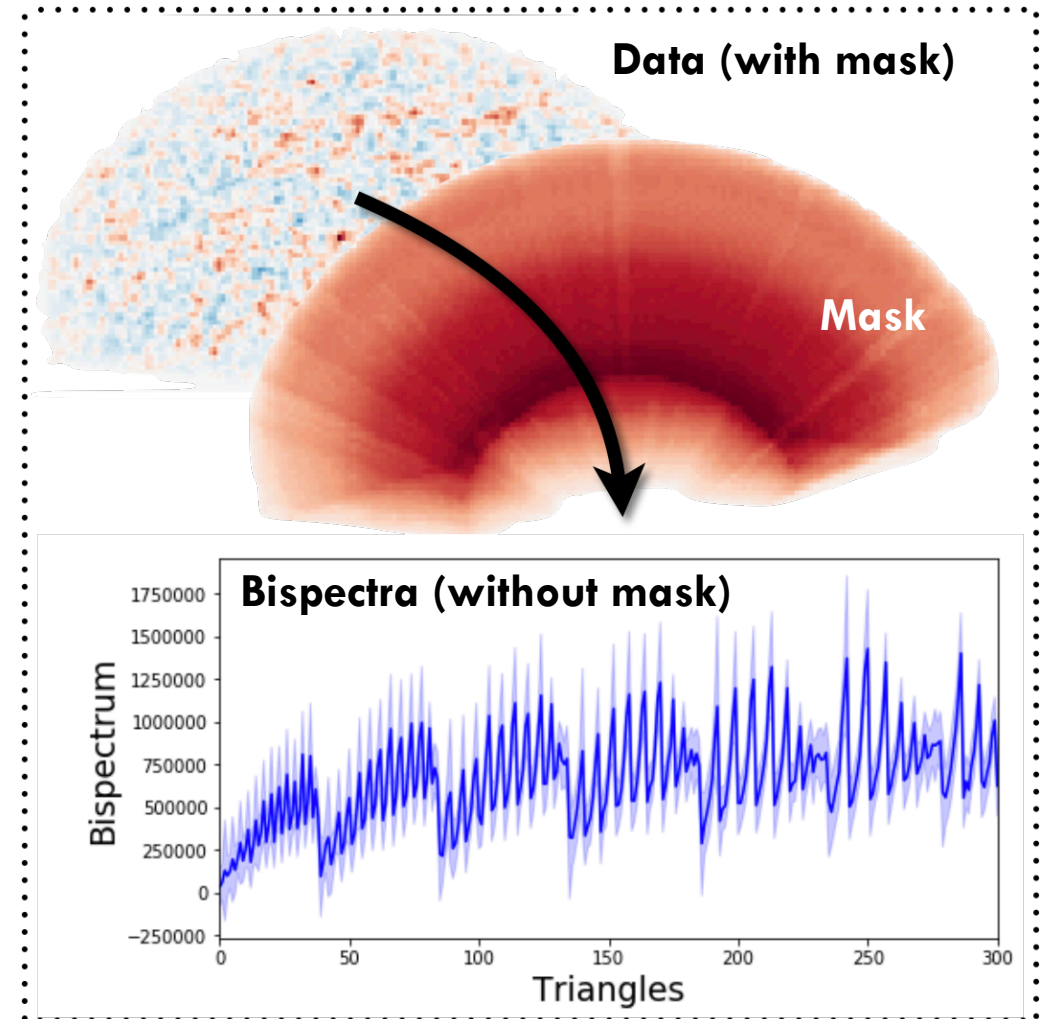
BISPECTRA ARE HARD (PART I)

Alternative: Measure the **true** bispectrum **directly**

$$\text{Observed bispectrum} = \text{true bispectrum} * \text{mask} * \text{mask} * \text{mask}$$

This is possible via **maximum-likelihood** estimators which **deconvolve** the mask → **no tricky modeling!**

This makes robust bispectrum analyses possible!



BISPECTRA ARE HARD (PART II)

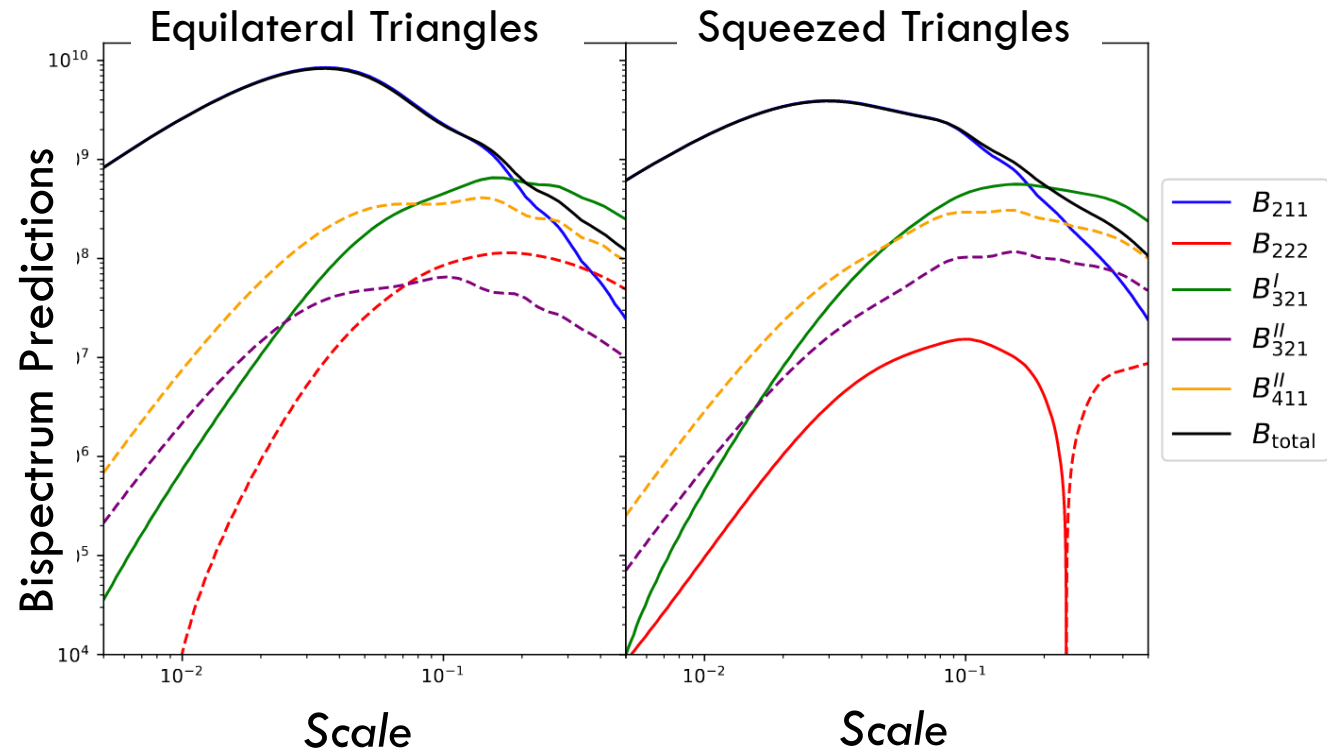
Problem: We don't have a good **theory** for the bispectrum

The bispectrum depends on

- ▶ **Early Universe** physics
- ▶ **Gravitational** evolution
- ▶ **Galactic** physics

Solution: Create a *new* theory model using Effective Field Theory

Depends on 10 cosmological parameters and 44 galaxy parameters

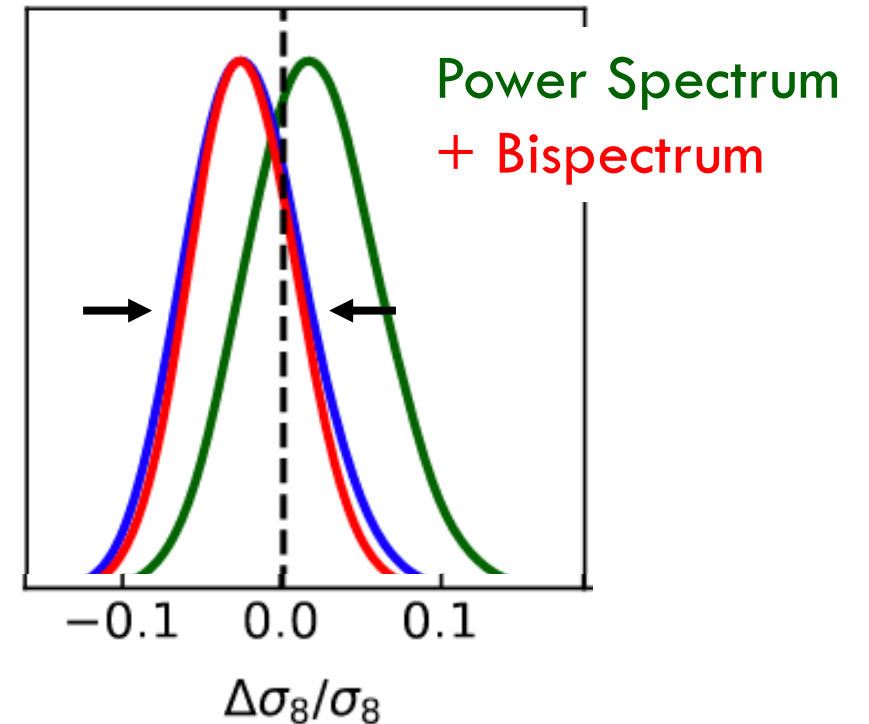


WHAT HAVE WE LEARNT FROM GALAXY TRIPLETS?

In the **standard** cosmological model, things don't improve much!

▷ Clustering strength measured clustering strength $\approx 15\%$ better

But, bispectra are **great** at probing **new physics** in the early Universe!

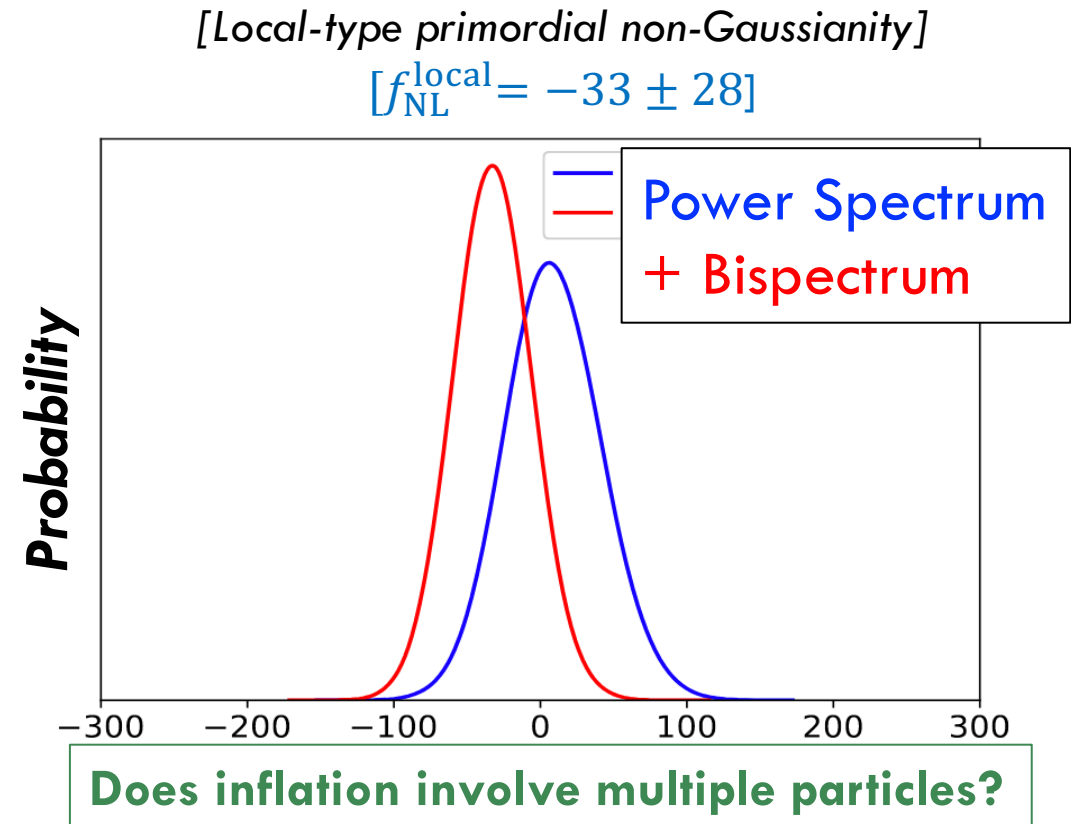


WHAT HAVE WE LEARNT FROM GALAXY TRIPLETS?

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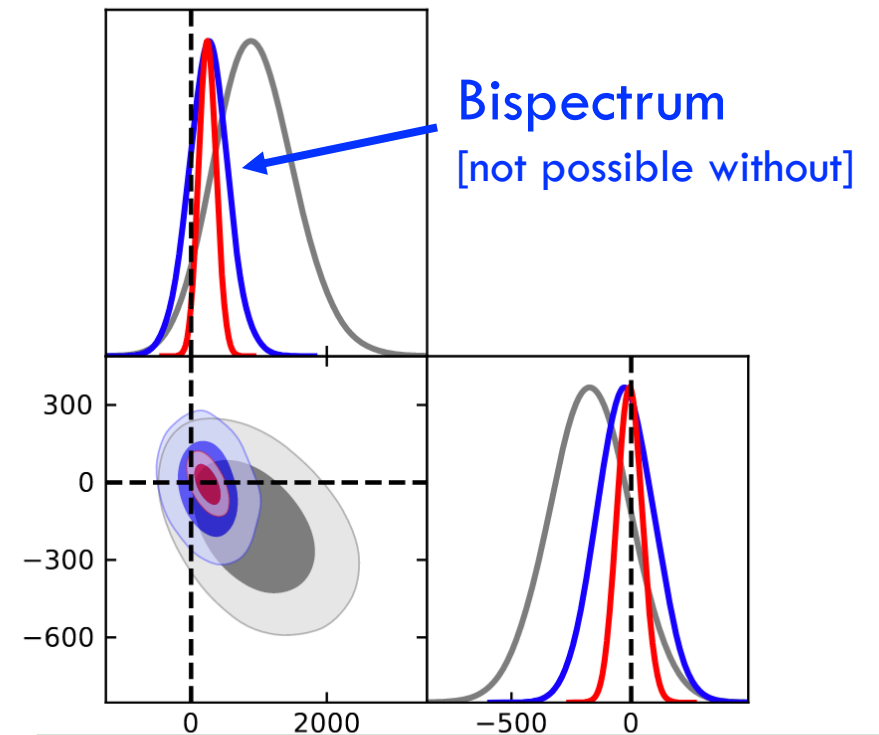
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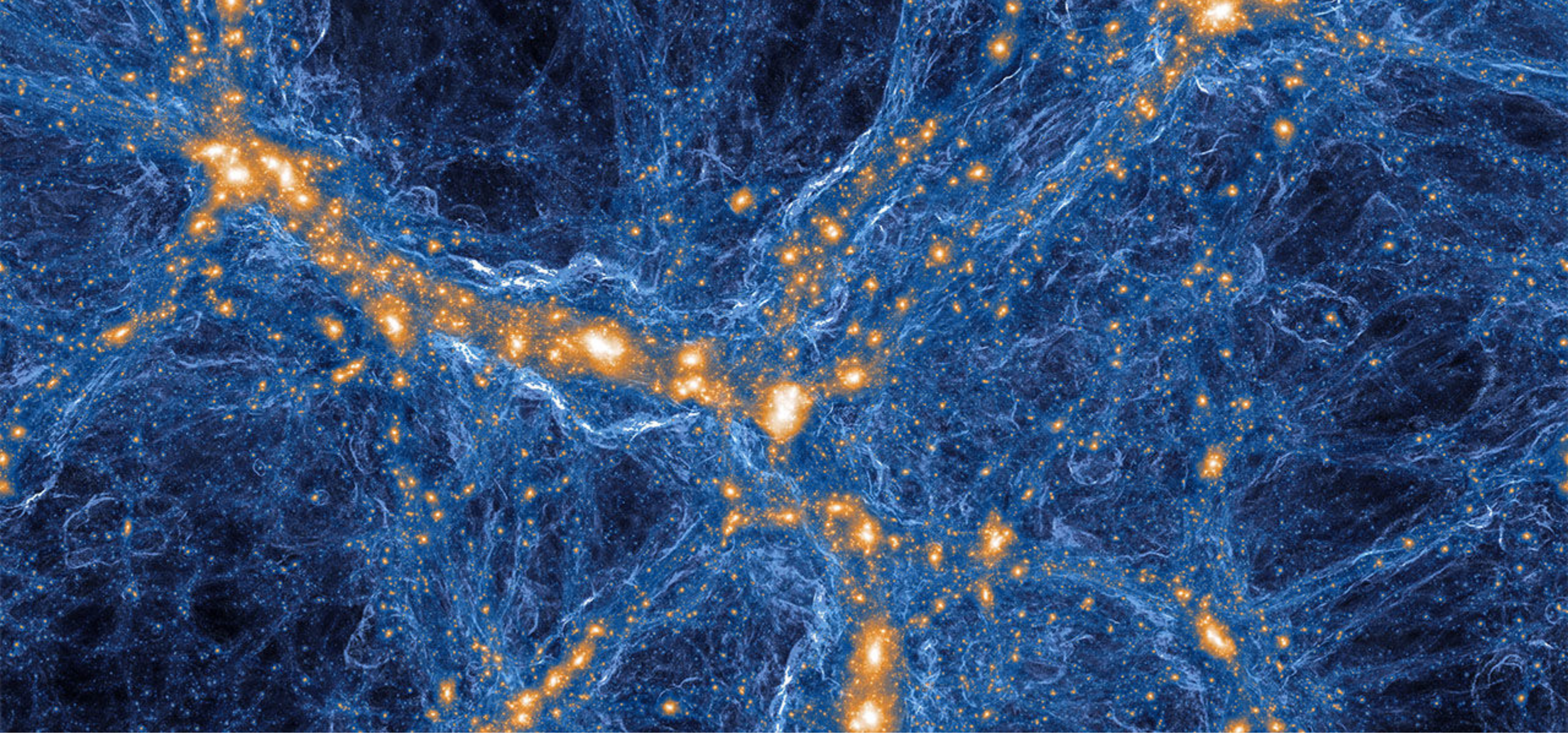
Constraints are **weak** compared to the CMB but will get **much** stronger soon!

[Non-local-type primordial non-Gaussianity]

$$[f_{\text{NL}}^{\text{equil}} = 260 \pm 300, f_{\text{NL}}^{\text{orth}} = -23 \pm 120]$$

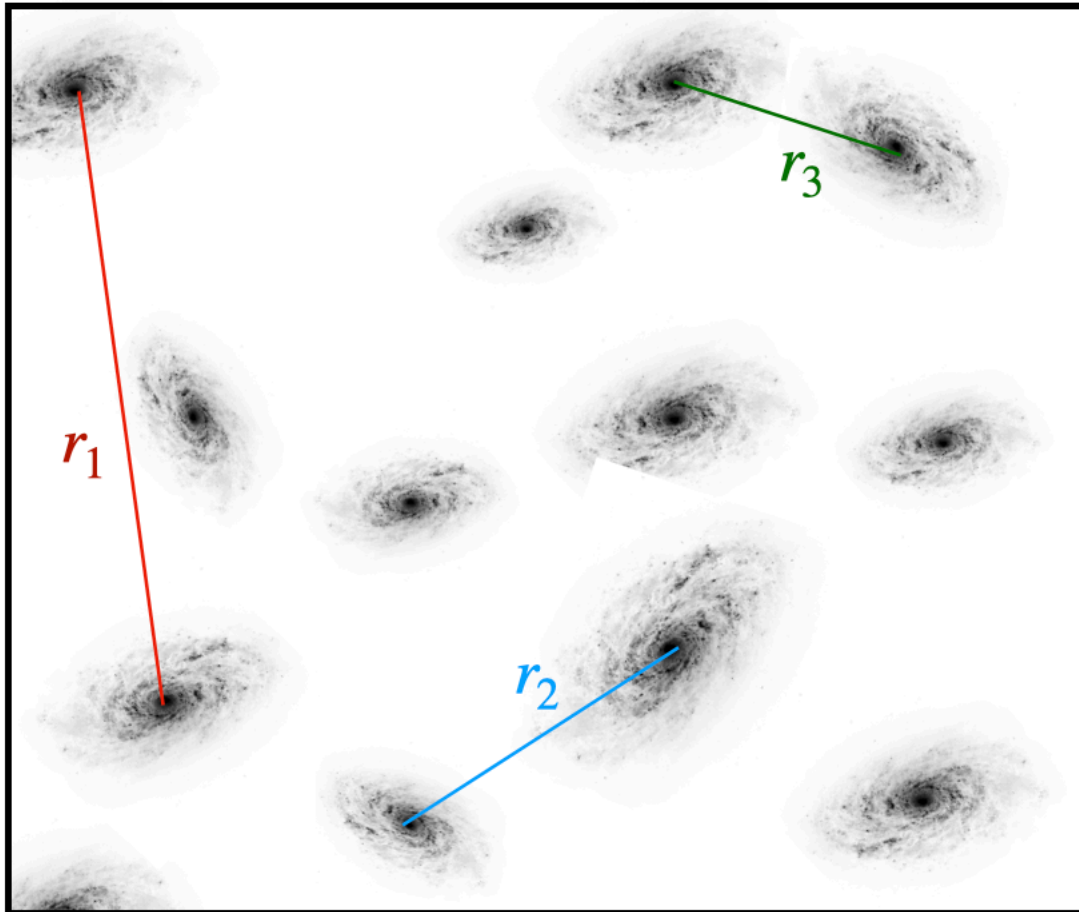


Is it one particle with weird physics?



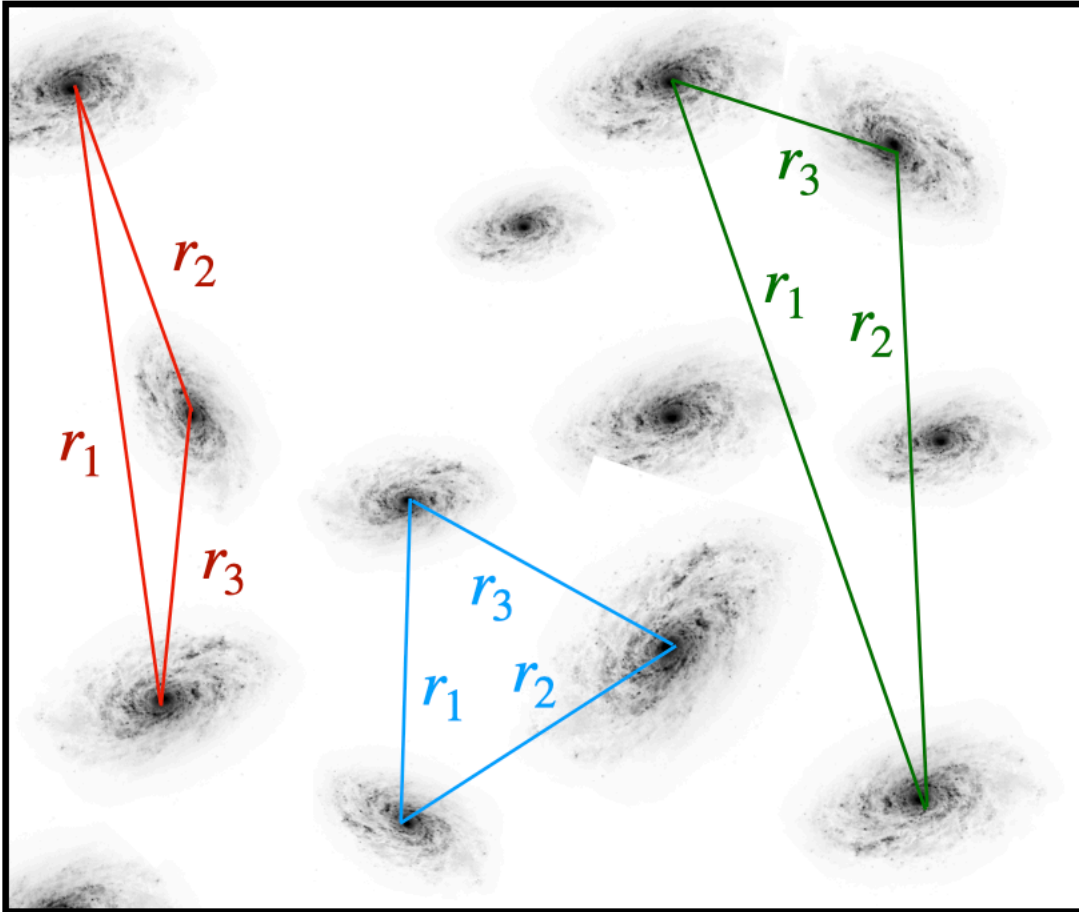
PART III: Cosmology with Galaxy Quadruplets

HOW DO WE DESCRIBE A GALAXY DISTRIBUTION?



The galaxy distribution is **not** fully described by **pairs** of points

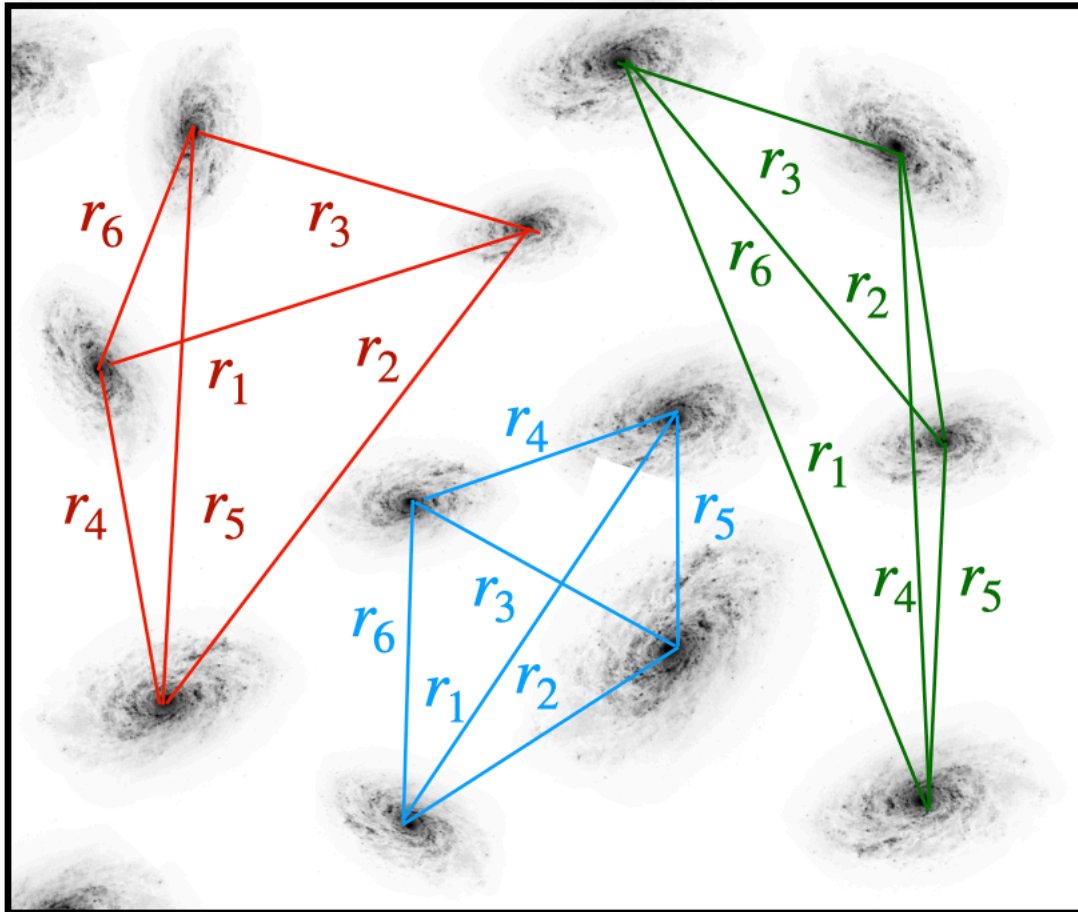
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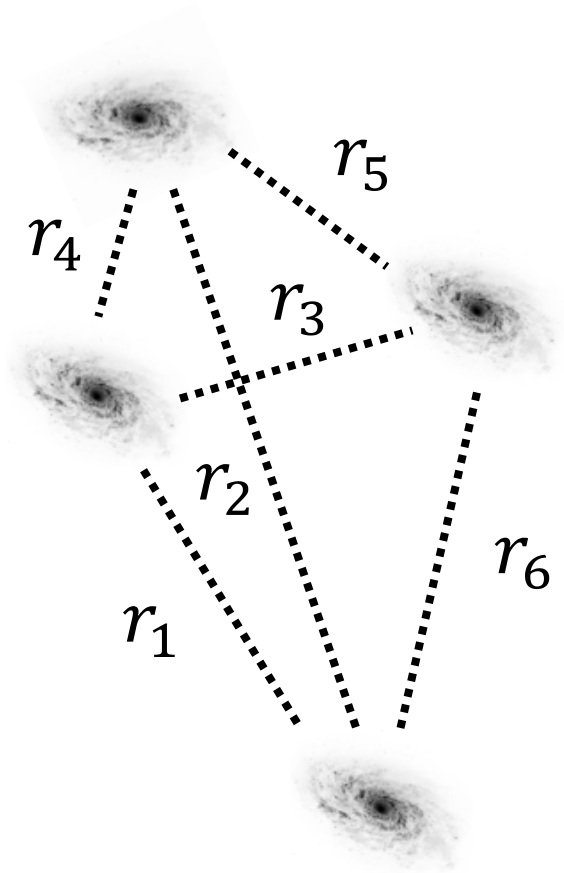


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It's also **not** fully described by **triplets** of points

What's the **distribution** of distances between **quadruplets** of galaxies?

FOUR-POINT STATISTICS

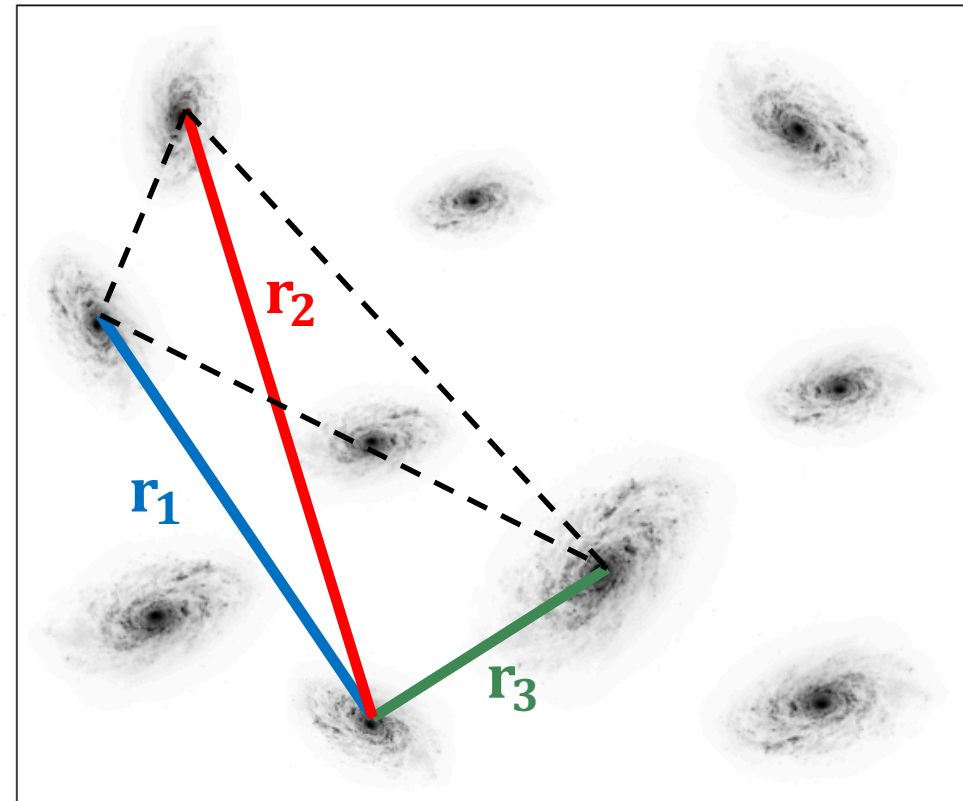


The **four-point correlation function** (or **trispectrum**)
=
Probability four galaxies make a **tetrahedron** with sides
 $r_1, r_2, r_3, r_4, r_5, r_6$

This traces **early Universe** and **gravitational** physics

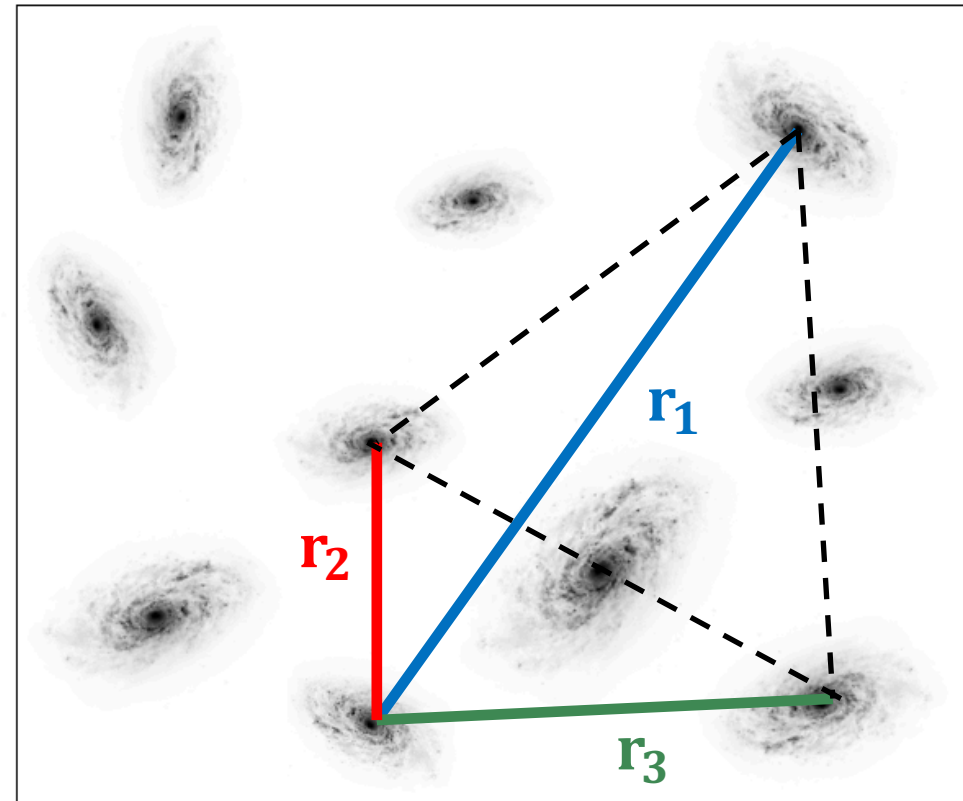
FOUR-POINT FUNCTIONS ARE HARD

Measuring the 4PCF involves counting **quadruplets** of galaxies



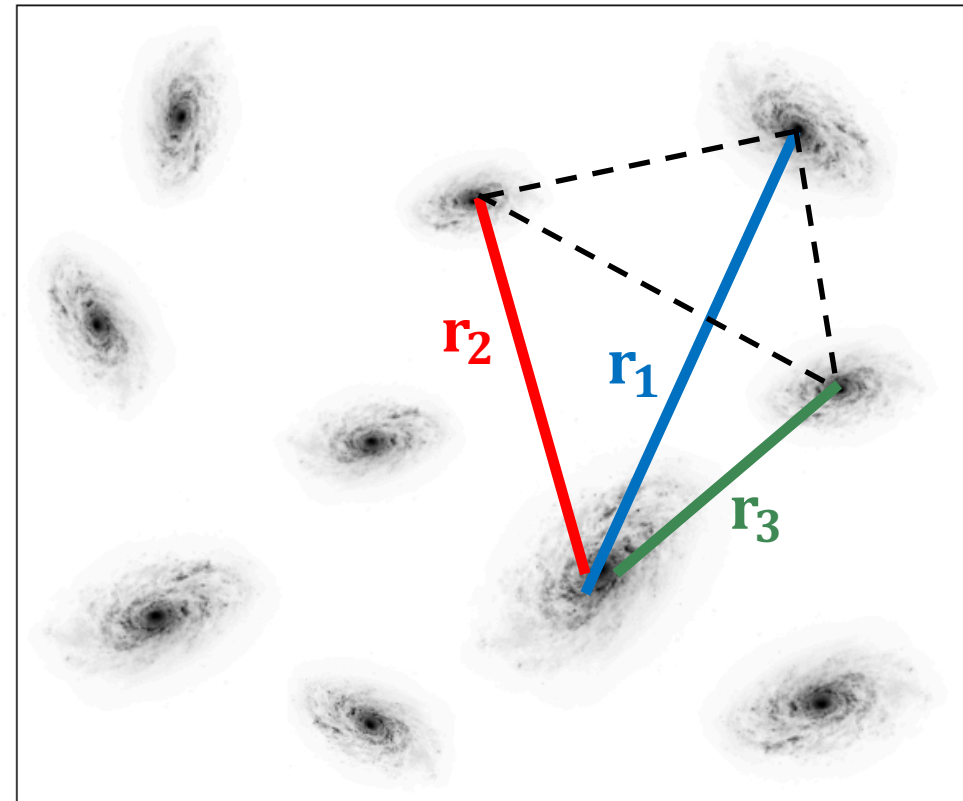
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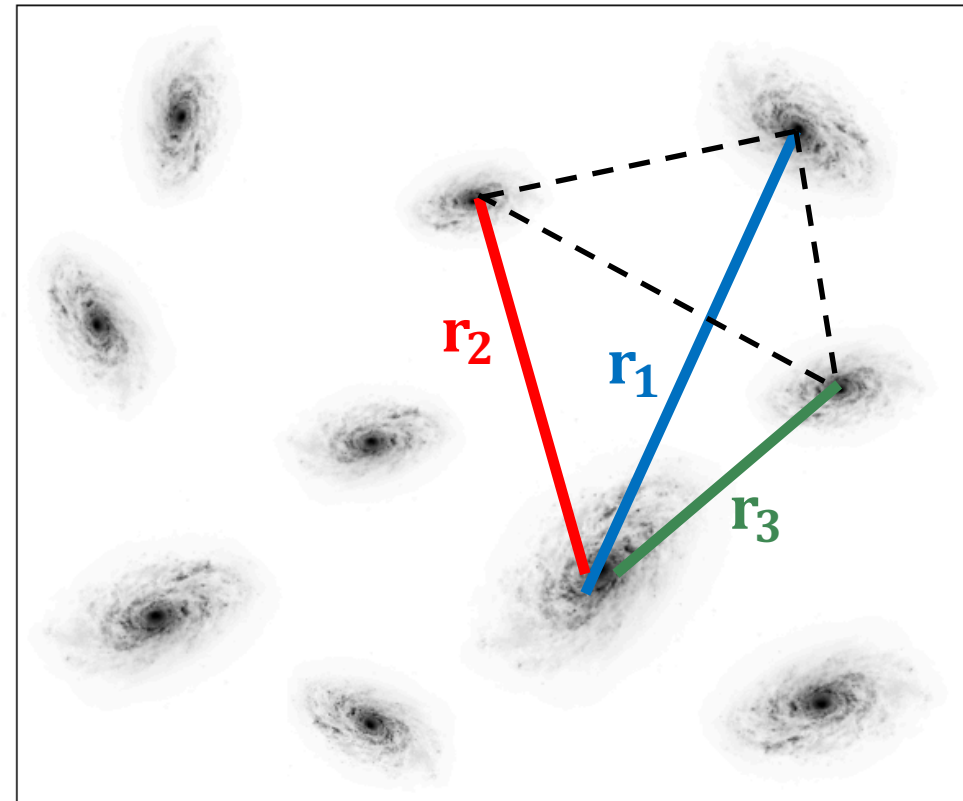


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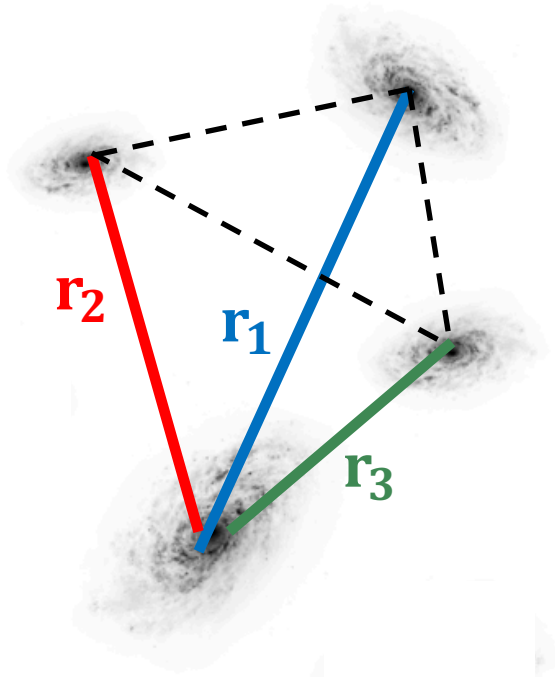
Measuring the 4PCF involves counting **quadruplets** of galaxies

With 1 000 000 galaxies, there are
1 000 000 000 000 000 000 000 000 000
combinations

We need a smarter method!

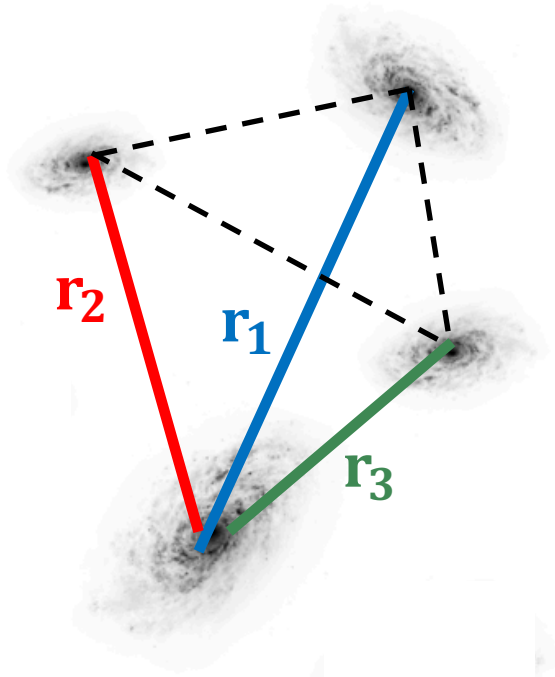


ONE TETRAHEDRON = THREE VECTORS



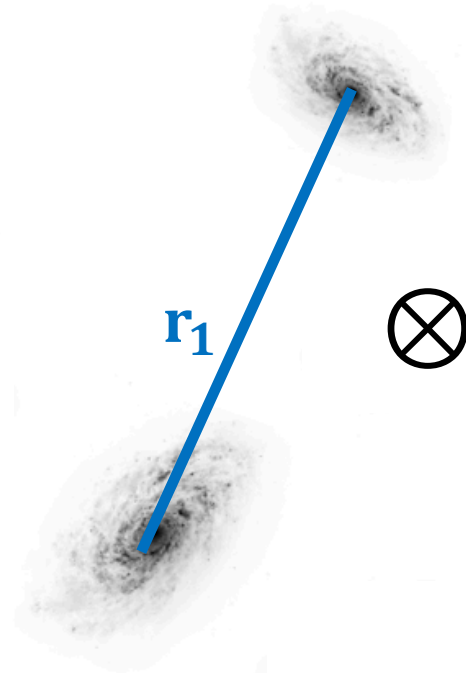
3 lengths + 3 angles

ONE TETRAHEDRON = THREE VECTORS

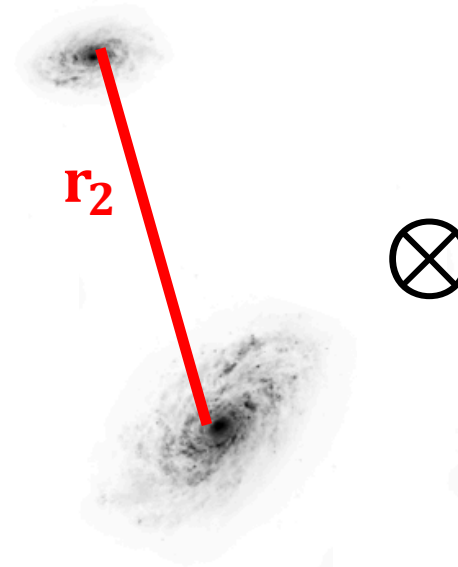


3 lengths + 3 angles

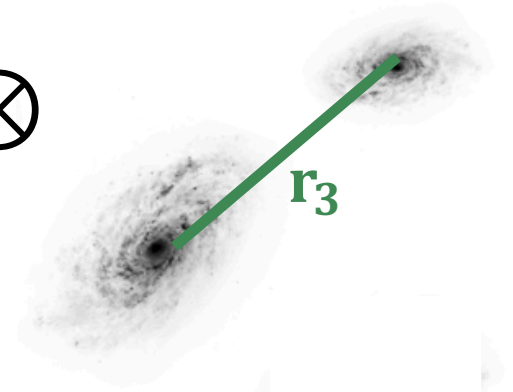
=



1 length + 1 direction

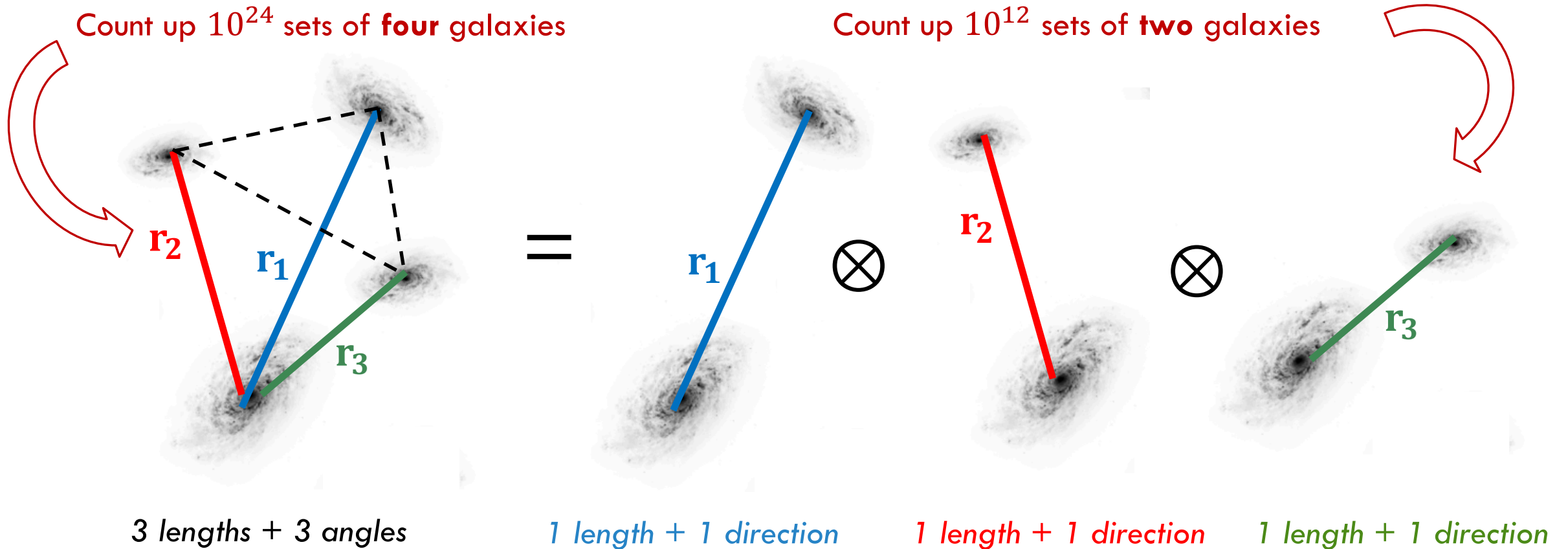


1 length + 1 direction



1 length + 1 direction

ONE TETRAHEDRON = THREE VECTORS

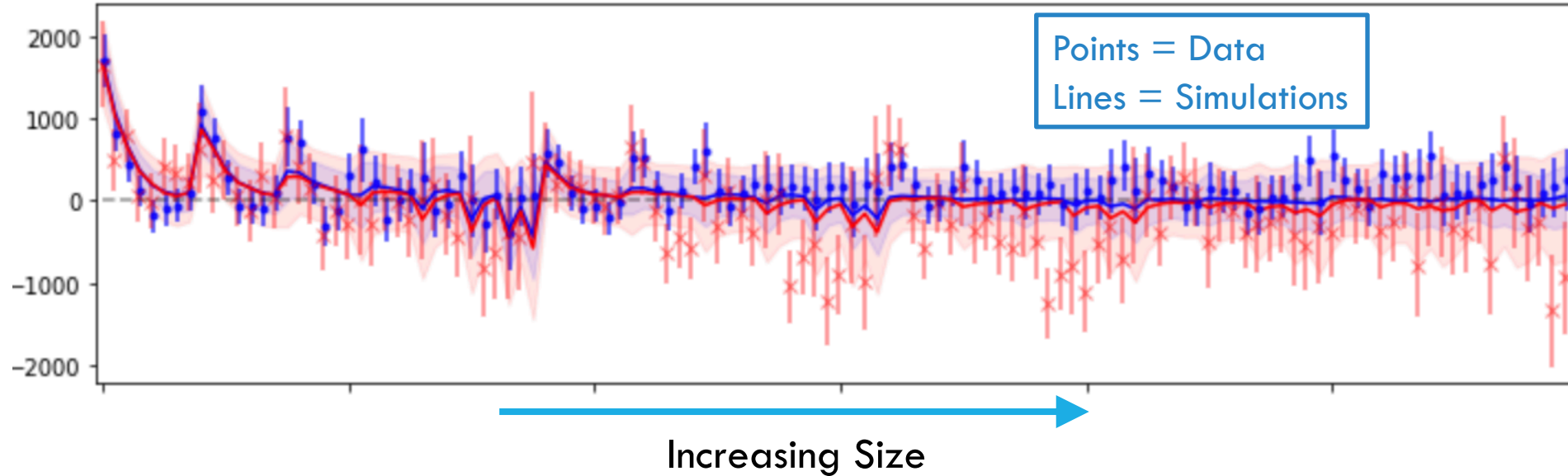


See [GitHub.com/oliverphilcox/encore](https://github.com/oliverphilcox/encore), [GitHub.com/oliverphilcox/NPCFs.jl](https://github.com/oliverphilcox/NPCFs.jl)

WHAT CAN WE LEARN FROM GALAXY QUADRUPLETS?

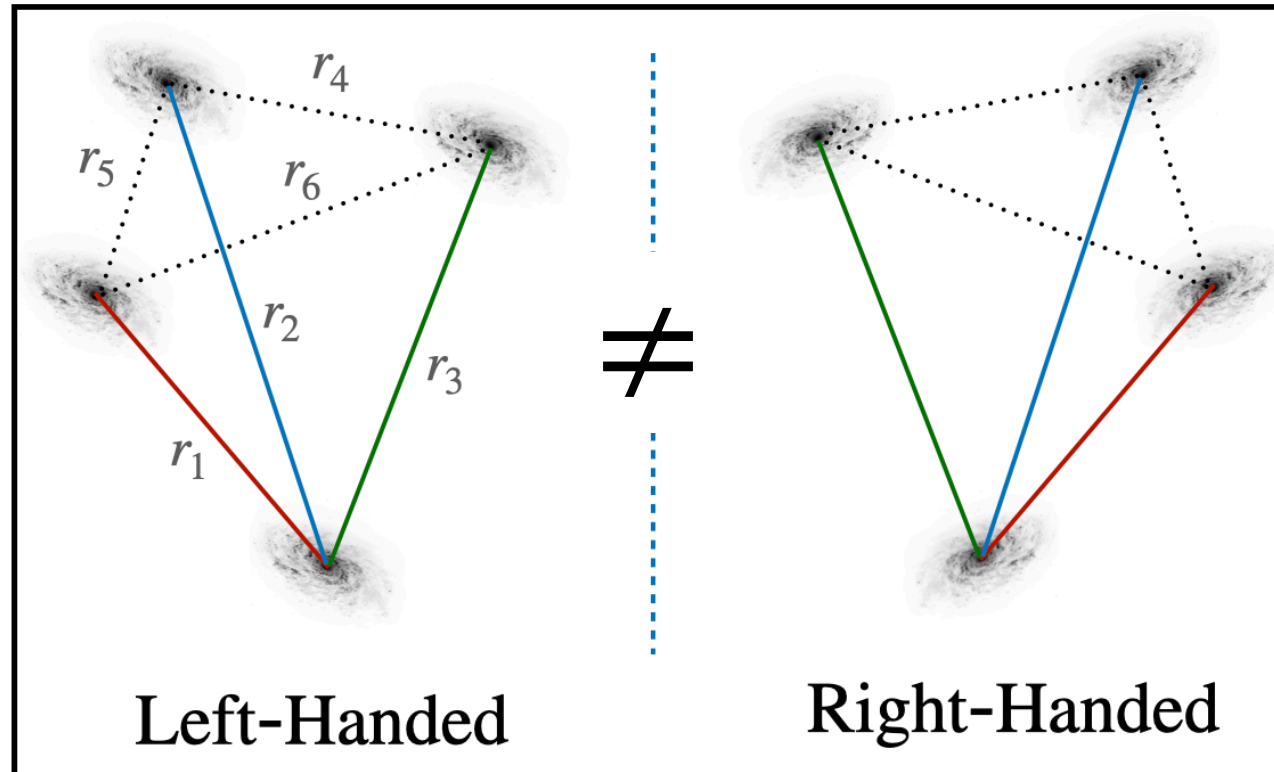
Can we measure a four-point correlation function in practice?

Four-Point Function of BOSS Galaxies



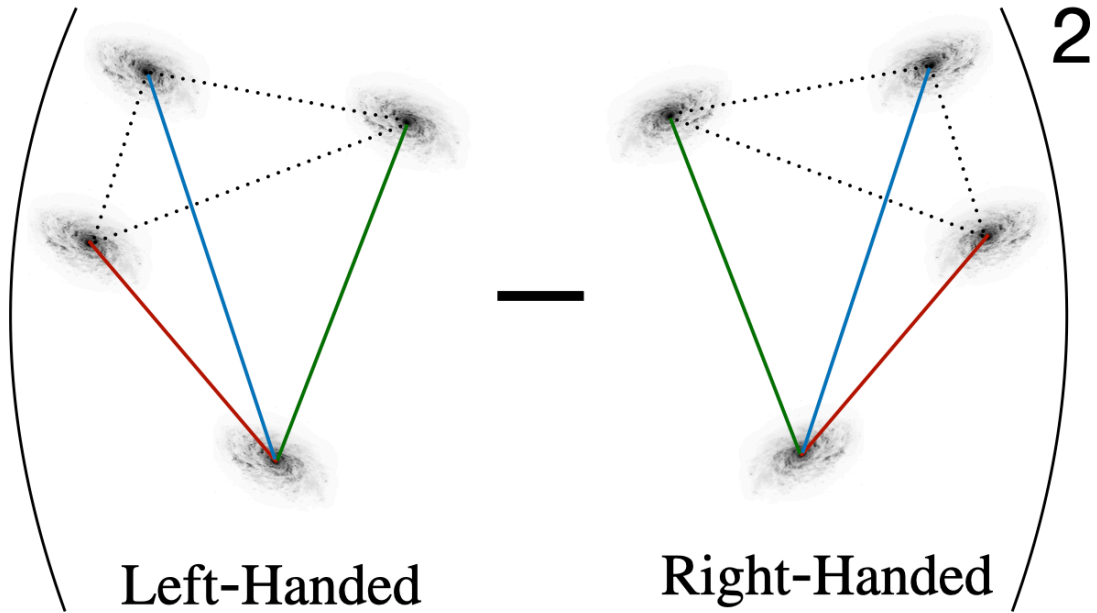
Strong detection of **gravitational** signature (at 8σ)
But, it's hard to understand theoretically!

FOUR-POINT FUNCTIONS PROBE MIRROR SYMMETRY

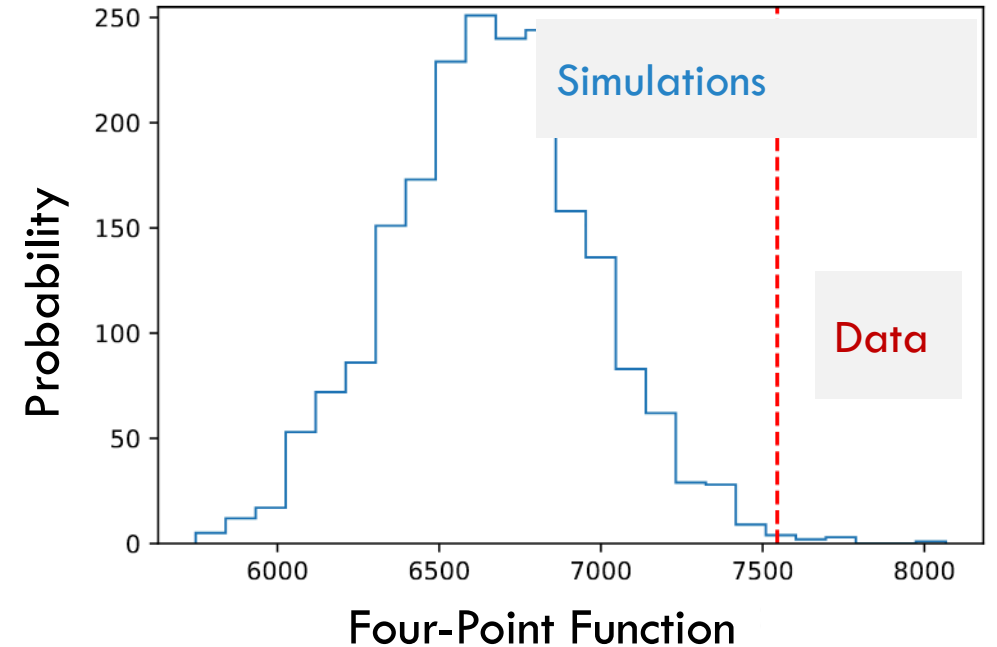
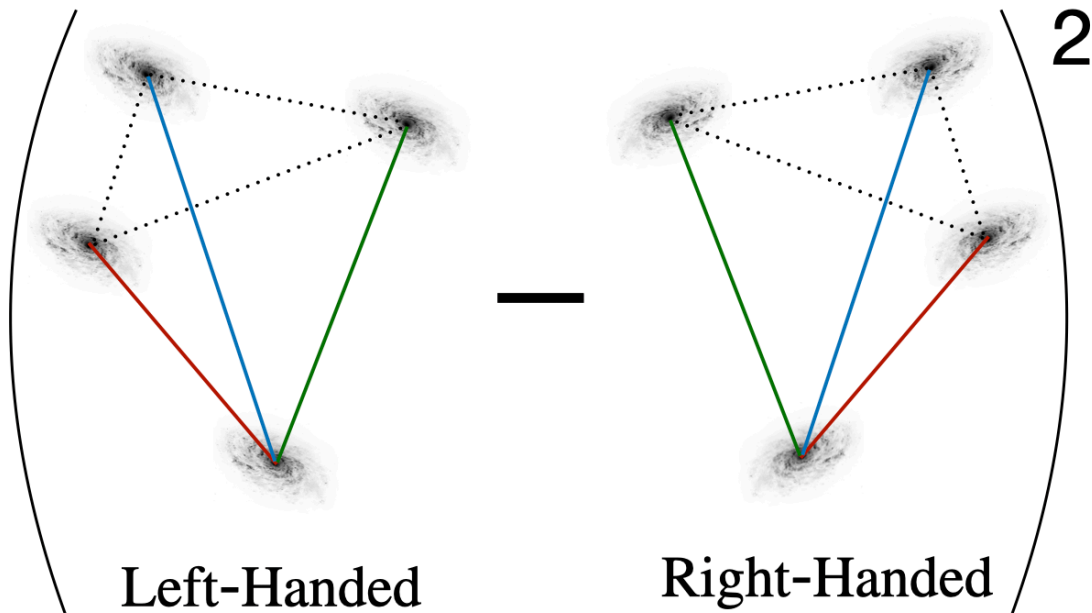


This is not true for two- and three-point functions!

DOES THE UNIVERSE BREAK MIRROR SYMMETRY?



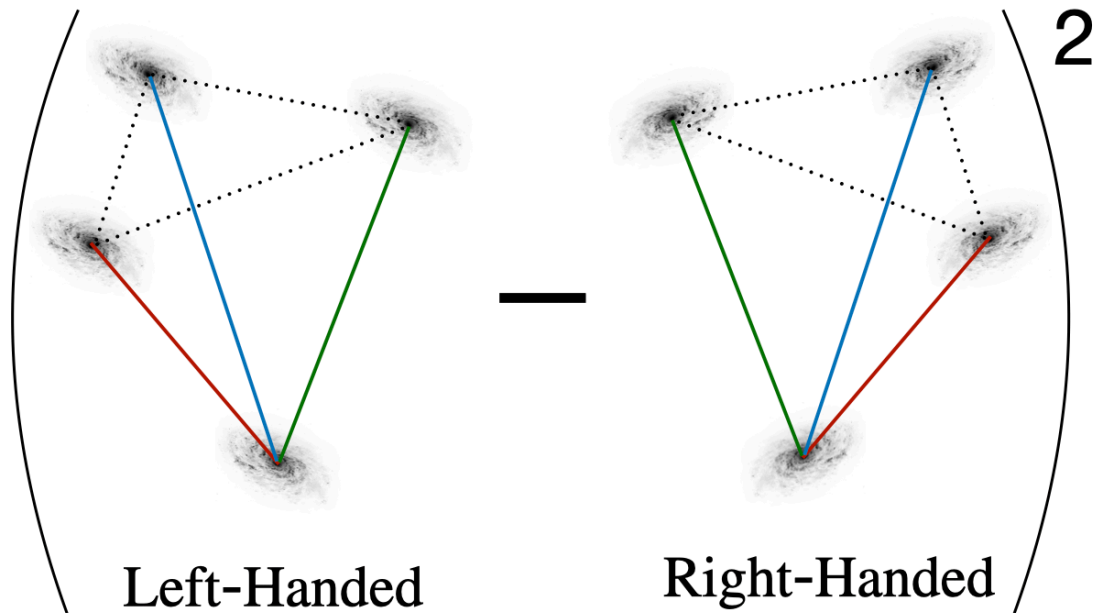
DOES THE UNIVERSE BREAK MIRROR SYMMETRY?



Interpretation:

- The **simulations** are not good enough
- There are weird things in the **data**
- The Universe is **not mirror-symmetric?**

DOES THE UNIVERSE BREAK MIRROR SYMMETRY?



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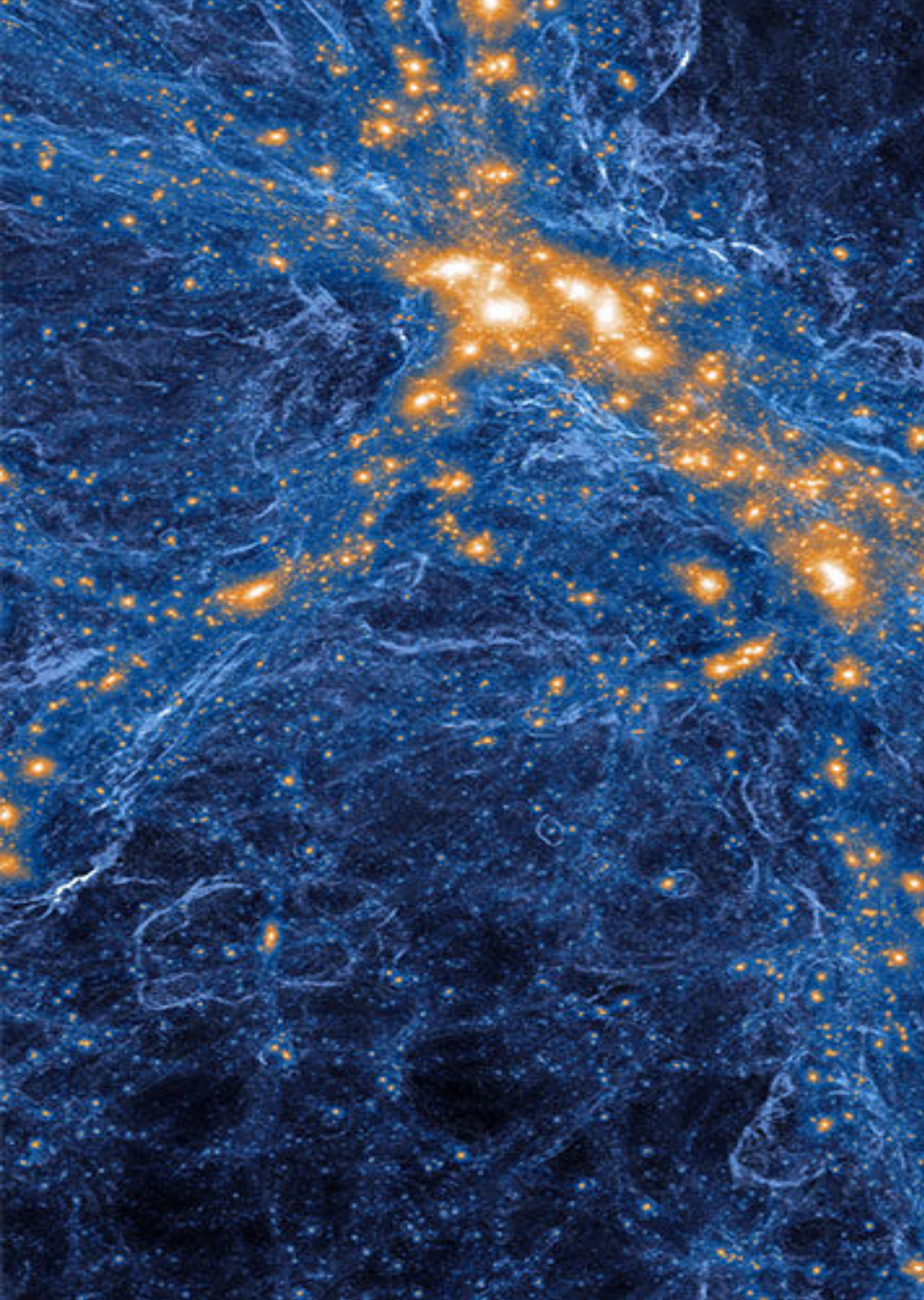
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The universe is surprisingly lopsided and we don't know why

Two analyses of a million galaxies show that their distribution may not be symmetrical, which may mean that our understandings of gravity and the early universe are incorrect

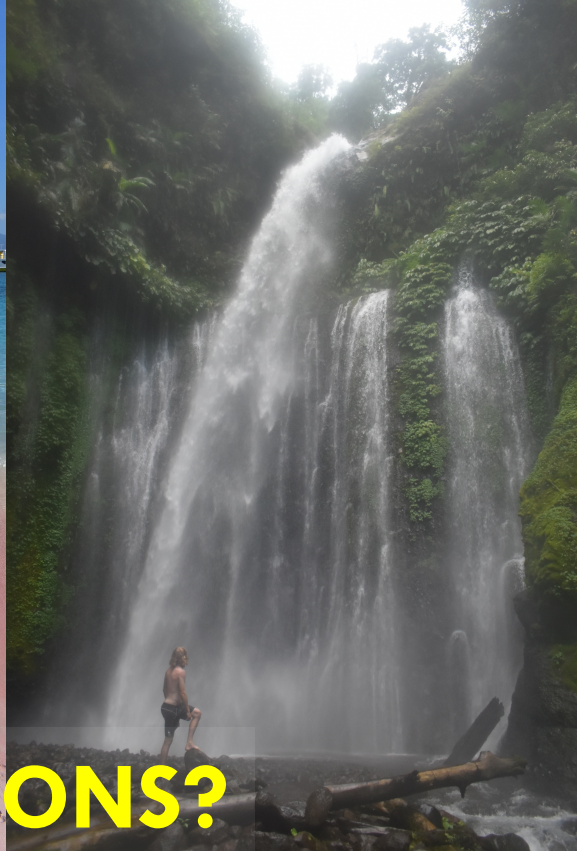
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- The **simulations** are not good enough
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CONCLUSIONS

- Galaxy **surveys** teach us about the Universe's **composition, structure, and history**
- We can now **measure, model, and interpret** analyze galaxy **pairs, triplets, and quadruplets**
- The future will see **better data, more statistics, and new physics!**



ANY QUESTIONS?